# PROGRESSIVE COLLAPSE ANALYSIS OF AN EXISTING BUILDING

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## ABSTRACT

This research study investigates an actual structure's potential to fail due to progressive collapse. Progressive collapse in a structure occurs when major structural load carrying members are removed suddenly, and the remaining structural elements cannot support the weight of the building and fail. This failure usually occurs in a domino effect and leads to a progressive collapse failure in the structure. The bombing of the Murray Federal Building in Oklahoma City is a typical example of progressive collapse failure. The initial bomb blast caused only 10% of the structure's damage, and the resulting progressive collapse failure lead to 90% of the structure's damage.

This experiment involved testing of a steel building scheduled for demolition in Northbrook, Illinois. The demolition team tore out four selected columns from the building to simulate the sudden column removal that leads to progressive collapse. The structure was instrumented with strain gauges that recorded the change in strain in various structural members while the columns were removed. The author instrumented the beams and columns in the building, managed the testing, and analyzed the recorded data.

The strain values recorded in the field were compared with the results from a computer model of the building. The model was created in a structural analysis program (SAP2000). The research is still underway, and the strain values recorded in the field and

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the computer model are being compared and analyzed. The percent error between the calculated and measured strains in a selected column was 21%.

The SAP2000 analysis conducted in this research was based on linear material properties. The numerical models and simulations will be expanded to include nonlinear effects and dynamic analysis. The ultimate goal of this ongoing progressive collapse research on real buildings is to develop better building evaluation and design guidelines for structural engineers to use to prevent progressive collapse in new and existing buildings. Future progressive collapse research recommendations are also presented. The instrumentation of strain gauges for optimum results is discussed, and column removal guidelines and linear displacement sensor instrumentation are also shown.

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## **CHAPTER 1**

## **1. INTRODUCTION**

#### 1.1 Overview

The progressive collapse of building structures is initiated when one or more vertical load carrying members (typically columns) is removed. Once a column is removed due to a vehicle impact, fire, earthquake, or other man-made or natural hazards, the building's weight (gravity load) transfers to neighboring columns in the structure. If these columns are not properly designed to resist and redistribute the additional gravity load, that part of the structure fails. The vertical load carrying elements of the structure continue to fail until the additional loading is stabilized. As a result, a substantial part of the structure may collapse, causing greater damage to the structure than the initial impact.

This research begins with the evaluation of the General Services Administration (GSA) Progressive Collapse Analysis and Design Guidelines (2003). The GSA guidelines provide general formulas and conditions that determine what members of a structure are susceptible to progressive collapse. Specifically, the demand-capacity-ratio (DCR) is used by the GSA guidelines to determine if individual members will fail leading to progressive collapse. This research analyzes and investigates the progressive collapse of an existing building using the 2003 GSA guidelines. The structure was a three story building located in Northbrook, Illinois. Built in 1968, the structure had reinforced concrete (RC) members in the basement, concrete slabs for the flooring, and was composed of steel framing on the first and second floors. The sixth edition of the AISC

Steel Construction Manual (1963) was used to design the structure, and the building was scheduled for demolition in early August, 2008.

Following a predetermined testing procedure (developed following the GSA guidelines), the demolition team removed four columns from the existing structure. In order to measure the strains in various columns and beams, the structure was instrumented with strain gauges prior to the column removals. As each column was removed, the strain gauges captured the data that is later analyzed and compared with the analysis results from the computer program SAP2000 (2008).

The Structural Analysis Program (SAP2000) is a powerful computer program used to design and analyze various structures. The program analyzes two dimensional linear static models to three dimensional nonlinear dynamic models. This study involves linear elastic static analysis of the structure. The data obtained from the strain gauges on the actual structure during the demolition is then compared to the analysis results of the linear static model in SAP2000.

The strain measured from the strain gauges in the field is used to understand the response of the structure during and after column removals. The load distributions, change in strains, and bending moments generated from each column removal are calculated from the measured strain values collected in the field. The load distributions, change in strains, and bending moments generated from each column removal are also calculated and compared in the SAP2000 computer simulation. This research study analyzes the data collected in the field and compares it to the SAP2000 simulation results to verify the GSA guidelines.

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#### **1.2 Scope and Objectives**

The focus of this research is to determine if a structure is susceptible to progressive collapse. The recorded strain values are analyzed, and compared with the results from SAP2000 computer model of the building. The accuracy of the measured strains and SAP2000 analysis is also discussed. Using SAP2000, the structure's potential for progressive collapse was determined. The theory and instrumentation of strain gauges and sensors is discussed. Guidelines for column removal in future experiments of existing buildings are developed.

The objectives of this experiment are:

- Describe the progressive collapse experiment conducted
- Analyze the strain values recorded by the strain gauges in the field
- Determine the Demand-Capacity Ratios (DCR) using SAP2000
- Compare the recorded strains with the strains obtained from SAP2000 analysis
- Discuss instrumentation plans for most beneficial results
- Discuss guidelines for column removals in future tests

## **1.3 Literature Review**

This experiment was influenced by two previously published research studies. Sasani and Sagiroglu (2007) reported experimental and analytical data from the testing of a building located in San Diego, California. Their research studied the progressive collapse potential of Hotel San Diego. The Hotel San Diego building was instrumented with similar strain gauges to measure the strain as two of the exterior columns were removed. The research conducted by Sasani and Sagiroglu (2007) gave valuable insight on how a structure would respond when faced with abnormal conditions. This research study also discussed the GSA (2003) guidelines, but did not calculate the DCR values for each member. The data recorded was purely field data, lacking a computer model simulation.

Another influential research study was conducted by Sezen and Song (2008) to test the progressive collapse potential of the Ohio State Union scheduled for demolition in 2007. Sezen and Song (2008) followed the GSA (2003) guidelines and calculated the DCR values as four exterior columns were removed from the structure. The computer program SAP2000 was used in the study to generate a computer model simulation of the Ohio State Union. Their research compared the predicted and calculated building responses using the GSA (2003) as a guideline.

## **1.4 Scope and Organization**

The research thesis begins with an introduction discussing related progressive collapse analysis literature. Chapter 2 provides the detailed building description and geometry of the structure. Chapter 3 addresses the instrumentation details and the testing procedure for column torching and removal, showing the data collected from the strain gauges as each column is torched and removed. Chapter 3 also analyzes the load distributions, change in strain, and change in the bending moment. Chapter 4 discusses the GSA guidelines for progressive collapse as they pertain to the data collected. Chapter

5 examines the SAP2000 analysis to determine the actual DCR values of the members. Chapter 6 develops a general guideline to advise the placement of sensors in order to obtain the most beneficial data measurements for future experiments. Finally, Chapter 7 provides the summary and conclusions for the research.

## **CHAPTER 2**

## 2. BUILDING AND EXPERIMENT DETAILS

#### 2.1 Building Description

The Bankers Life and Casualty Company insurance building, located in Northbrook, IL, was constructed in 1968 following the 6<sup>th</sup> edition of AISC Steel Construction Manual (1967) design code. The building had nine bays spanning 27 ft wide in the longitudinal direction, and 8 bays spanning 23 ft-6 in. in the transverse direction as shown in Figure 2.1. The basement and first story are 10 ft-6 in. and 20 ft-6 in. in height, as shown in Figure 2.2. The heights of the lower and high points of the second story are 14 ft-8 in. and 15 ft-2 in., respectively. Figure 2.3 shows the beam and column designation for the structure.

A large loading dock bay area is located at the far Northwest corner of the structure. In addition, a mezzanine level exists between the first and second floors at the Southeast and Southwest end of the structure. For this research, the docking bay and mezzanine level were not considered, because neither would affect the experiment. Also, the plans available do not include a recent addition of two stairwells at the south end of the building. This addition does not have any effect this study. Figures A.1 through A.9 in Appendix A contain the original structural drawings and design notes for the building.

The columns in the basement are reinforced concrete (RC) with a compressive strength of 4000 psi. The steel reinforcing bars had a specified yield strength of 75,000 pounds per square inch (psi). Figure A.5, in Appendix A, shows the typical exterior

column section detail. The steel columns, with a yield stress of 36,000 psi, were rigidly connected to the RC columns at the first floor level. The steel girders and beams had a specified yield stress of 42,000 psi. The steel girders, beams, and columns were connected with a simple connection.

## 2.2 Experiment Information

The entire experiment involves recording the strain on various structural members as four columns are removed from the North side of the building shown in Figures 2.4 and 2.5. The Environmental Cleansing Corporation was hired to demolish the Bankers Life and Casualty Company insurance building. They agreed to help with the study, tearing out the four columns as specified in this research using GSA (2003) as a guideline. Figure 2.5 highlights the four columns selected for removal.

