

There's always a solution in steel.

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Course Description

Designing Members for Torsion

February 12, 2015

This webinar will present an introduction to the general topic of torsion in structural members, including descriptions of St. Venant and warping resistance. Tools and methods for calculating twist and torsional demand stresses will be discussed. In addition to member behavior, the specific topic of Steel Lintel Design for Large Openings in Bearing Wall Buildings will also be addressed.





Learning Objectives

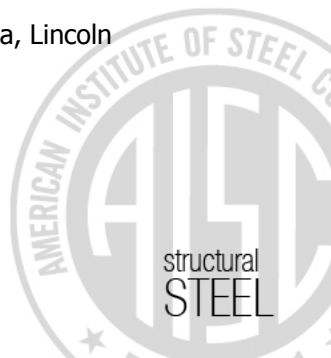
- Become familiar with the general topic of torsion in structural members.
- Gain an understanding of the principles of torsion such as St. Venant and warping resistance.
- Gain an understanding of the tools and methods for calculating twist and torsional demand stresses in structural members.
- Become familiar with the design of steel lintels by working through a design example.

There's always a solution in steel.

Designing Members for Torsion




written and presented by
Daniel Linzell, Ph.D., P.E.,
F.ASCE
Professor
University of Nebraska, Lincoln





Designing Members for Torsion (It's NOT a 4-LETTER WORD!!)

Daniel Linzell
University of Nebraska, Lincoln



*Torsional Analysis of
Structural Steel Members*

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Acknowledgements

- **Cristopher Moen, Virginia Tech**
- AISC – Charlie Carter, Brent Leu
- Lou Geschwindner, Penn State University
- Paul Seaburg, Penn State, University of Nebraska
- Walt Schneider, Penn State University



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Overview – The “T” Word

- Background
 - What is it? Why do we care?
- A Few Fundamentals (BUT NOT MUCH THEORY)
 - How can shear “flow”?
 - What is the shear center?
 - There are different types of torsion? Huh? Why? What are they?
- What Do I Do with This Info?
 - Design
 - Analysis
- Where Do I Go for More Help?
 - Texts, guides and specs
- The REAL Reason Why You’re Here – EXAMPLE

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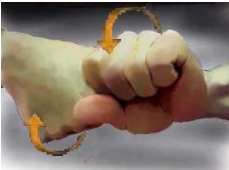





Background - Torsion

- What is it?
 - From Wikipedia

In solid mechanics, torsion is the twisting of an object due to an applied torque, therefore is expressed in N·m or ft·lb. In sections perpendicular to the torque axis, the resultant shear stress in this section is perpendicular to the radius.
 - Real world examples

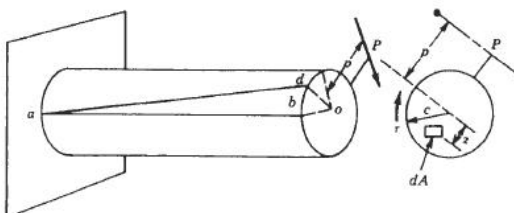




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Background - Torsion

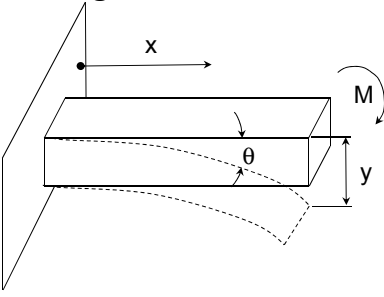
- From Your Undergrad Engineering Mechanics Class – “Pure Torsion”



$$\theta = \frac{TL}{GJ}$$

Torsion


↔



$$\frac{d\theta}{dx} = \frac{M}{EI}$$

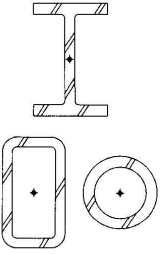
Bending

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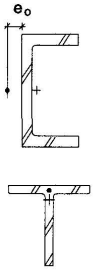


Background - Torsion

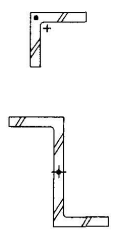
- From Your Undergrad Engineering Mechanics Class?
 - How many cantilevered, solid round bars are used in steel building structural elements? Not many – most are like those shown. Consequences?



(a) doubly symmetric shapes, shear center and centroid coincide




(b) singly symmetric shapes



(c) unsymmetric shapes

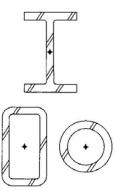
+ centroid • shear center

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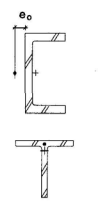


Background - Torsion

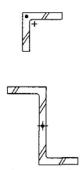
- From Your Undergrad Engineering Mechanics Class?
 - Consequences? New worries with these sections – shear flow, shear center, determining J.



(a) doubly symmetric shapes, shear center and centroid coincide

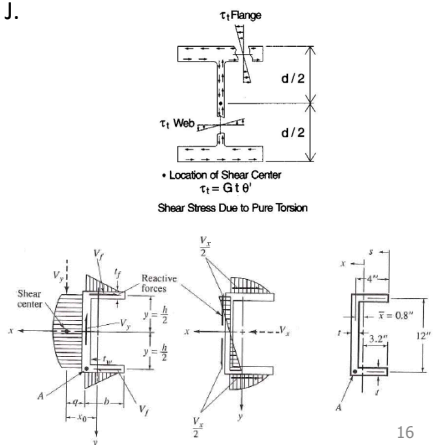


(b) singly symmetric shapes




(c) unsymmetric shapes

+ centroid • shear center



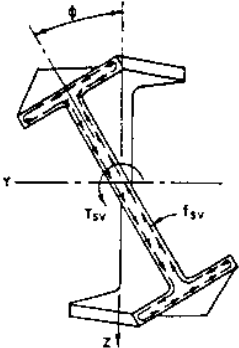
• Location of Shear Center
 $\tau_t = G t \theta'$
Shear Stress Due to Pure Torsion

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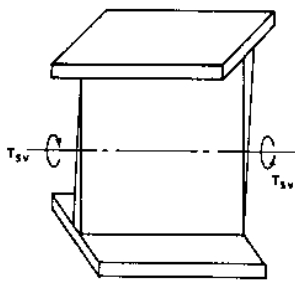


Background - Torsion

- From Your Undergrad Engineering Mechanics Class?
 - More consequences?
 - Pure (St. Venant's) vs. Warping Torsion.




