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## Course Description

### **Where Did That Force Come From?**

October 23, 2014

This presentation addresses the derivation of design forces for braced frame beams and their connections for various loading conditions. In particular, the live webinar focuses on the combination of frame-design and diaphragm-design forces. The presentation will give a methodology for determining consistent sets of design forces based on increasing levels of complexity. Emphasis will be placed on clear free body diagrams and consistent sets of forces corresponding to clear and understandable load conditions for the frame.



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## Learning Objectives

- Become familiar with the design challenges when combining frame and diaphragm forces.
- Gain an understanding of the anticipated behavior, particularly for seismic systems.
- Learn and understand how to reconcile design forces in braced-frame connections.
- Gain an understanding of a practical methodology for determining consistent sets of design forces.



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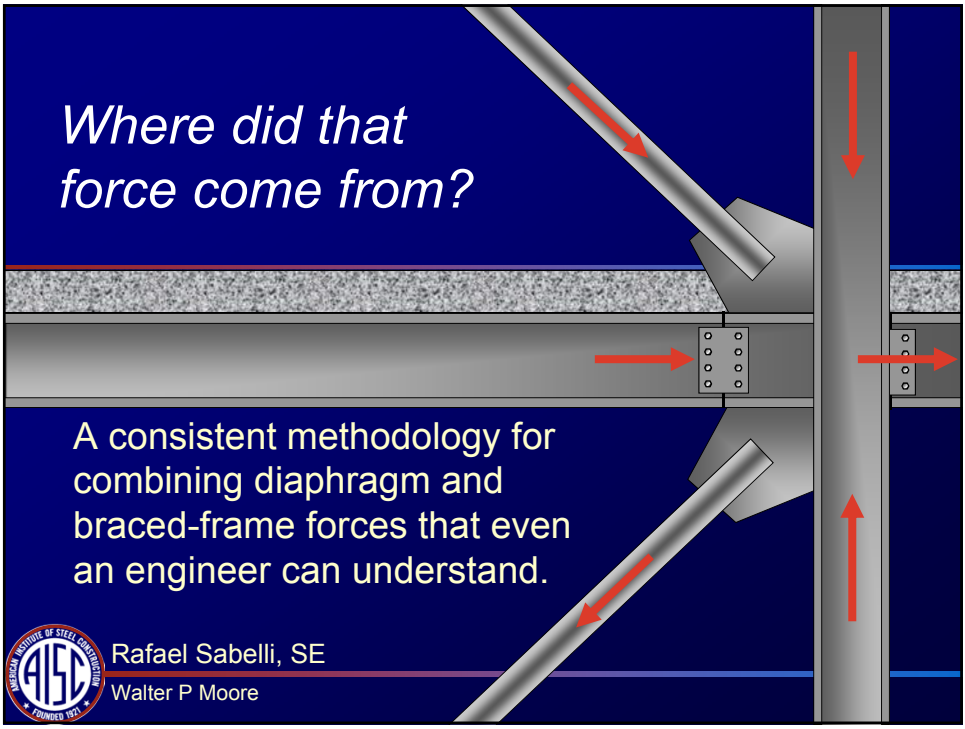
### *Today's AISC Live Webinar*

Where Did That Force Come From? Combining Diaphragm and Braced Frame Forces


written and presented by  
Rafael Sabelli, S.E.  
Director of Seismic Design, Walter P. Moore and Associates, San Francisco, CA.



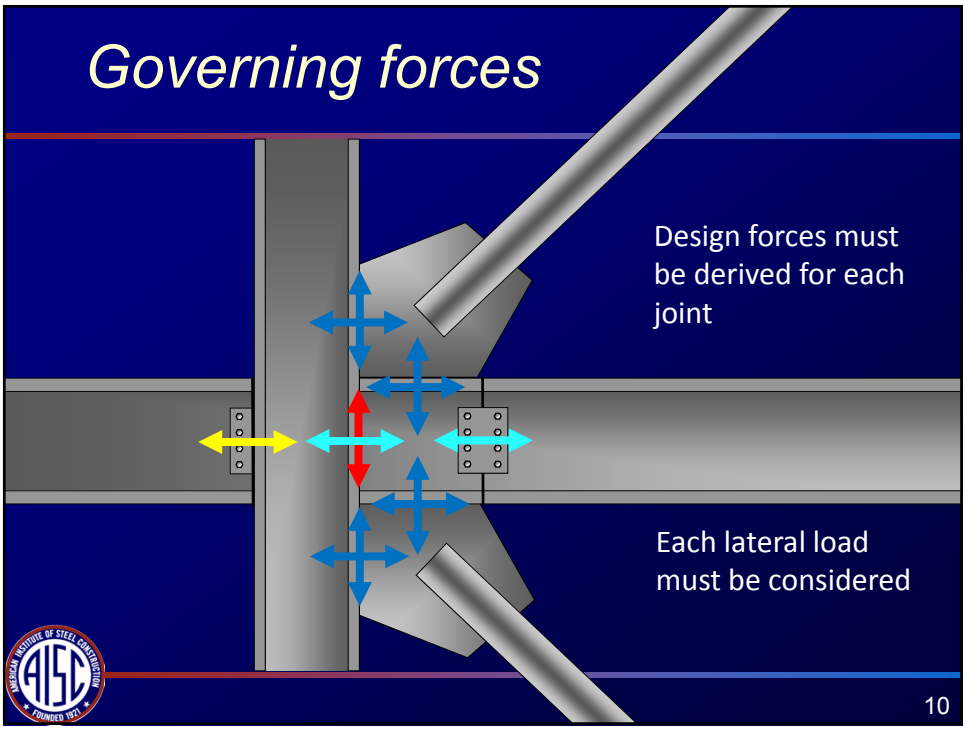
### Where did that force come from?