Prior to removing the columns, the demolition team tore down the second floor near the Northwest corner of the structure due to a miscommunication between the owner and the demolition team. As a result, all of the building materials remained on the second floor concrete slab. The joists, bridging joists, roofing, bricks, tie rods, and concrete masonry units (CMU) created a rubble mass on the second floor slab. This rubble spans the area of four bays east from the northwest corner and approximately two bays south, resulting in a slightly different loading scenario for the four columns nearest the Northwest corner. Figures 2.6 and 2.7 show the rubble mass at the North side of the building.



Figure 2.1- Dimensions for the Second Floor of the Bankers Life and Casualty Company Building and Experiment Location is Highlighted in Blue.

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Figure 2.2- Elevation of North End Frame of the Bankers Life and Casualty Company Building.

Beam Number	Beam Type	Column Number	Column Type
1	RC Flat Slab	1C	RC
2	RC Flat Slab	2C	RC
3	RC Flat Slab	3C	RC
4	RC Flat Slab	4C	RC
5	RC Flat Slab	5C	RC
6	RC Flat Slab	6C	RC
7	RC Flat Slab	7C	RC
8	RC Flat Slab	8C	RC
9	RC Flat Slab	9C	RC
10	24 I 79.9	10C	RC
11	21 WF 62	11C	10 WF 49
12	21 WF 62	12C	10 WF 72
13	21 WF 62	13C	10 WF 72
14	21 WF 62	14C	10 WF 72
15	21 WF 62	15C	10 WF 72
16	21 WF 62	16C	10 WF 72
17	21 WF 62	17C	10 WF 72
18	21 WF 62	18C	10 WF 72
19	18 WF 45	19C	10 WF 72
20	18 WF 45	20C	10 WF 72
21	18 WF 45	21C	8 WF 31
22	18 WF 45	22C	8 WF 31
23	18 WF 45	23C	8 WF 31
		24C	8 WF 31
		25C	8 WF 31
		26C	8 WF 31

Figure 2.3- Beam and Column Designation of the Bankers Life and Casualty Company Building Corresponding with Figure 2.2.



Figure 2.4- North Side of Bankers Life and Casualty Company Building.



Figure 2.5- The Circled Columns on North Side of the Building were Removed During the Experiment.



Figure 2.6- The Rubble Mass is Circled on the North Side of the Bankers Life and Casualty Company Building.



Figure 2.7- Close Up View of the Rubble at the North Side of the Building.

## **CHAPTER 3**

## **3. INSTRUMENTATION AND TESTING PROCEDURE**

#### **3.1 Instrumentation and Column Removal Process**

Chapter 3 discusses the placement of strain gauges on the structural members on the North side of the building. This chapter briefly explains how the strain gauges record data and their locations on the structure shown in the tables and graphs to follow. The results are used to determine which members have progressive collapse potential. Alternative column removal processes are also discussed for comparison. In addition, Chapter 3 describes the testing procedure and methodology for the experiment, exhibiting the columns removed, the removal method, and the data collection.

## 3.2 Instrumentation

The strain gauges attached to the columns and beams are universal generalpurpose strain gauges with a resistance of  $120 \pm 0.3\%$  Ohms, and have a strain range of  $\pm 3\%$ . They measure the strain in the Z direction caused by the compressive and tensile forces displayed in Figure 3.1. A set procedure was used to install the strain gauges on each column and beam.

The demolition team first exposed the columns and beams by removing the exterior brick wall. Then, the surface of the columns and beam were grinded down to remove all paint and debris. Next, a degreaser, conditioner and a neutralizer were applied

to the clean surface before attaching the strain gauges using an adhesive. The strain gauges were then covered with a strain gauge shield to protect against debris. Figure 3.2 shows a strain gauge attached to a column protected with a cover shield.

A total of nine strain gauges were used in the experiment, eight were attached on the columns and one was attached to a beam. Figures 3.3 and 3.4 display the Columns 13C, 14C and 17C instrumented with two strain gauges each approximately 6 ft from the bottom. One strain gauge was placed on the East facing web, and one strain gauge was placed on the North exterior facing flange. Columns 12C and 16C were each instrumented with one strain gauge on their Northern exterior facing flanges (Table 3.1 lists the locations of the strain gauges used).

The strain gauge attached on Beam 10 measured the strain in the Z direction caused by the bending moment. Due to very tall heights, only Beam 10 was instrumented with a strain gauge on the exposed bottom face of the flange approximately 1 ft-6 in. from the left of the beam. This bending moment along the length of Beam 10 is caused by the weight of the structure shifting as each column is removed.

#### **3.3 Testing Procedure**

The strain gauges were attached to a portable data acquisition scanner system and laptop. Figure 3.5 displays the computer station set up at the demolition site. During the column removal process, the computer measurement scanner and laptop recorded all nine strain gauge readings simultaneously. The strain values were recorded every tenth of a second during the column removal. Unfortunately, during the experiment several

columns were knocked as the bricks were being removed around each column, causing certain strain gauge readings to spike suddenly. The data collected takes into account these sudden changes in strain during the entire column removal process.

During the column removal process, each column was weakened by a blow torch prior to its removal for safety reasons. During the torching process, the demolition team melt nearly through each column's cross section at two points above the strain gauges. The distance between the torched lines on each column was approximately two to three feet. The demolition team then melted a hole in the Northern facing flange of each column between the torched lines. A chain was then attached to the hole, and the column was pulled out by a large backhoe. Figure 3.6 shows a torched column with a chain attached.

Figure 3.7 shows the North side of the structure and the order that each of the four columns was torched and removed. Column 15C was torched first, Column 16C was second, Column 12C was third, and Column 11C was fourth. After the four columns were torched, the removal process began. The columns were removed in the same order, but Column 11C was removed third, and Column 12C was removed fourth. The time span between the torching and removing of the columns was relatively short to simulate a more realistic immediate removal. Figure 3.8 shows Column 16C being torched, Figure 3.9 shows Column 16C removed, and Figure 3.10 shows Column 11C being removed.

### 3.4 Strain Gauge Data Measured During Column Removals

The strain variation was recorded by the nine strain gauges during the entire column removal process. Strain is a unitless value calculated using Equation 3.1.

$$\varepsilon = \frac{\Delta L}{L} \tag{3.1}$$

where  $\Delta L$  is the change in length of a structural member, and *L* is the original length of the structural member. A positive strain value means the structural member elongates and is in tension, and a negative strain value means the structural member contracts and is in compression. Figures 3.11-3.13 display the strain versus time graph of the strain gauge 7 attached to Column 14C. The graph shows the strain values generated from the four columns being torched and removed. The most important observations from Figure 3.11 occur between 2141-2870.5 seconds. There is a sudden compressive strain increase of  $65*10^{-6}$  indicating the torching of Column 16C resulted in additional axial loads on Column 14C. Further implications of the measured strain data are investigated in the next few sections and Chapter 4.

Figures B.1 through B.3 in Appendix B show the strain versus time graphs for all nine strain gauges attached to the structure. Each graph highlights when each column was torched, knocked/poked, and removed. Strain gauge 5 was hit by the demolition team's backhoe approximately 1620 seconds into the experiment and was severed.

## 3.5 Load Redistribution During Column Torching and Removal

As each column was torched and removed, the remaining columns and beams must resist a new gravity load to support the building. This additional loading, caused by the redistribution of the building's weight to neighboring columns and beams, creates new additional stress in the structural members. The new stress is due to the combination of axial loading and a bending moment.

The axial loading is a concentrated force, from the live and dead loads in the building, acting at the center of the structural member's cross section. The axial loading generates a compressive or tensile axial stress in the structural member. The bending moment is generated by the weight of the structure acting not directly at the structural member's cross section center. The bending moment generates a bending stress in the structural member. The total stress generated in each column and beam can be calculated from the following equations. The first equation is for axial stress,  $f_a$ . Axial stress can be calculated using Equation 3.2.

$$f_a = \frac{P}{A} \tag{3.2}$$

where *P* is the weight load from the structure and *A* is the cross sectional area of the column or beam. The second equation is for the stress created from the bending moment. The bending stress,  $f_b$ , is calculated using Equation 3.3.

$$f_b = \frac{M \cdot c}{I} \tag{3.3}$$

where M is the bending moment, c is the distance from the neutral axis to top or bottom of structural member, and I is the moment of inertia given for a structural member.

The total stress generated in each column and beam is found by combining Equations 3.2 and 3.3 to create Equation 3.4.

$$f_{total} = \frac{P}{A} + \frac{M \cdot c}{I}$$
(3.4)

where  $f_{total}$  is the total stress generated in each column and beam under combined action of axial load in bending moment.