ST. VENANT TORSION




WARPING OF CROSS SECTION


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Background - Torsion

- Why Do We Care?
 - Even Though Publications We Use Say/Show This:






Torsional Analysis of
Structural Steel Members

2.3 Avoiding and Minimizing Torsion






The commonly used structural shapes offer relatively poor resistance to torsion. Hence, it is best to avoid torsion by detailing the loads and reactions to act through the shear center of the member. However, in some instances, this may not always be possible. AISC (1994) offers several suggestions for eliminating torsion; see pages 2-40 through 2-42. For

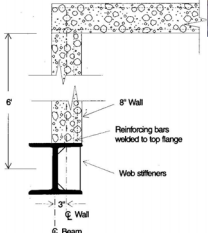
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Background - Torsion

- Why Do We Care?
 - We Run Into Situations Like This:









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Background - Torsion

- Why Do We Care?
 - AND too much twist can be a bad thing





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A Few Fundamentals

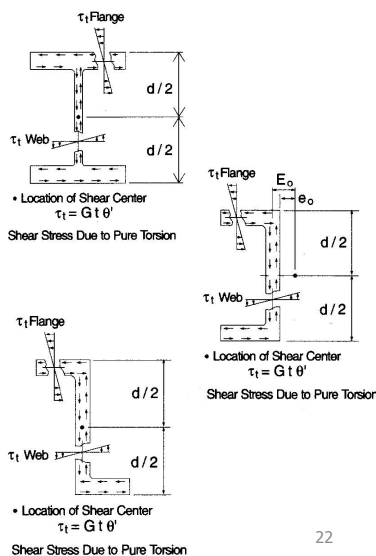
- Terms You May (or May Not) Know

- Shear Flow
 - Again, Wiki:

The gradient of a shear stress force through the body (in solid mechanics)


The flow induced by such a force gradient (in a fluid)

- Both definitions applicable?



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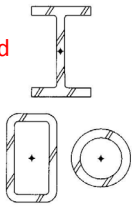


A Few Fundamentals

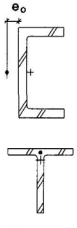
- Terms You May (or May Not) Know
 - Shear Center (Wiki!!)

“An imaginary point on a section, where a shear force can be applied without inducing any torsion”

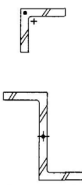
- Sometimes coincides with centroid (center of area)
- How establish? Look @ “twist equilibrium” in-plane. No twist occurs due to in-plane shears that develop due to flexure – location where they cancel each other out is shear center.



(a) doubly symmetric shapes, shear center and centroid coincide




(b) singly symmetric shapes



(c) unsymmetric shapes

+ centroid • shear center

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A Few Fundamentals

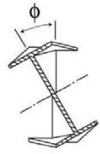
- Terms You May (or May Not) Know (NO WIKI!!)
 - Pure (St. Venant's) Torsion

Planar rotation of a structural element. Generates in-plane shear stresses.

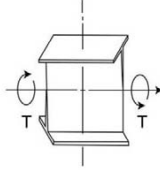
- Warping Torsion

Tendency of portions of structural element to move out of plane. If out of plane movement not prevented, no stresses developed. If prevented, generates BOTH in-plane shear stresses and stresses normal to plane.

ALL THIN WALLED SECTIONS WANT TO WARP!! DIFFERENCES RELATE TO HOW MUCH. CAN IT BE IGNORED?




Rotated Cross Section



Warped Section

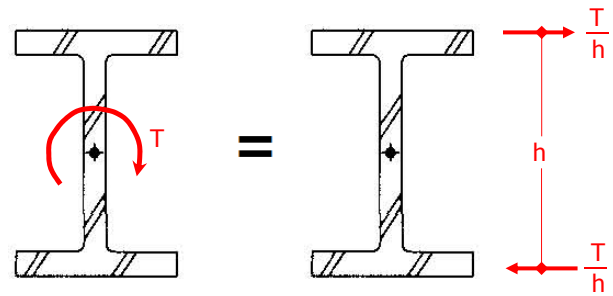
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A Few Fundamentals

- Warping Torsion

Can also be seen as a force couple to each flange



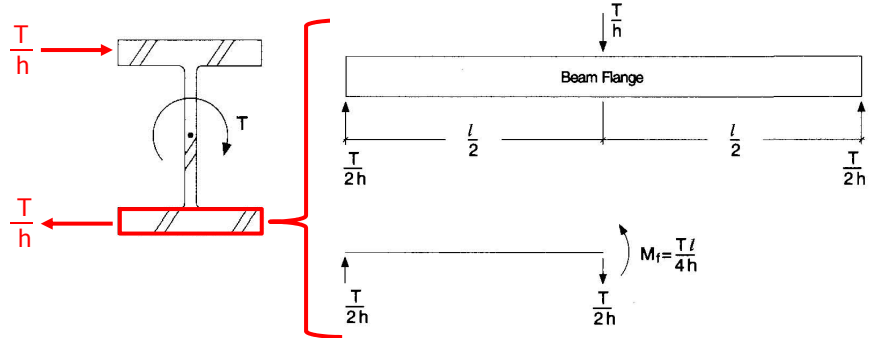
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A Few Fundamentals

- Warping Torsion

Now lets look at the bottom flange



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A Few Fundamentals

A) ST. VENANT-TORSIONAL BEHAVIOR

B) WARPIING-TORSIONAL BEHAVIOR

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What Do I Do? Design

- AISC Manual – Art. H3.2 for HSS
 - HSS Subject to Combined Torsion, Shear, Flexure and Axial Force. INTERACTION approach w/ Eqn. H3-6:

$$\left(\frac{P_r}{P_c} + \frac{M_r}{M_c} \right) + \left(\frac{V_r}{V_c} + \frac{T_r}{T_c} \right)^2 \leq 1.0$$

- $T_r < 0.2 * T_c$, ignore torsion.
- T_c prescribed in Eqns. H3-2a or H3-2b.