The total strain generated from the column removals can be found using a modified Equation 3.4. Equation 3.5 relates stress to strain in the elastic range.

$$\varepsilon = \frac{f_{total}}{E} \tag{3.5}$$

where  $\varepsilon$  is the strain and *E* is the modulus of elasticity for a given structural member. The total strain generated can be found from Equation 3.6 when  $f_{total}$  is solved for in Equation 3.5 and combined with Equation 3.4.

$$\varepsilon = \frac{P}{E \cdot A} + \frac{M \cdot c}{E \cdot I} \tag{3.6}$$

As the strain changes in Equation 3.6, *P* and *M* values will also change. Equation 3.7 relates the change in strain to changes in *P* and *M*.

$$\Delta \varepsilon = \frac{\Delta P}{E \cdot A} + \frac{\Delta M \cdot c}{E \cdot I}$$
(3.7)

where  $\Delta \varepsilon$  change in strain,  $\Delta P$  is the change in axial load, and  $\Delta M$  is the change in bending moment.  $\Delta \varepsilon$  can be the change in strain recorded from the strain gauges in the field.

If Equation 3.7 is solved simultaneously for two strain gauges attached at the same elevation on a structural member,  $\Delta M$  and  $\Delta P$  can be calculated using  $\Delta \varepsilon$  for the

two strain gauges. Chapter 6, Section 6.5 gives more detail about strain gauge placement and solving Equation 3.7 correctly. Figure B.4 in Appendix B shows the strain values at specific times for all nine strain gauges. Figure B.5 in Appendix B shows a graphical example where  $\Delta \varepsilon$  was measured from.

Beams on a structure typically will be subjected to very small or no axial load. Therefore, Equation 3.7 becomes Equation 3.8 for beams not carrying an axial load.

$$\Delta \varepsilon = \frac{\Delta M \cdot c}{E \cdot I} \tag{3.8}$$

Equation 3.8 can be solved directly for any strain gauge attached to a beam since  $\Delta P$  equals zero. Due to extreme heights, Beam 10 was the only beam accessible to be instrumented with a strain gauge. The change in moment values ( $\Delta M$ ) and the total change in moment can be found in Figure B.6 in Appendix B for Beam 10. The total change in moment,  $\Delta M$ , is measured from a starting strain of zero to the final strain value at the removal of the last column, Column 12C.

## 3.6 Load Redistribution Analysis from Strain Gauge Readings

The maximum axial load a column can endure before failure is found using Equation 3.9, assuming the applied moments are relatively small.

$$P_y = f_y \cdot A \tag{3.9}$$

where  $P_y$  is the maximum axial load capacity,  $f_y$  is the yield stress, and A is the cross sectional area of the column or beam. The maximum axial load capacity can be found using Equation 3.10.

$$P_{max} = P_{existing} + \Delta P \tag{3.10}$$

where  $P_{max}$  is the maximum applied axial load capacity,  $P_{existing}$  is the original/existing load on the column or beam caused from the weight of the structure, and  $\Delta P$  is the change in loading caused by column removal.  $P_{max}$  is limited by  $P_y$  ( $P_{max} \leq P_y$ ).

The  $\Delta P$  can be calculated using Equation 3.7, and the  $P_{existing}$  on the columns will be analyzed in Chapter 5 using the computer program SAP2000. Using the  $\Delta P$  recorded in the field and the  $P_{existing}$  calculated in SAP2000,  $P_{max}$  can be determined and compared with  $P_y$ . For example, the 10WF72 columns have an area of 21.18 in<sup>2</sup> and a yield stress of 36,000 psi, and the maximum load ( $P_{max}$ ) the columns can withstand before inelastic failure is 762.5 kips (Equation 3.9).

### 3.7 Strain Analysis from Strain Gauge Readings

The maximum strain the columns and beam can endure before failure is calculated using Equation 3.11, assuming the strain hardening of steel material can be ignored for practical purposes.

$$\varepsilon_y = \frac{f_y}{E} \tag{3.11}$$

where  $\varepsilon_y$  is the yielding strain,  $f_y$  is the yield stress, and *E* the modulus of elasticity for a given structural member. The maximum strain can be found using Equation 3.12.

$$\varepsilon_{max} = \varepsilon_{existing} + \Delta \varepsilon \tag{3.12}$$

where  $\varepsilon_{\text{max}}$  is the maximum strain that is measured in the member ( $\varepsilon_{\text{max}} \le \varepsilon_y$ ),  $\varepsilon_{\text{existing}}$  is the original/existing strain on the column or beam caused from the weight of the structure, and  $\Delta \varepsilon$  is the change in strain caused by column removal.  $\varepsilon_{\text{max}}$  is not necessarily equal to  $\varepsilon_y$ .

The  $\Delta \varepsilon$  was recorded directly from the strain gauges, but the original/existing strain conditions on the columns and beams are unknown. The existing strains ( $\varepsilon_{existing}$ ) will be analyzed in Chapter 5 using SAP2000.

All the columns and beams in the test building have a yield stress of 36,000 psi and 42,000 psi respectively. The modulus of elasticity for both steel columns and beams is 29,000 kips per square inch (ksi). The yield strain for steel columns and beams is 0.00124 and 0.001445 respectively (Equation 3.11). Once the strain of 0.00124 is reached, the column becomes inelastic and has a greater chance of failure, and beams also become inelastic once the strain of 0.001445 is reached. The maximum value the strain gauges recorded for  $\Delta \varepsilon$  on the building during the column removal never exceeded 0.0008. The original/existing ( $\varepsilon_{existing}$ ) strain on the columns and beams caused by the weight of the structure must be less than 0.00044 (Equation 3.12) or these members could fail. The actual field measurements of strain show the structure did not seem susceptible to progressive collapse.

#### 3.8 Bending Moment Analysis from Strain Gauge Readings

The maximum bending moment that the beam could endure before yielding is calculated using Equation 3.13.

$$M_y = f_y \cdot S_x \tag{3.13}$$

where  $M_y$  is the yield moment,  $f_y$  is the yield stress, and  $S_x$  is the elastic modulus given for a steel structural member. The maximum bending moment that the beam can endure before a plastic hinge is formed is found using Equation 3.14.

$$M_p = f_y \cdot Z_x \tag{3.14}$$

where  $M_p$  is the plastic moment,  $f_y$  is the yield stress and  $Z_x$  is the plastic modulus given for a steel structural member. The maximum moment (yielding or plastic) can be found using Equation 3.15.

$$M_p \text{ or } M_y = M_{existing} + \Delta M \tag{3.15}$$

where  $M_p$  is the plastic moment,  $M_y$  is the yield moment,  $M_{existing}$  is the original/existing moment on the column or beam caused from the weight of the structure including live load, and  $\Delta M$  is the change in moment caused by column removal. The SAP2000 analysis in Chapter 5 will be used to calculate the  $M_{existing}$  values for the beams and columns, and the maximum moment recorded in the field,  $\Delta M$ , was 13.45 kip-ft on the beam.

For example, the elastic modulus for the 24 I 79.9 beam (Beam 10) is 173.9 in.<sup>3</sup>, and the maximum bending moment is 608.65 kip-ft (Equation 3.13). The plastic modulus

for the 24 I 79.9 beam is 203.0 in.<sup>3</sup>, and the maximum plastic moment is 710.5 kip-ft (Equation 3.14). The original/existing moment ( $M_{existing}$ ) cannot be greater than 594.78 kip-ft for yielding moment and 696.63 kip-ft for plastic moment for the beam (Equation 3.15). The beams actual field measurement of  $\Delta M$  (Equation 3.8) show the structure was not susceptible to progressive collapse.

#### 3.9 Strain Relationship between Torching and Removal Phases

Figure B.4 in Appendix B displays the recorded strains,  $\varepsilon$ , and change in strain,  $\Delta \varepsilon$ , at specific times. The reported strains do not take into account the initial strain in the frame due to existing loads (discussed in Section 3.7). Ideally, the strain recorded at the end of each column torching process should equal the strain at the beginning of the next column torching. However, the strains fluctuate slightly between column torchings. The  $\Delta \varepsilon$  values are greatest when the columns are torched, because the columns lose most of their structural strength and loads have to be redistributed. Most of the  $\Delta \varepsilon$  values increase very slightly between the last column being torched and the first column removed.