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What Do I Do? Design

- AISC Manual – Art. H3.3 for non-HSS
 - Non-HSS Members Subjected to Torsion and Combined Stress. Following STRESS LIMITS Apply.
 - Yielding under normal stress (Eqn. H3-7):

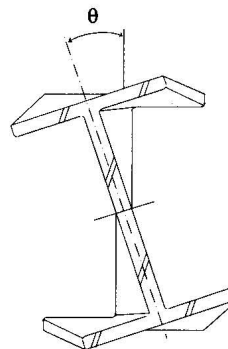
$$F_n = F_y$$

- Shear yielding (Eqn. H3-8):

$$F_n = 0.6F_y$$

- Buckling (Eqn. H3-9):

$$F_n = F_{cr}$$



Rotated Cross Section

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What Do I Do? Analysis

- AISC DG9 – Cumulative Stress from Superposition, using Proper Signs

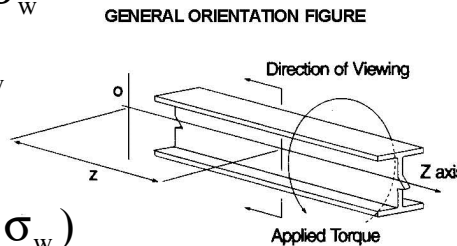
$$f_n = \sigma_a \pm \sigma_{bx} \pm \sigma_{by} \pm \sigma_w$$

$$f_v = \tau_{bx} \pm \tau_{by} \pm \tau_t \pm \tau_w$$

I-Shapes:

$$f_n = \sigma_a \pm (\sigma_{bx} + \sigma_{by} + \sigma_w)$$

$$f_v = \tau_{bx} + \tau_{by} + \tau_t + \tau_w$$



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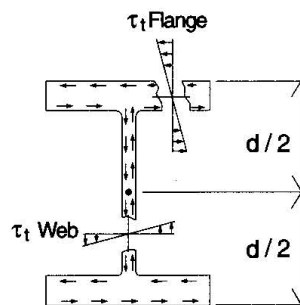


What Do I Do? Analysis

- Determine All Contributors to Stress States
 - Shear
 - St. Venant's Torsion

$$\tau_t = Gt\theta'$$


G = shear modulus
 t = element thickness
 θ' = Rate of change of θ



• Location of Shear Center
 $\tau_t = Gt\theta'$
Shear Stress Due to Pure Torsion

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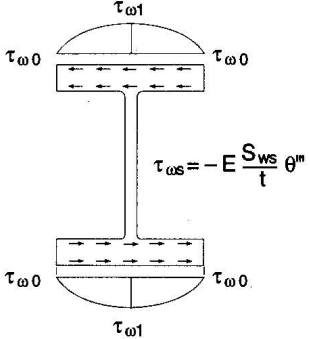


What Do I Do? Analysis

- Determine All Contributors to Stress States
 - Shear
 - Warping Torsion

$$\tau_{ws} = \frac{-ES_{ws}\theta'''}{t}$$


E = elastic modulus
 S_{ws} = warping statical moment at s
 $= hb^2t/16$
 t = element thickness
 $\theta''' = 3^{\text{rd}}$ derivative of θ



$\tau_{\omega s} = -E \frac{S_{ws}}{t} \theta'''$

Shear Stress Due to Warping

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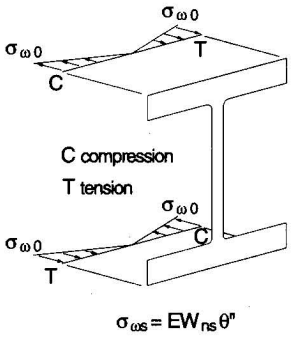


What Do I Do? Analysis

- Determine All Contributors to Stress States
 - Normal
 - Warping Torsion

$$\sigma_{ws} = EW_{ns}\theta''$$


E = elastic modulus
 W_{ns} = normalized warping function at s
 $= hb/4$
 $\theta'' = 2^{\text{nd}}$ derivative of θ