However, some of the  $\varepsilon$  values do increase greatly between the last torching and the first column removal. Once the column removal phase begins, the  $\Delta \varepsilon$  values generated between each column removal are very close to zero and the  $\varepsilon$  values are fairly constant. This appears to be because most of the load redistribution between members has taken place during the torching phase. A relationship between the measured strains during the torching phase and removed phase needs to be developed in order to directly compare with the SAP2000 analysis presented in Chapter 5. Ideally, the experiment would completely remove one column at a time, and the  $\varepsilon$ and  $\Delta \varepsilon$  values would be created from the column removals only. The entire torching phase would be eliminated. However, the columns must be torched first for safety. A relationship between the torching and column removal phases is found in Equation 3.16. This equation is used to create a single column removal phase in the structure to determine the  $\varepsilon$  and  $\Delta \varepsilon$  values, eliminating the torching phase.

$$\varepsilon$$
 current removed =  $\varepsilon$  current torching + ( $\varepsilon$ removed average -  $\varepsilon$ last torching) (3.16)

where  $\varepsilon_{current removed}$  is the strain generated in a structural member after one to four columns are removed (taking into account the torching phase),  $\varepsilon_{current torching}$  is the strain generated in a structural member after one to four columns are torched (Figure B.4),  $\varepsilon_{removed average}$  is the  $\varepsilon$  value created from averaging the recorded strains from all four column removals for a given structural member. Since there is very little change in the strain during the column removal phase, the four strains for a given structural member are averaged to generate a single value ( $\varepsilon_{removed average}$ ).  $\varepsilon_{last torching}$  is the final  $\varepsilon$  value for a given structural member generated from the final column torching. The  $\varepsilon_{last torching} = \varepsilon_{current}$ torching during the last column torching.

For example, the Strain Gauge 7 in Figure B.4 had a strain of -0.000105 when Column 16C was torched. The -0.000105 strain is the  $\varepsilon_{current torching}$  value. The  $\varepsilon_{removed}$  $_{average}$  value averages all four strains recorded during the column removal. The strains during each column removal are -0.000652, -0.000668, -0.000668, and -0.000691. The average of those strains is -0.000669.75 and becomes the  $\varepsilon_{removed average}$  value. The  $\varepsilon_{last}$  torching value is a strain of -0.000447 from the torching of Column 11C. Therefore, the  $\varepsilon$ current removed value for Column 16C removed from Equation 3.16 is -0.000328.

Strain Gauge		
Name	Member	Location
12	Beam 10	Bottom Flange
11	Column 12C	Exterior Flange
10	Column 13C	Web
9	Column 13C	Exterior Flange
8	Column 14C	Web
7	Column 14C	Exterior Flange
5	Column 16C	Exterior Flange
4	Column 17C	Web
3	Column 17C	Exterior Flange

Table 3.1- Strain Gauge Numbers with Location.



Figure 3.1- Axis Labels for Columns and Beams.



Figure 3.2- Strain Gauge Attached to a Column with a Cover Shield Applied.



Figure 3.3- Exposed Columns and Beam Labeled.



Figure 3.4- Strain Gauge Placement with Columns and Beam Labeled.



Figure 3.5- Computer Station and Data Acquisition System.



Figure 3.6- Torched Column Ready to be Pulled Out.



Figure 3.7- Order of Column Torching and Removal.



Figure 3.8- Column 16C Being Torched.



Figure 3.9- Column 16C Removed.



Figure 3.10- Torched Section of Column 11C Being Removed.



Figure 3.11- Strain versus Time Chart for Strain Gauge 7: Measurements during Torching (Time: 0-3200 seconds).


Figure 3.12- Strain versus Time Chart for Strain Gauge 7: Measurements during Torching (Time: 3200-6398 seconds).



Figure 3.13- Strain versus Time Chart for Strain Gauge 7: Measurements during Column Removal (Time: 5000-5800 seconds).

# **CHAPTER 4**

# 4. GSA GUIDELINES FOR PROGRESSIVE COLLAPSE

## 4.1 Introduction

Chapter 4 discusses the General Services Administration (GSA) Progressive Collapse guidelines. This chapter explains the procedure GSA (2003) follows in order to determine if a structure will be susceptible to progressive collapse. GSA (2003) recommendations and formulations for column removal are illustrated in various figures, and the Demand-Capacity Ratios (DCR) values for the building are presented.

### 4.2 General GSA (2003) Guidelines

The GSA Progressive Collapse Analysis and Design Guidelines (2003) define analysis procedures to evaluate the vulnerability of a structure against progressive collapse. GSA (2003) recommends that a structure be analyzed by instantaneously removing a column from the middle of the traverse side of the building, near the middle of the longitudinal side of building, and at the corner of the building (Figure 4.1). When analyzing the structure for progressive collapse potential, GSA (2003) recommends a general loading factor to be used for every structural member in the building being tested. GSA (2003) factors the loading conditions using Equation 4.1:

## $Load=2.0(Dead \ Load + 0.25(Live \ Load)) \tag{4.1}$

Equation 4.1 is used for all loads acting on the structure, and increases the loading condition to account for irregularities in the structure. This equation presents the worst case scenario for the structure being tested for progressive collapse potential. Using Equation 4.1, the allowable extents of collapse resulting from instantaneous removal of primary exterior vertical supports are found in Figure 4.2.

When vertical members are instantaneously removed, GSA (2003) uses Demand-Capacity Ratios (DCR) to analyze which structural members will exceed their loading capacity and lead to progressive collapse. Using the linear elastic static analysis, the DCR values are found using Equation 4.2.

$$DCR = \frac{M_{max}}{M_p} \tag{4.2}$$

where  $M_{max}$  equals the moment demand calculated using linear elastic static analysis from SAP2000, and  $M_p$  equals the ultimate moment capacity (plastic moment) can be calculated from Equation 3.14. Using these two values, the DCR value for each structural member of the building is calculated. The DCR values calculated from Equation 4.2 cannot exceed the DCR limits presented in Figure 4.3.

Figure 4.3 contains the GSA (2003) DCR limit calculation table for beams and columns. All the beams were considered to be flexure, and the columns were assumed to be subjected to axial loads in the range of Equation 4.3:

$$\theta < \frac{P}{P_{CL}} < 0.5 \tag{4.3}$$

Where  $P_{CL}$  equals the gross area multiplied by the yield stress of the member  $(P_{CL}=P_y)$ , and *P* equals the axial force acting on the columns. It is realistic to assume that the load ratio in Equation 4.3 never exceeds 0.5 for any of the columns. Therefore, the DCR limits presented in Figure 4.3 are accurate.

### 4.3 GSA Guidelines Used for Experiment

The experiment conducted as part of this study involves the instantaneous removal of four columns shown in Figures 2.5 and 3.7. The two columns removed, 15C and 16C, were located near the middle of the North side of the building. One Column, 11C, was removed at the Northeast corner, and another Column, 12C, was removed directly adjacent to the Northeast corner on the North side of the building. These columns were chosen following Figure 4.1 as close as feasibly possible.

Table 4.1 displays the calculated DCR values using Figure 4.3 for the beams and columns on the structure. The DCR value for the 24 I 79.9 beam is reduced by 25% to account for an atypical section (described in Section 6.7). The 24 I 79.9 beam is considered atypical, because it spans 25 ft-6 in. over a stairwell between Columns 11C and 12C.



Figure 4.1- GSA (2003) Recommendation for Column Removal for Steel Frame Buildings.



Figure 4.2- GSA (2003) Allowable Extent of Collapse from Column Removal for Steel Frame Buildings.

	Values for Linear Procedures
Component/Action	DCR
Beams – flexure	
a. $\frac{b_f}{2t_f} \leq \frac{52}{\sqrt{F_{ye}}}$ and $\frac{h}{t_w} \leq \frac{418}{\sqrt{F_{ye}}}$	3
b. $\frac{b_f}{2t_f} \ge \frac{65}{\sqrt{F_{ye}}}$ or $\frac{h}{t_*} \ge \frac{640}{\sqrt{F_{ye}}}$	2
c. Other	Linear interpolation between the values on lines a and b for both flange slenderness (first term) and web slenderness (second term) shall be performed, and the lowest resulting value shall be used.
Columns – flexure	
For 0 < P/P <sub>CL</sub> < 0.5	
a. $\frac{b_f}{2t_f} \le \frac{52}{\sqrt{F_{ye}}}$ and $\frac{h}{t_w} \le \frac{300}{\sqrt{F_{ye}}}$	2
b. $\frac{b_f}{2t_f} \ge \frac{65}{\sqrt{F_{ye}}}$ or $\frac{h}{t_w} \ge \frac{460}{\sqrt{F_{ye}}}$	1.25
c. Other	Linear interpolation between the values on lines a and b for both flange slenderness (first term) and web slenderness (second term) shall be performed, and the lowest resulting value shall be used.

Figure 4.3- GSA (2003) Specified DCR Limits for Steel Frame Components.

Beam	DCR value
24 I 79.9	2.25
21 WF 62	3
18 WF 45	3
Column	DCR value
Column 10 WF 49	DCR value
Column 10 WF 49 10 WF 72	<b>DCR value</b> 1.9 2
Column           10 WF 49           10 WF 72           10 WF 77	DCR value           1.9           2           3

Table 4.1- Required DCR Limits for the Beams and Columns of the Structure.