$\sigma_{\omega s} = EW_{ns}\theta''$

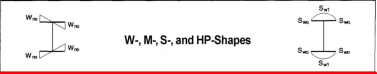
Normal Stress Due to Warping

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What Do I Do? Analysis

Appendix A
TORSIONAL PROPERTIES

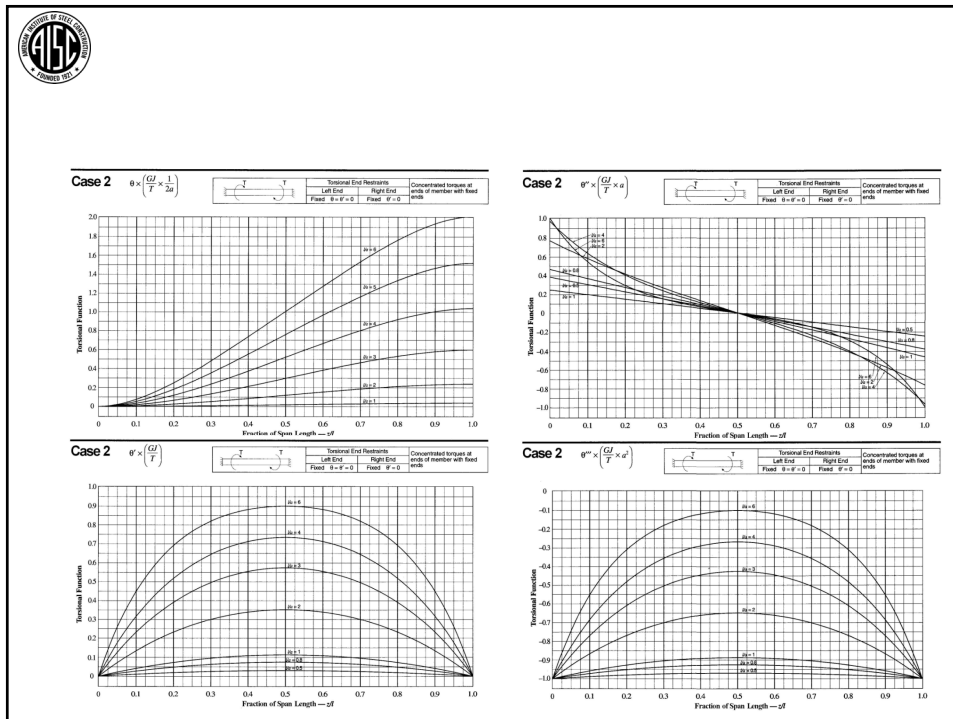


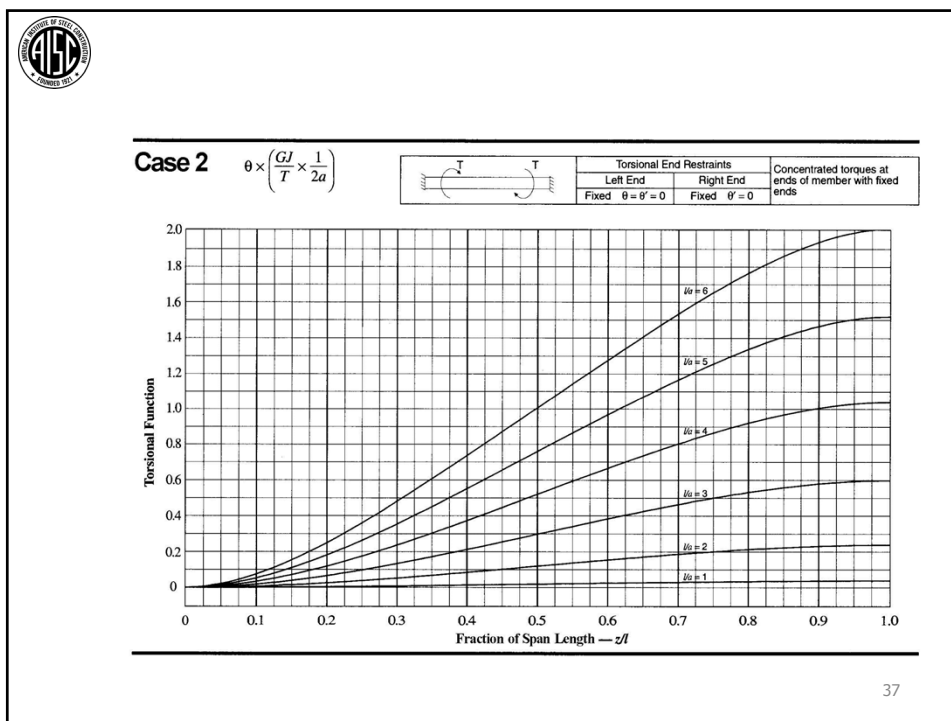
W-, M-, S-, and HP-Shapes

Shape	Torsional Properties					Static Moments	
	J in. ⁴	C_w in. ⁶	a in.	W_{no} in. ²	S_w1 in. ³	Q_r in. ³	Q_w in. ³
W44x335	74.4	536,000	137	168	1,190	282	811
335	51.5	400,000	109	125	866	204	596
230	24.9	346,000	190	164	789	194	551

Shape	Torsional Properties					Static Moments	
	J in. ⁴	C_w in. ⁶	a in.	W_{no} in. ²	S_w1 in. ³	Q_r in. ³	Q_w in. ³
W44x335	74.4	536,000	137	168	1,190	282	811
335	51.5	400,000	109	125	866	204	596
230	24.9	346,000	190	164	789	194	551

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What Do I Do? Analysis


- Approximations to St. Venant's, Warping Stresses – DG9 and others
 - Warping – Torque resolved into flange forces. Those forces on flange “beam” generate shear and bending stresses – approximate using beam theory (DG 9).

$$\tau_w = \frac{1.5V_f}{b_f t_f}$$

$$\sigma_w = \frac{M_f}{S_f}$$


The diagram illustrates the resolution of a torque T applied to an I-beam into two equal and opposite forces T/h acting on the top and bottom flanges. Below this, a beam flange model is shown with a length l and a height $2h$. Shear forces $T/2h$ are applied at the ends, and a bending moment $M_f = Tl/4h$ is shown at the center.

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Where Do I Go for More Help?

- Buildings
 - Seaburg, P.A. and Carter, C. J. AISC Steel Design Guide Series #9, Torsional Analysis of Structural Steel Members, American Institute of Steel Construction, 2003.
 - Steel Construction Manual, 14th Ed., American Institute of Steel Construction, 2011.
- Bridges
 - AASHTO/NSBA G 13.1 – Guidelines for Steel Girder Bridge Analysis (2011), <http://www.aisc.org/contentNSBA.aspx?id=20130>
 - AISC/NSBA Steel Bridge Design Handbook, <http://www.aisc.org/contentNSBA.aspx?id=20244>
- General
 - Salmon, C.G., Johnson, J.E. and Malhas, F.A., Steel Structures – Design and Behavior, 5th Ed., Pearson Prentice Hall, 2009.
 - Young, W. and Budynas, R., Roark's Formulas for Stress and Strain, 7th Ed., McGraw Hill, 2001.
 - Your undergrad mechanics textbook
 - Your undergrad steel design textbook



Torsional Analysis of Structural Steel Members

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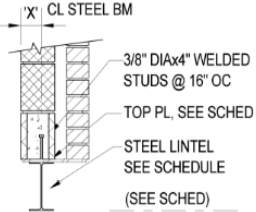
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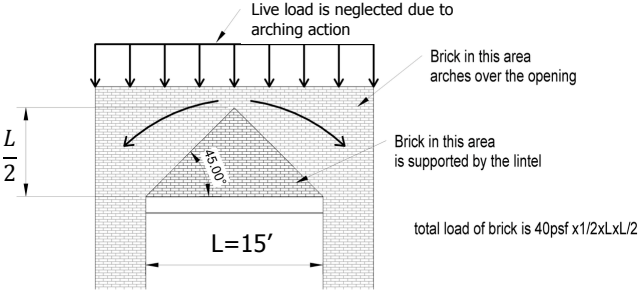


Example

Steel lintel beam spanning opening in a bearing wall building




CL STEEL BM
3/8" DIAx4" WELDED STUDS @ 16" OC
TOP PL, SEE SCHED
STEEL LINTEL SEE SCHEDULE (SEE SCHED)



Live load is neglected due to arching action
Brick in this area arches over the opening
Brick in this area is supported by the lintel
total load of brick is $40\text{psf} \times \frac{1}{2} \times L \times \frac{L}{2}$
 $L = 15'$
 $\frac{L}{2}$

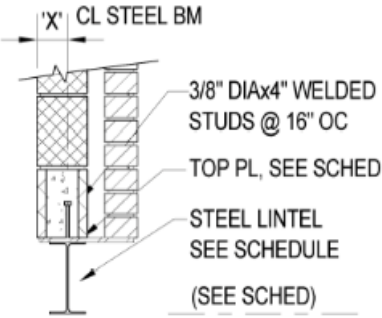
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Design approach including torsion...