# **CHAPTER 5**

## 5. SAP2000 ANALYSIS

#### 5.1 SAP2000 Analysis Introduction

Chapter 5 describes the computer simulation from the structural analysis program, SAP2000. The calculations for loading conditions are described and presented, and the assumptions for the building model are presented. The demand-capacity-ratios (DCR), strain variations ( $\Delta\epsilon$ ), and change in moment ( $\Delta$ M) values are generated from the SAP2000 analysis and are compared with the actual values from the strain gauges. This comparison is then discussed and analyzed.

## 5.2 SAP2000 Information, Assumptions, and Loading Conditions

The structural analysis computer program, SAP2000, is used to analyze the Bankers Life and Casualty Company Insurance building. A linear elastic static analysis was done on the two dimensional exterior frame located on the North side of the building, which takes into account the effect of immediate surrounding structural members. SAP2000 analyzes the loading conditions caused by the structure's weight.

Loading conditions for the structural members on the North side of the structure were hand calculated. The loads acting on the structural members were caused by the dead load weight from various structural members. The joists (28 LH 06) are 19 pounds per linear foot (plf), and the bridging (L  $1 \frac{1}{4}$  in. x  $1 \frac{1}{4}$  in. x  $1 \frac{1}{8}$  in.) is 1.01 plf. The 1 in. diameter tie rods weight is calculated using Equation 5.1 from 1963 AISC manual.

$$0.223(L) + 0.56 \, lb \tag{5.1}$$

where *L* is the length of the tie rod. The tie rods weigh 145.6 lbs. The roof material is assumed to be 25 pounds per square foot (psf). The concrete slabs are assumed to be 150 pounds per cubic foot (pcf), the concrete masonry units are assumed to be 135 pcf, the exterior bricks are assumed to be 120 pcf, and the glass is assumed to be 160 pcf. The second floor has an assumed dead load of 45 psf acting upon it from carpet, electric wires, ceiling panels, lights, tubing ducts, partition walls, and a small air conditioning unit.

Equation 4.1 was used for the loading conditions. Therefore, all the dead loads were multiplied by a factor of two. The same procedure for the field experiment was implemented in the SAP2000 analysis, and all the structural properties of the members were inserted into the computer model. The SAP2000 analysis is a two dimensional linear elastic static simulation, and the columns were removed in SAP2000 in the same order they were torched in the field. The computer model of the structure in SAP2000 analyzes the original building conditions and each subsequent column removal.

#### 5.3 SAP2000 DCR Computer Simulation

The hand calculated loads were inserted into the SAP2000 program, and a model of the building was created. A SAP2000 computer simulation was performed after each

column removed on the model and the results are analyzed. Figures 5.1 through 5.5 show the SAP2000 bending moment diagrams and DCR values for the two dimensional exterior frame on the North side of the structure. The DCR values in red in Figures 5.1 through 5.5 have exceeded the specified DCR limits shown in Table 4.1.

Column 12C was torched third and removed last in the field, but was removed third in SAP2000. This removal was deliberately done, because the strains had the largest readings when the columns were torched and barely reacted and changed when the columns were removed. For this experiment, the column torching order is the SAP2000 column removal order.

Some of the DCR values for the members exceeded the specified DCR limit (GSA,2003) by a factor of eight. These high DCR values could partially be due to the inaccuracy in dead and live load predictions. Approximately half of the second floor was collapsed by the demolition team (Figures 2.6 and 2.7) prior to the first column removal, the GSA guidelines require all dead loads be multiplied by a factor of two (Equation 4.1), or inaccuracy in our judgment for assumed loading conditions. Also, the structure could not redistribute the gravity loads as easily because it was a two story tall structure, half of the second story was collapsed, and had large spans between columns. A taller structure probably would be able to distribute gravity loads to more members and would generate smaller DCR values as found in Sezen and Song (2008).

The SAP2000 study conducted showed eight columns and seven beams exceeded their respected DCR limits when all four columns were removed (Figure 5.5). These members are deemed susceptible to progressive collapse. The DCR limit for 8 WF 31 columns is 1.8. The DCR value for a 8 WF 31 column above the removed Column 12C was 16.12 after all four columns were removed. The DCR limit was exceeded by a factor of 8.8. However, during the experiment the building did not experience progressive collapse when all four columns were removed. A nonlinear dynamic analysis performed in SAP2000 would provide more accurate DCR values.

### 5.4 SAP2000 Analysis & Clarifications

The SAP2000 program calculates the  $\varepsilon$  when a column is completely removed only, i.e., either there is a column or no column in the model. There is not a way for a linear elastic static analysis to account for the torching and removal of the columns using the same model. The  $\Delta \varepsilon$  value can be determined in SAP2000 by taking the difference in  $\varepsilon$ values for each column removal (i.e., based on analysis with and without a column in the model). The  $\varepsilon$  and  $\Delta \varepsilon$  created in SAP2000 between column removals cannot be compared directly with the  $\varepsilon$  and  $\Delta \varepsilon$  generated between actual column removals, because the  $\varepsilon$  and  $\Delta \varepsilon$  have the greatest change during the torching phase and change slightly during column removals as shown in Figure B.4 and discussed in Section 3.9. The  $\varepsilon$  and  $\Delta \varepsilon$  from Equation 3.16 are compared with the  $\varepsilon$  and  $\Delta \varepsilon$  generated from the SAP2000 analysis.

#### 5.5 SAP2000 Analysis Comparison with Recorded Data

The strain gauges in the field were set to zero before the experiment began. There was an initial strain in the columns before the strain gauges were instrumented, but could not be recorded (discussed in Section 3.7). Table 5.1 shows the axial force (P), bending

moment (*M*), strain ( $\varepsilon$ ) after each torching phase, average  $\varepsilon$  value from the four similar strain values recorded during column removal process (discussed in Section 3.9). The final  $\varepsilon$ , and  $\Delta \varepsilon$  for Strain Gauge 7 on Column 14C are compared with the generated SAP2000 values.

Strain Gauge 7 was selected for this experimental study because it was believed to have recorded the most consistent and accurate data in the field. Table 5.1 shows that the strain values recorded in the field from Strain Gauge 7 had an average 21% error between the field and SAP2000 results using Equation 5.2.

$$Percent Error = \frac{SAP2000 - Field}{Field}$$
(5.2)

where the *percent error* is the error between the SAP2000 strains and the strains recorded in the field, *SAP2000* is the strain after each column removal (Table 5.1), and *Field* is the strain recording in the field after each column removal (Table 5.1). The *percent error* was calculated for each column removal. The absolute values of the four percent errors were then averaged to generate the 21% error. These values were very close considering all the possibilities for error. The exact time of each column torching and removal was not recorded, the exact locations of strain gauges were not recorded, and the demolition atmosphere could have caused recording discrepancies.

Figure 5.6 shows the comparison between the  $\varepsilon$  values from the SAP2000 analysis and the actual field measurements. Referring back to Chapter 3 and Table 5.1, the measured maximum *P* value of Strain Gage 7 never exceeded the allowable  $P_{max}$  value, 762.5 kips (Equation 3.9). The initial strain,  $\varepsilon_{existing}$ , was equal to 0.000192 which did not exceed the allowed  $\varepsilon_{existing}$  value of 0.00044 (Equation 3.12). The  $M_{existing}$  value in Table 5.1 for Strain Gauge 7 was equal to -0.85 kip-ft and was not greater than allowable  $M_{existing}$  absolute value of 594.78 kip-ft (Equation 3.15). Using Equations 3.13 and 3.14, the moment from the SAP2000 analysis in Table 5.1 for Strain Gauge 7 never exceeded the maximum bending (238 kip-ft) or plastic moment (269 kip-ft).

Strain Gauge 12 located on Beam 10 was also directly compared strain generated SAP2000. There was over a 400% error between the SAP2000 and field recorded strains (Equation 5.2). This large error could be partially attributed to the linear elastic static analysis, because it does not include dynamic, nonlinear, and three dimensional effects. Therefore, corner columns and beams are not able to transfer loads around the corner to neighboring columns and beams. Also, the beams in on the structure were assumed to have zero or little axial loads from Equation 3.8. The SAP2000 analysis had cases where approximately 70 kips were applied in some beams. The SAP2000 results had Beam 10 very close to failure, while the recorded strains in the field had Beam 10 not close to failure.

0.34	0.31	0.28	0.34	0.35	-1			
0.37 0.39	0.14 0.48	0.01 0.38	0.04 0.38	0.03 0.39	0.26 0.33	0.33	0.36	0.38
0.05	0.07	0.03	0.01	0.02	0.01	0.02	0.01	0.05 0.18
		+		Z	-	-		1

Figure 5.1- SAP2000 Model of Original Intact Building with DCR Values.



Figure 5.2- SAP2000 Model after Column 15C Removed with DCR Values.

0.75	0.42	3.99	4.96	2.27				
0.58	1.64 0.59	2.64 3.69	3.74 5.86	7.52 5.57	6.88 7.83	5.51	0.73	0.63
0.10	0.12	0.31	2.95			4.31	1.07	0.09 0.0'
	1			ž	1		-	

Figure 5.3- SAP2000 Model after Columns 15C and 16C Removed with DCR Values.