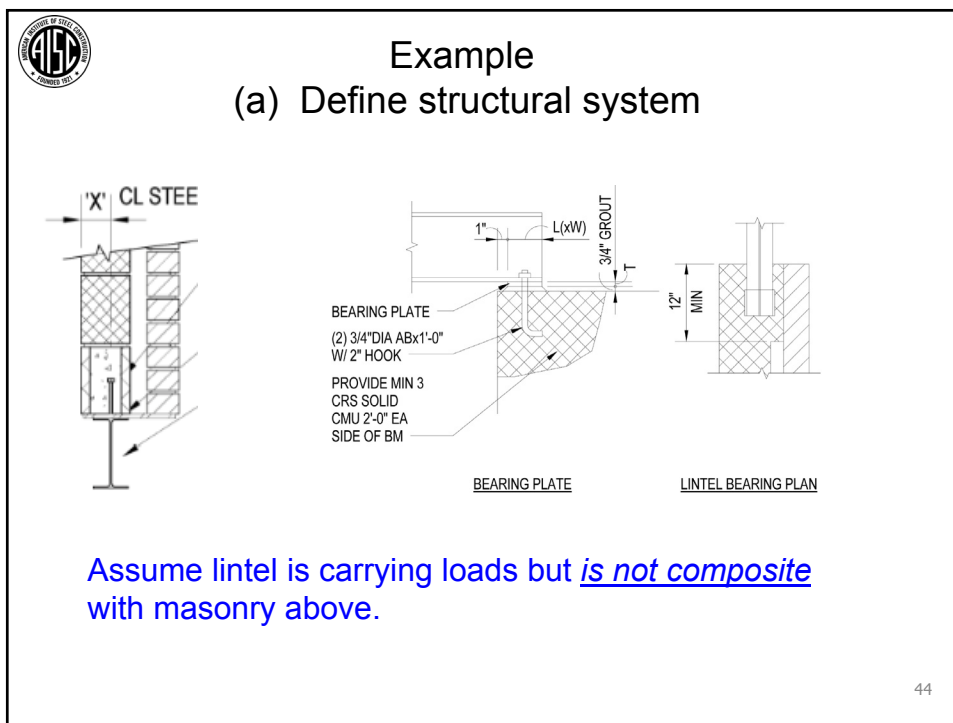
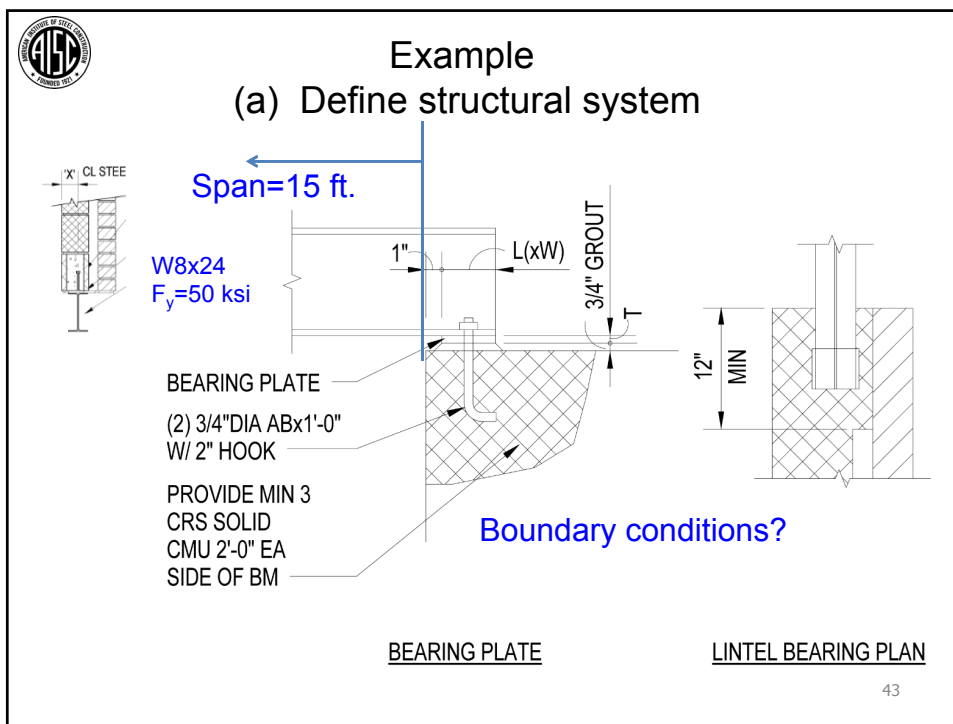
Steel lintel beam spanning opening in a bearing wall building




CL STEEL BM
3/8" DIAx4" WELDED STUDS @ 16" OC
TOP PL, SEE SCHED
STEEL LINTEL SEE SCHEDULE (SEE SCHED)

- (a) Define structural system – span, boundary conditions, materials
- (b) Find member demand shear V , moment M , torsion T , and axial force P
- (c) Calculate angle of twist θ and its derivatives
- (d) Check $M+T+P$ normal stresses
- (e) Check $V+T$ shear stresses

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Example

(a) Define structural system

BEARING PLATE
(2) 3/4" DIA ABx1'-0"
W/ 2" HOOK

PROVIDE MIN 3
CRS SOLID
CMU 2'-0" EA
SIDE OF BM

Boundary conditions?


Moment

OR

Torsion

OR

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Example

(a) Define structural system

Boundary conditions?

Torsion


OR

Twist fixed
Warping free

θ

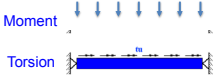
Twist fixed
Warping fixed

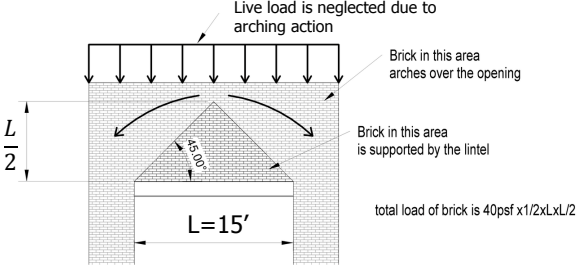
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Example

(b) Find member demand shear V , moment M , torsion T , and axial force P






For simplicity, we will approximate the triangular load as a uniform load
Therefore we need w_{facade} , $w_{masonry}$

$p_{facade} = 40 \text{ lb/ft}^2$

$w_{masonry} = 60 \text{ lb/ft}^2$

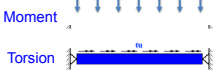
$w_{facade} = 40 \text{ psf} \left(\frac{15'^2}{4} \right) \left(\frac{1}{15'} \right) = 150 \text{ plf}$

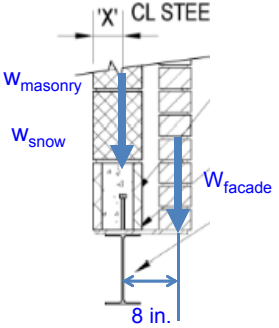
$w_{masonry} = 60 \text{ psf} \left(\frac{15'^2}{4} \right) \left(\frac{1}{15'} \right) = 225 \text{ plf}$



Example

(b) Find member demand shear V , moment M , torsion T , and axial force P






LRFD – factored loads!