1.56	2.14	3.77	4,89	2.38	•			
2.28 1.75	2.02	5.10 3.33	3.91 5.73	7.23 5.58	7.32 7.93	5.60	0.74	0.65
0.56		1.46	3.33			4.31	1.14	0.15 0.13
		1		Z				_

Figure 5.4- SAP2000 Model after Columns 12C, 15C, and 16C Removed with DCR Values.



Figure 5.5- SAP2000 Model after Columns 11C, 12C, 15C, and 16C Removed with DCR Values.



Figure 5.6- SAP2000 and Field Strain Values Shown for Strain Gauge 7 (21% Error between SAP2000 Results and Actual Measurements).

	SAP2000-	Field-	SAP2000-	Field-	SAP2000-	Field-
	Prior to	prior to	15 C	15 C	16 C	16 C
	removal	removal	removed	removed	removed	removed
Axial Force at 6 ft						
from bottom (kip)	-113.8	?	-193.72	?	-317.23	?
Moment at 6 ft from						
bottom (kip-ft)	-0.85	?	-6.28	?	-23.1	?
Strain from Torching						
at 6 ft from bottom	-	?	-	-37	-	-105
Avg. Strain from						
Removal at 6 ft from						
bottom	-	?	-	-222.75	-	-222.75
Strain ( $\epsilon$ ) 6 ft from						-
bottom	-0.000192	-0.000192	-0.000351	-0.000451	-0.000642	0.000519
Absolute Change in						
Strain ( $\Delta \epsilon$ )	0.000000	0.000000	0.000160	0.000260	0.000291	0.000068

			SAP2000-	
	SAP2000-12	Field-12 C	11 C	Field-11 C
	C removed	removed	removed	removed
Axial Force at 6' from				
bottom (kip)	-291.5	?	-195	?
Moment at 6' from				
bottom (kip-ft)	-29.64	?	-64.85	?
Strain from Torching				
at 6' from bottom	-	-138	-	-447
Avg. Strain from				
Removal at 6' from				
bottom	-	-222.75	-	-222.75
Strain (ɛ) 6' from				
bottom	-0.000634	-0.000552	-0.000659	-0.000861
Absolute Change in				
Strain ( $\Delta \epsilon$ )	0.000008	0.000033	0.000025	0.000309

Average % ε Error 21

Table 5.1- Axial Force and Moment Acting on Column 14C at Location of Strain Gauge 7, and Strain Gauge 7 Values from SAP2000 Analysis and Field Measurements.

# **CHAPTER 6**

# 6. GENERAL GUIDELINES FOR INSTRUMENTATION AND COLUMN REMOVAL PROCEDURE

## 6.1 Introduction

Chapter 6 discusses strain gauge instrumentation and suggests placement of sensors for optimum results. The strains generated from bending moments and axial loads applied on columns and beams are discussed. The instrumentation of linear displacement sensors is also introduced. The optimum column removal procedure to produce the most beneficial data measurements is also presented. Methods for removing exterior columns are discussed, and suggestions for interior column removal are presented.

### 6.2 Strain Gauge Theory

Strain gauges were used to measure the strain in the longitudinal direction of beams and columns on the first floor of the structure. The strain gauge will face vertically for columns (silver solder points facing down), and will face left or right for beams. Figure 6.1 shows a typical strain gauge.

Most columns and beams in structures are designed to resist lateral forces about their strong axis or X axis (see Figure 3.1 for axis details). As a result, most exterior columns of a building will have their flanges facing inward and outward, and beams have their flanges facing upwards and downward. Most W shape columns and beams have a larger moment of inertia about the X axis, and can resist a greater bending moment in that direction. For this research, it is assumed the exterior columns of structures have their flanges facing inward and outward and beam's flanges are facing upward and downward.

Many columns resist an axial stress and a bending stress from the building's gravity load (dead and live loads). Beams generally resist a bending stress from the building's gravity load and usually an axial stress is not generated. The stress generated from the gravity load of the structure is directly proportional to strain as long as the steel material stays elastic and does not yield. The stress-strain relationship for elastic steel material is linear (Equation 3.5). Therefore, the larger the stress generated, the greater the strain.

### 6.3 Strain Gauge Instrumentation Theory on Columns

If a structure fails due to progressive collapse, it is difficult to determine which direction the column will fail. The column can bend about the X axis and fail outward or inward, it can fail by bending about the Y axis, or a combination of both. Theoretically, the strain should be the same value on the flange in compression and the flange in tension from a bending moment alone. As the weight of structure shifts, a combination of an axial load and bending moment is generated. As the weight of the structure shifts, one flange of a structural member becomes more in compression. The strain and stress are uniform across the cross sectional area of the column from the axial force, and are linear across the cross sectional area of the column from the bending moment. Shown in Figure 6.2, the strain generated from the bending moment is added to the strain created from the

compressive axial loading creating a larger strain in the compression flange (Equation 3.6).

Figures 6.3 and 6.4 show the two possible cases for a fixed end connection column bending about the X axis. Figure 6.3 shows the orientation of the column when the flange on the right, near the top of the column, is in compression. Figure 6.4 shows the orientation of the column when the flange on the left, near the top of the column, is in compression.

The stress and strain developed is the greatest at the ends of the cross sectional area of the W shape, and the greatest strain is generated where the moment is the largest (Equation 3.8 and Figure 6.2). Therefore, one strain gauge should be attached on the column at the center of the compression flange near the top of the column to record the largest strain readings. Unfortunately, it is difficult to determine which flange will become more in compression when the neighboring columns are removed.

If the column fails due to bending about the Y axis, the strain gauges attached vertically on the flanges theoretically should not record any strain. The strain developed from bending about the Y axis can be recorded if the strain gauge was instrumented facing left or right on the flange. This strain gauge would record the strain in the X direction, and further investigation will be done in future research. For most progressive collapse research, the strain gauges will be placed at the center of column's flanges facing upwards near the top of the column.

Theoretically, the column cross section will have a zero bending moment value at the point where the bending direction changes. Figures 6.3 and 6.4 show this point at the

line labeled C. The strain developed only from axial loading in the column can be determined if a strain gauge is attached facing vertically at the very center of the web at the point of zero moment. Although there is no easy way to determine the inflection point or zero moment location, a preliminary analysis predication shows the bending effects will be very small (close to zero) at 1/3 the length of the column from the bottom.

## 6.4 Strain Gauge Theory on Beams

Beams generally carry have a very small axial load. The bending moment due to gravity loads will create the largest strains in the flanges of the beam (Figure 6.5). Attach strain gauges facing left or right to the bottom flange of the beam (flange facing the ground) because the bottom flange will most likely be easier to access.

The greatest strains will be generated where the bending moment is the largest. For beams with fixed ends, the moment will be greatest at the ends of the beam and possibly near the middle of the span length as shown in Figure 6.6.

The strain gauges should be placed as close to the ends of the beam as possible at the center of the flange. The strain gauges should face the column that they are closer to, but investigation will be done for future research (silver solder points facing away from the column closest). If an axial force is believed to be developed during the experiment, a strain gauge will only record the strain generated from the axial force if it is placed at the center of the beam's web at either point C in Figure 6.6. The strain gauge should be facing left or right (facing the direction the axial force will come from).

#### 6.5 Strain Gauge Locations for Columns and Beams

The strain gauges record a uni-axial strain generated from a combination of the axial loads and bending moments as described in Chapter 3 (Equations 3.6 and 3.7). In order to determine the actual variation of axial load ( $\Delta P$ ) and the moment ( $\Delta M$ ) in the member, placement of sensors should follow Figures 6.7 and 6.8.

Strain gauges must be placed near the top of columns at points A and C shown in Figure 6.7. It is expected that the maximum moment will occur at the top of the column both before and after the removal of neighboring column(s). The axial load will be constant over the length of the column. Strain gauges A and C in Figure 6.7 will be used to determine which flange is in compression and has a greater strain. Strain gauge B will record strains mostly due to axial load, and possibly some strains due to bending moment. Therefore, strain gauge B in Figure 6.7 is not necessary at the top of the column. Strain gauges A and C should be sufficient to determine the strain distribution at the top of the column. Once the strain gauges at points A and C record the  $\Delta \varepsilon$  in Figure 6.7, Equation 3.7 can be used to calculate the strains at point A and C. When both equations are solved simultaneously, the  $\Delta P$  and  $\Delta M$  values acting on the column can be determined.