$U = 1.4D$

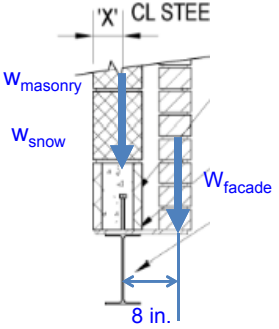
$V_u = 1.4(150 \text{ plf} + 225 \text{ plf}) \left(\frac{15'}{2} \right) = 3.9 \text{ kips}$

$M_u = 1.4(150 \text{ plf} + 225 \text{ plf}) \left(\frac{15^2}{8} \right) = 14.8 \text{ kip} \cdot \text{ft}$

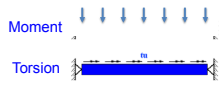


Example


(b) Find member demand shear V , moment M , torsion T , and axial force P



$$t_u = 1.4(150 \text{ plf}) \left(\frac{8''}{12} \right) = 0.14 \frac{\text{kip} * \text{ft}}{\text{ft}}$$

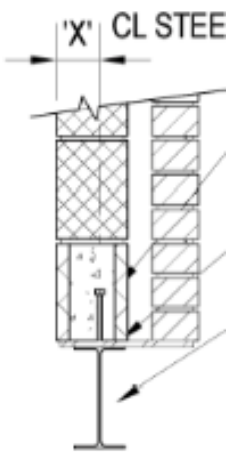


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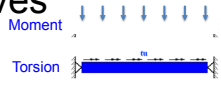
Example

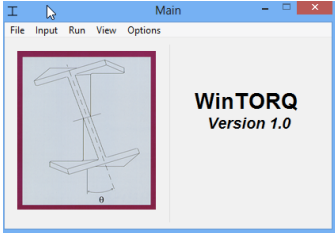
(c) Calculate angle of twist, derivatives




But there is software to help, for example WinTORQ!

<http://www.steeltools.org/resources/viewdocument/?DocumentKey=45f39369-2ac2-4a33-a131-7e727afc8cab>



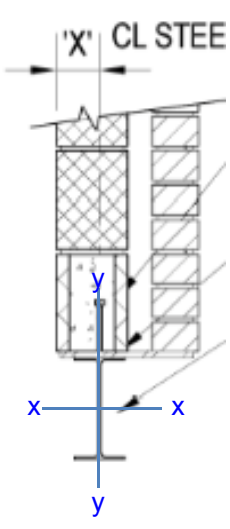


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Example

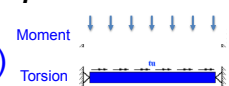
(d) Check normal stresses $P+M+T$




Demand stresses (bending)

$$f_n = \sigma_a \pm (\sigma_{bx} + \sigma_{by} + \sigma_w)$$

$$\sigma_{bx} = \frac{Mc}{I} = \frac{14.8 \text{ kip} \cdot \text{ft} (12''/\text{ft}) \frac{7.93''}{2}}{82.7 \text{ in}^4} = 8.5 \text{ ksi}$$

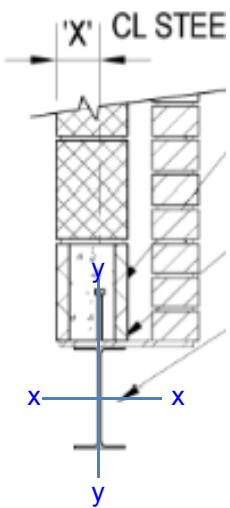


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Example

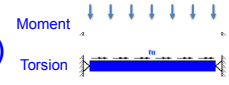
(d) Check normal stresses $P+M+T$

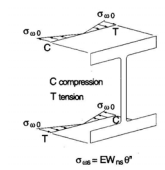


Demand stresses (torsion)

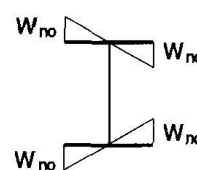
$$f_n = \sigma_a \pm (\sigma_{bx} + \sigma_{by} + \sigma_w)$$

$$\sigma_w = EW_{no} \theta''$$

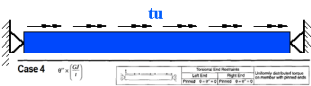


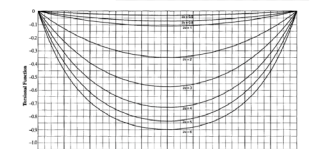


$\sigma_{ws} = EW_{no} \theta''$
Normal Stress Due to Warping



Torsion





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Example
(d) Check normal stresses $P+M+T$

$\theta'' \times \left(\frac{GJ}{t}\right)$

Case 4 $\theta'' \times \left(\frac{GJ}{t}\right)$

$L/a = \frac{15'(12)}{43.8} = 4.11$

$$-0.75 = \theta'' \left(\frac{11200 \text{ ksi} \times 0.35 \text{ in}^4}{0.14 \frac{\text{kip} \cdot \text{in}}{\text{in}}} \right) \qquad \theta'' = -2.68E - 5 \text{ rad/in}^2$$

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Example
(d) Check normal stresses $P+M+T$

Demand stresses (torsion)

$$f_n = \sigma_a \pm (\sigma_{bx} + \sigma_{by} + \sigma_w)$$

$$\theta'' = 2.08E - 5 \frac{\text{rad}}{\text{in}^2}$$


$$\sigma_w = E W_{no} \theta''$$

$$\sigma_w = 29000 \text{ ksi} (12.2 \text{ in}^2) \left(2.68E - 5 \frac{\text{rad}}{\text{in}^2} \right) = 9.5 \text{ ksi}$$

$$f_n = 0 \pm (8.5 \text{ ksi} + 0 + 9.5 \text{ ksi}) = 18.0 \text{ ksi}$$

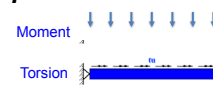
54

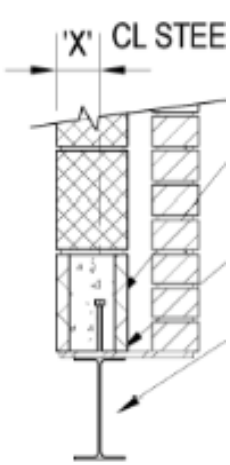




Example

(d) Check normal stresses $P+M+T$





Beam capacity...

Yielding under normal stress (Eqn. H3-7):

$$F_n = F_y$$


Buckling (Eqn. H3-9): Take the minimum F_n from Eq. H3-7 and H3-9!

$$F_n = F_{cr}$$

$f_n \leq \phi_T F_n$ Compare capacity to demand

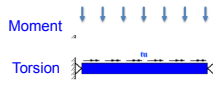
$F_n = F_y = 50 \text{ ksi}$
 $\phi F_n = 0.9(50 \text{ ksi}) = 45 \text{ ksi}$
 $f_n = 18.0 \text{ ksi} \leq \phi F_n = 45.0 \text{ ksi}$ OK

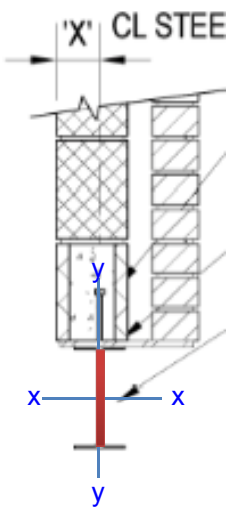
55



Example

(e) Check shear stresses $V+T$






Demand stresses (in web)

$$f_v = \tau_{bx} + \tau_{by} + \tau_t + \tau_w$$

$$\tau_{by} = \frac{V_u Q_w}{I_x t_w}$$
 Direct shear

$$\tau_{by} = \frac{3.9 \text{ kip} (11.6 \text{ in}^3)}{82.7 \text{ in}^4 (0.245 \text{ in})} = 2.23 \text{ ksi}$$

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Example

(e) Check shear stresses V+T

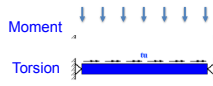
Demand stresses (in web)

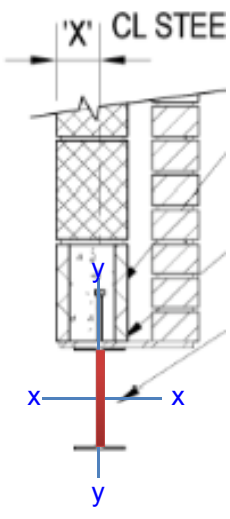
$$f_v = \tau_{bx} + \tau_{by} + \tau_t + \tau_w$$

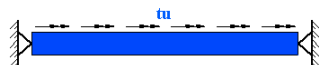
$$\tau_t = Gt_w \theta'$$

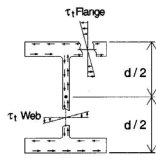
Shear stresses from St. Venant torsion

Torsion

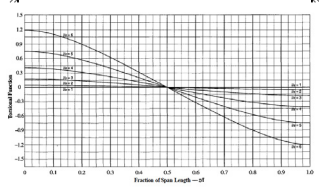









Location of Shear Center
 $\tau_t = Gt_w \theta'$
Shear Stress Due to Pure Torsion



θ'

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Example

(e) Check shear stresses V+T

Demand stresses (in web)

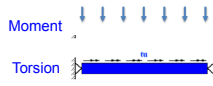
$$f_v = \tau_{bx} + \tau_{by} + \tau_t + \tau_w$$

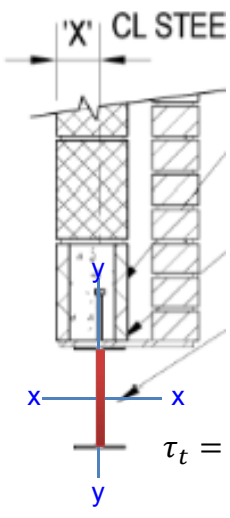
$$\tau_t = Gt_w \theta'$$

Shear stresses from St. Venant torsion


$$\theta' = 1.70E - 3 \frac{rad}{in}$$

$$\tau_t = 11200 \text{ ksi} (0.245 \text{ in}) \left(1.70E - 3 \frac{rad}{in} \right) = 4.67 \text{ ksi}$$





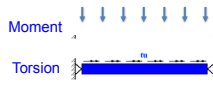
58

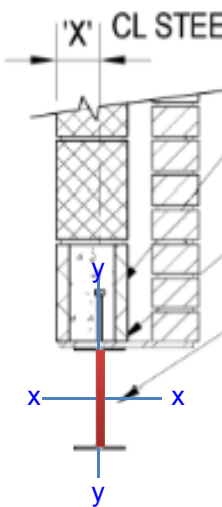


Example

(e) Check shear stresses V+T

Demand stresses (in web)






$$f_v = \tau_{bx} + \tau_{by} + \tau_t + \tau_w$$

$$f_v = 2.23 \text{ ksi} + 0 + 4.67 \text{ ksi} + 0 = 6.90 \text{ ksi}$$

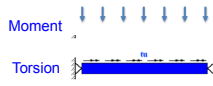
59

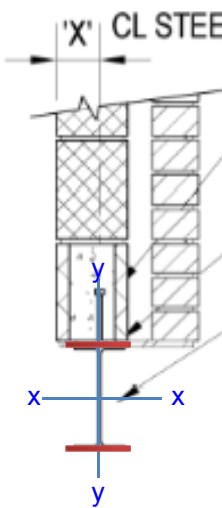


Example

(e) Check shear stresses V+T

Demand stresses (in flange)

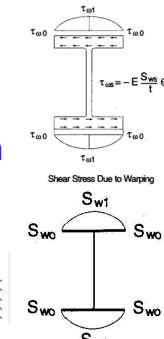


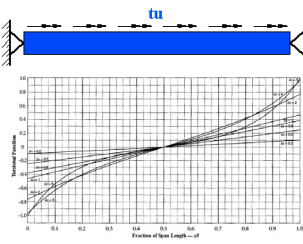


$$f_v = \tau_{bx} + \tau_{by} + \tau_t + \tau_w$$


$$\tau_{ws} = \frac{-ES_{ws} \theta'''}{t_f}$$

Shear stresses from warping torsion





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Example

(e) Check shear stresses V+T

Demand stresses (in flange)

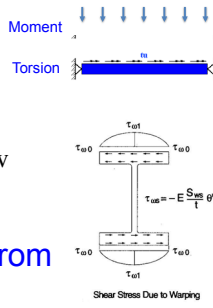
$$f_v = \tau_{bx} + \tau_{by} + \tau_t + \tau_w$$

$$\tau_{ws} = \frac{-ES_{ws} \theta'''}{t_f}$$


Shear stresses from warping torsion

$$\theta''' = 7.90E - 7 \frac{rad}{in^2}$$

$$\tau_{ws} = \frac{-29000 \text{ ksi}(7.94in^4) (7.90E - 7 \frac{rad}{in^2})}{0.4 \text{ in}} = 0.45 \text{ ksi}$$



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Example

(e) Check shear stresses V+T

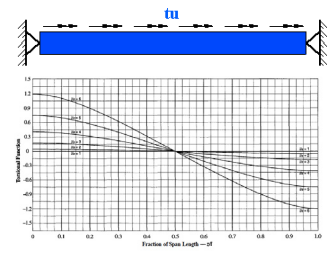
Demand stresses (in flange)