We predict a strain gauge placed approximately 1/3 the length of the column from the bottom at point B in Figure 6.7 will record the strain from the axial load only. Using Equation 3.7, the  $\Delta P$  can be calculated because  $\Delta M$  is theoretically close to zero. This  $\Delta P$ value can be checked with the  $\Delta P$  calculated from the strain gauge readings near the top of the column at points A and C shown in Figure 6.7, and should be similar in value. At least, a single strain gauge must be placed near the end of the beam at either point A or C shown in Figure 6.8. Since beams are rarely subjected to an axial load, placement of a strain gauge at point B in Figure 6.8 is probably not necessary. Theoretically, the strains due to bending moments will be the same at points A and C in Figure 6.8. Using the strains recorded at point A or C and Equation 3.8, the  $\Delta M$  can be determined since  $\Delta P$  is approximately zero. Figure 6.9 shows the beam response stages.

The two beams immediately above a removed column can be subjected to tensile axial load, especially if catenary action develops (Figure 6.9). Prior to inelastic or catenary action, the moments in the midspan of beams can be reduced significantly (Figure 6.6). Similarly, after the column removal, the ends of elastic beams near the removed column can be subjected to large positive moments (Figure 6.6). Under positive moments, the beam ends will have tension in the bottom flange and compression in the top flange. Before the column removal, the same beam ends would carry negative moments with the top flange in tension and the bottom flange in compression. Therefore, it is critical to capture this stress change at beam ends. As a result, at least two strain gauges are necessary, one on the top flange and another on the bottom flange at the ends of beams jointed above the removed column. To summarize, a minimum of two strain gauges are needed in each beam end at M and two gauges on columns at M shown in Figure 6.10.

Figure 6.10 shows three columns and two beams instrumented with strain gauges, and the column in the middle is removed. If the axial load is to be determined for the beam, then strain gauges should be installed at locations where the moment will be close

to zero as discussed earlier in this section. The strain gauge instrumentation presented in Figure 6.10 should be applied to the entire part of a structure used for a progressive collapse experiment.

Table 6.1 provides recommendation for the amount of strain gauges to use depending on availability. The minimum number of strain gauges used in a progressive collapse experiment for one column removal is eight, shown in Table 6.1. If the minimum amount of strain gauges is to be used, strain gauges need to be attached near the most critical sections where columns will be removed labeled M in Figure 6.10 following the guidelines presented in this chapter

The practical number of strain gauges to use in a progressive collapse experiment is 12, shown in Table 6.1. If the practical amount of strain gauges is available, attach strain gauges on beams and columns surrounding columns to be removed. The strain gauges labeled M and P in Figure 6.10 show where the strain gauges should be placed on each structural member, and Table 6.1 shows how many strain gauges should be attached to each column and beam for practical purposes. In addition to each column having two strain gauges instrumented at location M, each beam should be instrumented with a strain gauge on each flange at each end labeled M and P shown in Figure 6.10.

The desirable amount of strain gauges to use in a progressive collapse experiment is 16, as shown in Table 6.1. If the desirable amount of strain gauges is available, attach strain gauges on every beam and column around the column to be removed during the progressive collapse experiment. The strain gauges labeled M, P, and D in Figure 6.10 show where the strain gauges should be placed, and Table 6.1 shows how many strain gauges should be attached to each column and beam for the desirable chase. Each column should have two strain gauges instrumented at M and one strain gauge at the center of the web 1/3 the length of the column from the bottom labeled D (Figure 6.10). Each beam should be instrumented with strain gauges on each flange at each end labeled M and P, and one at the center labeled D, as shown in Figure 6.10. Should the axial load need to be determined for the beam, an extra strain gauge can be added at section D following the procedure presented earlier in the section. If strain gauges are still available, attach strain gauges following Section 6.5 to columns that will be removed.

### 6.6 Linear Displacement Sensor Instrumentation and Placement

Linear displacement sensors (LDS) are used to measure the vertical or horizontal displacement of beams or columns. Linear displacement sensors are connected to the same data acquisition system and computer station the strain gauges are, and the computer program records the displacements and strains simultaneously. The varying models of LDS can record a displacement ranging from 0.25 in. to 4 in., and can work in almost any temperature conditions. A LDS is shown in Figure 6.11.

The sensor needs to be attached to a fixed stand completely separate from structure. A wooden frame and retractable metal stand is being developed to support the sensor. These stands need to be absolutely secure and should not move during the experiment or the LDS will record data inaccurately.

The sensor needs to be depressed slightly against an exposed exterior flange (bottom face) of a beam supporting the second floor. Placement of the LDS should be where the engineer believes the greatest vertical displacement will occur. Using Figure 6.5, the largest displacements would be at the ends of beams near the removed column. As each column is removed, the beam to column connection points will have the largest vertical displacement, and the LDS should be placed near and under these connections to record the largest vertical displacement.

### 6.7 Column Removal Guidelines

Structural redundancy and continuity across the structure is crucial for the prevention of progressive collapse. Beams jointed together independently from a column form a beam-to-beam structural continuity across a removed column. A column should be removed if the two beams above it do not form a beam-to-beam structural continuity. A typical beam-column frame structure usually has a relatively simple, uniform, and repetitive layout (GSA, 2003). An atypical structure with plan or vertical irregularities requires a different approach than described here.

Atypical structures may contain: combination structures, vertical discontinuities, transfer girders, variations in bay sizes, bay sizes greater than 30 ft. in any direction, plan irregularities, and closely spaced columns (GSA,2003). Combination structures combine frame and wall systems; therefore, engineering judgment is needed for combination structures, closely following the typical structural analysis results. Vertical discontinuities/transfer girder areas of the structure require column removal around these areas (GSA 2003). Therefore, if a vertical discontinuity exists, the neighboring columns of the vertical discontinuity must be removed. If a bay size should vary, the columns

nearest the largest bay size variation should be removed. Extreme bay sizes (30 ft or greater) have greater potential for progressive collapse.

Plan irregularities usually need the engineer's judgment for column removal. If a re-entrant corner is present, the column at the re-entrant corner should be removed (GSA, 2003). For closely spaced columns, GSA (2003) recommends: "...the structure should be analyzed for the loss of both columns if the distance between the columns is less than or equal to 30% of the longest dimension of the associated bay. Otherwise, only the loss of one column shall be required in the analysis."

In this study, we developed a general procedure for removing first story columns from a regular frame building. The procedure is illustrated in Figure 6.12. Figure 6.12 shows the order for which column should be removed. For safety reasons, the columns all have to be torched first, and the columns will be removed in the same order. Following the procedure in Chapter 3, the column circled 6th should be torched first. Prior to torching, the 2<sup>nd</sup> floor has to be supported near the column circled 6<sup>th</sup> in Figure 6.12. Steel supports being developed will support the weight of the structure above the interior column is to be torched and removed while the support mechanism supports the weight of the structure above the column. The jacking system will be disengaged once the interior column is to be removed.

The interior column circled 6th will be considered removed once the jacking system is disengaged. The columns circled 7th and 8th are optional to be torched and

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removed. Also, it may not be possible to remove columns 5<sup>th</sup> and 8<sup>th</sup> if the left side of the building is not accessible for testing.

Ideally, each column would need to be removed immediately after it was torched. This is almost impossible to do for safety reasons. Instead of using the torching method, a controlled blast can be the best method for removal of columns. Several critical columns would be attached with explosives, and all exterior and interior columns could be removed in a set order until collapse occurs. Controlled explosives would eliminate the need for the steel support jacking system, and create a more realistic progressive collapse scenario.



Figure 6.1- A Typical Strain Gauge.



Figure 6.2- Strain from Combination of Axial Load (P) and Bending Moment (M).



Figure 6.3- (a) is Orientation of a Column, (b) is the Bending Moment Diagram of the Column.



Figure 6.4- (a) is Orientation of a Column, (b) is the Bending Moment Diagram of the Column.



Figure 6.5- Beam Deflection and Moment Diagrams before and after Column Removal.



Figure 6.6- (a) Deflected Shape of a Fixed Ended Beam Under Uniform Vertical Load, (b) Moment Diagram of the Beam.



Figure 6.7- Strain Gauge Instrumentation on a Column.



Figure 6.8- Strain Gauge Instrumentation on a Beam.



Figure 6.9- Stages of Beam Response.



Figure 6.10- Strain Gauge Instrumentation for Columns and Beams Labeled by Importance Corresponding with Table 6.1.

	Strain Gauges needed per Beam	Strain Gauges needed per Column
(1) <b>Minimum</b> (8 strain		
gauges)	2	2
(2) Practical (12 strain		
gauges)	4	2
(3) <b>Desirable</b> (16 strain		
gauges)	5	3

Table 6.1- Number of Strain Gauges Needed if One Column is Removed (Figure 6.10).



Figure 6.11- Linear Displacement Sensor.



Figure 6.12- Suggested Order of Column Removal for the First Floor.