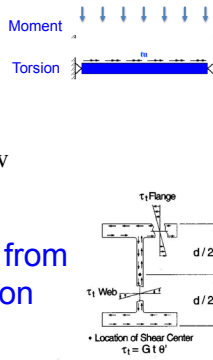
$$f_v = \tau_{bx} + \tau_{by} + \tau_t + \tau_w$$

$$\tau_t = Gt_f \theta'$$


Shear stresses from St. Venant torsion

Torsion





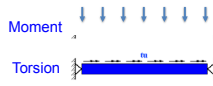
62

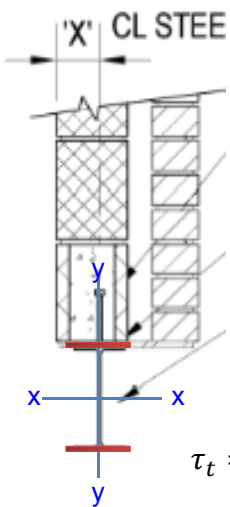


Example

(e) Check shear stresses $V+T$

Demand stresses (in flange)





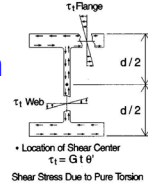
$$f_v = \tau_{bx} + \tau_{by} + \tau_t + \tau_w$$

$$\tau_t = Gt_f \theta'$$


Shear stresses from St. Venant torsion

$$\theta' = 1.70E - 3 \frac{rad}{in}$$

$$\tau_t = 11200 \text{ ksi}(0.4 \text{ in}) \left(1.70E - 3 \frac{rad}{in} \right) = 7.62 \text{ ksi}$$



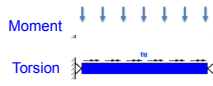
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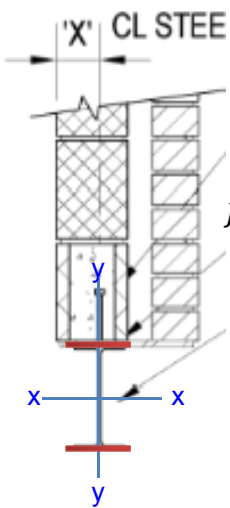


Example

(e) Check shear stresses $V+T$

Demand stresses (in flange)






$$f_v = \tau_{bx} + \tau_{by} + \tau_t + \tau_w$$

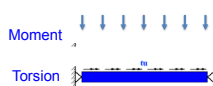
$$f_v = 0 + 0 + 7.62 \text{ ksi} + 0.46 \text{ ksi} = 8.08 \text{ ksi}$$

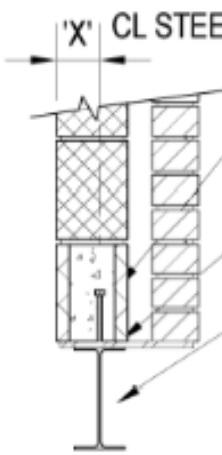
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Example

(e) Check shear stresses V+T





Web/flange capacity...

Yielding under normal stress (Eqn. H3-7):

$$F_n = 0.6F_y$$

$$f_v \leq \phi_T F_n \quad \text{Compare capacity to demand}$$


$$F_v = 0.6F_y = 30 \text{ ksi}$$

$$\phi F_v = 0.9(30 \text{ ksi}) = 27 \text{ ksi}$$

$$F_v = 8.08 \text{ ksi (flange)} \leq \phi F_v = 27.0 \text{ ksi}$$

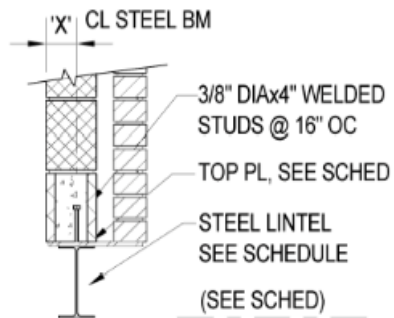
OK

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Design approach including torsion...

Steel lintel beam spanning opening in a bearing wall building



(a) Define structural system – span, boundary conditions, materials

(b) Find member demand shear V , moment M , torsion T , and axial force P

(c) Calculate angle of twist θ and its derivatives

(d) Check $M+T+P$ normal stresses

(e) Check $V+T$ shear stresses

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References

- AASHTO/NSBA G 13.1 – Guidelines for Steel Girder Bridge Analysis (2011)
- Domalik, D.E., Shura, J.F. and Linzell, D.G., "Design and Field Monitoring of Horizontally Curved Steel Plate Girder Bridge," *Transportation Research Record, Journal of the Transportation Research Board No. 1928*, pp. 83-91, 2005.
- Salmon, C.G., Johnson, J.E. and Malhas, F.A., *Steel Structures – Design and Behavior*, 5th Ed., Pearson Prentice Hall, Upper Saddle River, NJ, 2009.
- Seaburg, P.A. and Carter, C. J. *AISC Steel Design Guide Series #9, Torsional Analysis of Structural Steel Members*, American Institute of Steel Construction, Chicago, IL, 2003.
- <http://www.news.com.au/national-news/melbourne-teacher-under-investigation-over-alleged-punishments/story-e6frtkvr-1226035003739>
- http://www.gestech.net/shaft_torsional_failure1.htm
- http://www.proactivefluidpower.com/shaft_failures.htm
- http://www.ecourses.ou.edu/cgi-bin/ebook.cgi?doc=&topic=me&chap_sec=02.2&page=theory
- <http://www.transtutors.com/homework-help/mechanical-engineering/torsion/shafts-circular-section.aspx>
- <http://www.renovateforum.com/f83/hhow-much-can-c-purlin-span-shed-frame-53666/>
- <http://www.structuremag.org/article.aspx?articleid=527>
- <http://faculty.kirkwood.edu/jlopez/details/floor004.jpg>
- <http://www.gostructural.com/magazine-article-gostructural-com-4-2010-structural-detailing-solutions-to-avoid-thermal-bridging-7838.html>
- <http://www.pascalsteel.com/content/girts-and-panel-metal-building>
- <http://alviassociates.com/awards>
- <http://appliedconceptengineering.com.au/construction/structural/rounded-steel-frames>
- http://orthostreams.com/wp-content/uploads/2013/02/OilRig_OilRig_WEB.jpg

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There's always a solution in steel.

Thank You

Please give us your feedback!
Survey at conclusion of webinar.