# **CHAPTER 7**

# 7. SUMMARY AND CONCLUSION

## 7.1 Summary

This research investigated the progressive collapse potential of an actual building scheduled for demolition. The data recorded in the field was analyzed and compared with data from a SAP2000 computer model. The GSA (2003) guidelines were discussed, and the demand-capacity-ratio (DCR) values were calculated. An in depth investigation of testing procedure and instrumentation for future experiments was done in Chapter 6. Suggestions for instrumentation placement and column removal guidelines were presented. The experience gained and errors observed in this research will be used to improve future progressive collapse research.

## 7.2 Conclusion

The building itself was unique because some of the second floor was collapsed prior to initiation of our experiment. Future structures should be fully intact and not damaged. The DCR values and some SAP2000 analysis results were excessively high due to the unique properties of the structure, inaccurate data recording, and demolition site inconsistencies. However, a great deal was learned and investigated from this research study.

Future progressive collapse experiments will be more informative and accurate. A more in depth SAP2000 analysis will be developed for future research that will analyze every member on the structure near the removed columns. The SAP2000 analysis for this experiment was similar to some of the strain gauge recordings, and Strain Gauge 7 had an average 21% error from the SAP2000 analysis. The DCR values deemed the structure to be at high risk for progressive collapse when all four columns were removed, while the field recorded strains did not come close to failure. It should be noted that DCR values are calculated from linear elastic static analysis, as recommended by GSA (2003). A more accurate numerical simulation should include the material nonlinearity, three-dimensional, and dynamic effects which are the subject of future research.
## **APPENDIX A**

# A. STRUCTURAL NOTES AND BUILDING PLANS



Figure A.1- Foundation Plan (Structural).

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Figure A.2- First Floor Framing Plan (Structural).

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Figure A.3- Second Floor Framing Plan (Structural).



Figure A.4- Roof Framing Plan (Structural).



Figure A.5- Typical Exterior Column Section (Structural).



Figure A.6- Concrete Notes (Structural).

	COM	POS	ITE BE	AM	SCH	IEDL	ILE	đ ž
BEAM		COV	SR PLATE	END	WELD	INTERME	PLATE WEL	NO. OF
MARK	SIZE	5128	CUTOFF	SIZE	LENGTH	SIZE	SPACIN	CONNECT
CBI	210502							35
Св2	36WF137	11"+196	3.9 FROM LOR J	38"	34"	2 = 2"	6'	108 2. Rowe
свз	30W 135	105-170	10:0 FROM B" 12:0 FROM COR"C	38	22	3'+2"	6"	108 2- Rowe
СВ4	21 wf 35	7"* 3	1:0" FROM BACH SUPPORT	ng"	14	35+2"	5"	32
C 85	211455	7"+ 34"	1-0 FROM BACH SUPPORT	38	14"	3 <sup>"</sup> B * 2"	5"	32
сва	36Wi135	11'*12'	3-8 FROM "A"	3 <sub>8</sub>	28	3. × 2'	Ġ <sup>"</sup>	108 2 RONE
C 87	24 wf <b>GB</b>	7"* 2"	2.0 FROM BACH SUPPORT	3,,"	14"	38"+2"	G"	32

Figure A.7- Composite Beam Schedule (Structural).



Figure A.8- Steel Notes (Structural).

GENERAL NOTES L DUBIGN LIVE LOADS ARE AS POLLOWING ROOF \* 30°/ 2' 2ND FLOOR •350 W FIRST FLOOR \* 400 % MESEANINE FLOOR . 100 4/2 2. ALL DIMENSIONS ON STRUCTURAL DRAWINGS THE CHICKED AGAINST ARCHITECTURAL PRAWINGS BY THE CONTRACTOR. FOR OPENINGS, SLEEVES, CHASES AND COCESSES IN WALLS з. AND SLADS SEE ARCHITECTURAL AND MECHANICAL DRAWINGS, 4. ALL FILL AND BLACK SOIL BELOW SLAS ON GRADE SPALL BE REMOVED AND REPLACED WITH APPROPRIATE NEW FILL IN & LAYERS & COMPACTED TO MIN. OF SAL DENSITY OF TAINED BY A.S.T.M. SPECIFICATION 12-1587-87.T. UNTIL PINAL GRADE 13 ATTAINED. 9 BOTTOM OF FOOTING SHOWN IS MINIMUM FOR DID PURPOSED ONLY. CONTRACTOR AT ALL TIMES SHALL CARRY FOOTINGS TO SOLID UNDISTURBED SOIL OF A MINIMUM BEARING PRESSURE OF 4000 %/R. Θ FOR ADDITIONAL MISCELLANEOUS STEEL REFER TO ARCHITECTURAL DRAWINGS. 7 PROVIDE & PLATE CLOSURES FOR EXTERIOR COLUMNS AS SHOWN ON SHEET A 10 United and the

Figure A.9- General Notes (Structural).

### **APPENDIX B**

### **B. STRAIN GAUGE CHARTS AND LOAD DISTRIBUTION** VALUES DURING COLUMN REMOVAL







Figure B.2- Strain versus Time Chart Measurements during Torching, (Time: 3200 – 6398 seconds).

	Column 15C Torched @233secs -1465 seconds	Column 16C Torched @2141secs -2870.5 seconds	Column 12C Torched @3000secs -3676.9 seconds	Column 11C Torched @3799secs -4385.6 seconds
Strain 3	-23 up to 18 increase of 41	22 to 21decrease of 1	22up to 26increase of 4	29 up to 41increase of 12
Strain 4	-11 up to 17 increase of 28	17to 13decrease of 4	17up to 17no change	18 up to 30increase of 12
Strain 5	-11 up to 5 increase of 16	gone	gone	gone
Strain 7	-5 up to 16 to -37- -decrease of 32	-40 to -105 decrease of 65	-101 up to -138 decrease of 37	-153 to -447decrease of 294
Strain 8	-13 up to 7 increase of 20	28 to 26decrease of 2	28 up to 30increase of 2	31 to 30decrease of 1
Strain 9	112 fluctuates wildly to 774- increase 662	768 to 749 decrease of 19	746 to 741decrease of 5	737 up to 880increase of 143
Strain 11	-65 up to -38 increase of 27	128 fluctuates up finally ends at 120 decrease of 8	133 to 0decrease of 133	9 up to 12increase of 3
Strain 12	-6 up to 16 increase of 22	27 to 25decrease of 2	25up to 29increase of 4	29 up to 32increase of 3

	Column 15C Removed @ 5269	Column 16C Removed	Column 11C Removed	Column 12C Removed
	seconds	@ 5308 seconds	@ 5449 seconds	@ 5532 seconds
Strain 3	45 to 44decrease of 1	45 to 44decrease of 1	45 to 45no change	45 to 45no change
Strain 4	38-37decrease of 1	38 to 38 no change	38 to 37decrease of 1	37 to 37no change
Strain 5	gone	gone	gone	gone
Strain 7	-650 to -652 decrease of 2	-671 to -668decrease of 3	-669 to -668decrease of 1	-690 to -691decrease of 1
Strain 8	9 to 9no change	8 to 8 no change	8 to 6decrease of 2	6 to 6no change
Strain 9	882 to 882no change	882 to 882 no change	882 to 882 no change	880 to 880-no change
Strain 11	29 to 29no change	27 to 28no change	33 to 33 no change	33 to 33 no change
Strain 12	32 to 32no change	34 to 34 no change	33 to 33 no change	33 to 33 no change

Figure B.3- Strain Values (10<sup>-6</sup>) and Change in Strain at Specific Times during Column Torching and Removal.



Figure B.4- Change in Strain ( $\Delta \epsilon$ ) Measurement.

Strain Gauge	∆M only from Column 15C Torched (kip-ft.)	∆M only from Column 16C Torched (kip-ft.)	∆M only from Column 12C Torched (kip-ft.)	∆M only from Column 11C Torched (kip-ft.)
On flange of 24 I 79 9				
Beam: 10	9.25	0.84	1.68	1.26
Strain Gauge	∆M only after Column 15 C removed (kip-ft.)	∆M only after Column 16 C removed (kip-ft.)	∆M only after Column 11 C removed (kip-ft.)	∆M only after Column 12 C removed (kip-ft.)
On flange of 24 I 79.9 Beam: 10	No Change	No Change	No Change	No Change
Strain Gauge	Total ∆M			
On flange of 24 I 79.9 Beam: 10	13 45			

KEY
$\mathbf{f} = (M^*c)/I = Bending Stress : (ksi)$
$\varepsilon = (f/E) = $ Strain : (unit less)
$\Delta \mathbf{M} = (\Delta \varepsilon * E * I)/c = \Delta \varepsilon * E * S = Change in Moment determined by change in Strain: (kip-$
ft.)
<b>T</b> =Member is in Tension
C=Member is in Compression

Figure B.5- Change in Bending Moment,  $\Delta M$  (kip-ft), from Column Removal and Total  $\Delta M$  (kip-ft) from Strain Gauge 12.

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