A consistent methodology for combining diaphragm and braced-frame forces that even an engineer can understand.


 Rafael Sabelli, SE  
Walter P Moore

### Governing forces



Design forces must be derived for each joint

Each lateral load must be considered



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## Types of forces

- Applied load patterns of the design base shear
  - Wind
  - Seismic
- Diaphragm accelerations  $F_p$ 
  - Seismic
  - Inconsistent with design base shear
- Member yielding capacity & system mechanism
  - Seismic
  - Inconsistent with
    - Design base shear
    - $F_p$  forces

Note the  
color coding!



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## Two definitions & an important question

### Analysis:

Application of physical laws and mathematics to compute the deformations, internal forces, and stresses of structures resulting from the application of loads.

### Analysis:

Derivation of forces to permit the design of members and connections resulting in a structure adequate for the anticipated loads.

What are the forces in the braces when the  $F_p$  force is in the diaphragm?


“Zero” would seem to be a poor answer.



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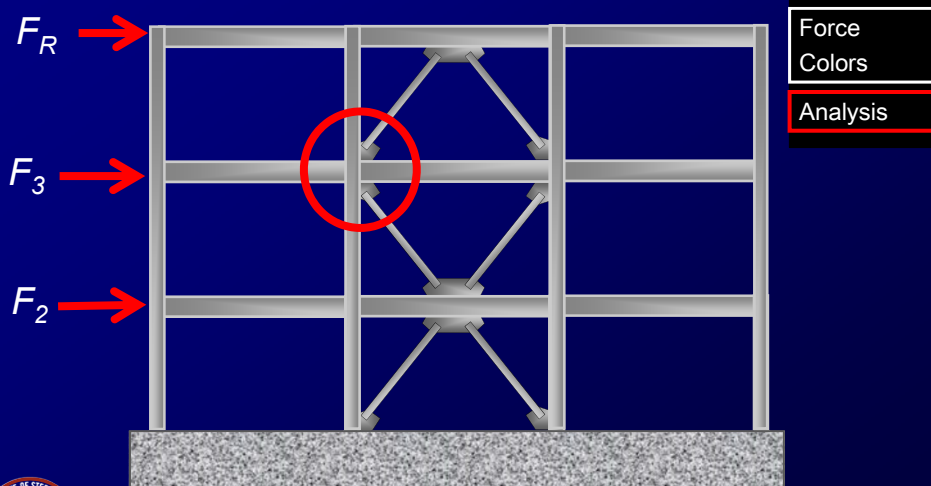
# Outline

Wind	$R=3.25$
Seismic	OCBF
$R=3$	$R>3.25$
SDC B	SCBF
SDC C	EBF
<i>Apply <math>\Omega_o</math> at collectors</i>	BRBF
Numerical example	Post-buckled SCBF
R3BF	Numerical example
	SCBF



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# Wind




$F_R$

$F_3$

$F_2$

Force Colors

Analysis



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### Seismic ( $R=3$ )

$F_R$

$F_3$

$F_2$

$F_{P3}$

Force  
Colors  
Analysis  
Diaphragm

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### Seismic ( $R=3.25$ )

$F_R$

$F_3$

$F_2$

$F_{P3}$

$\Omega_0 E$

$\Omega_0 E$

Force  
Colors  
Analysis  
Diaphragm

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### Seismic ( $R > 3.25$ )

$F_R$

$F_3$

$F_2$

$F_{P3}$

$T_{max}$

$C_{max}$

- Force
- Colors
- Analysis
- Diaphragm
- Capacity

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### Seismic (SCBF)

$F_R$

$F_3$

$F_2$

$F_{P3}$

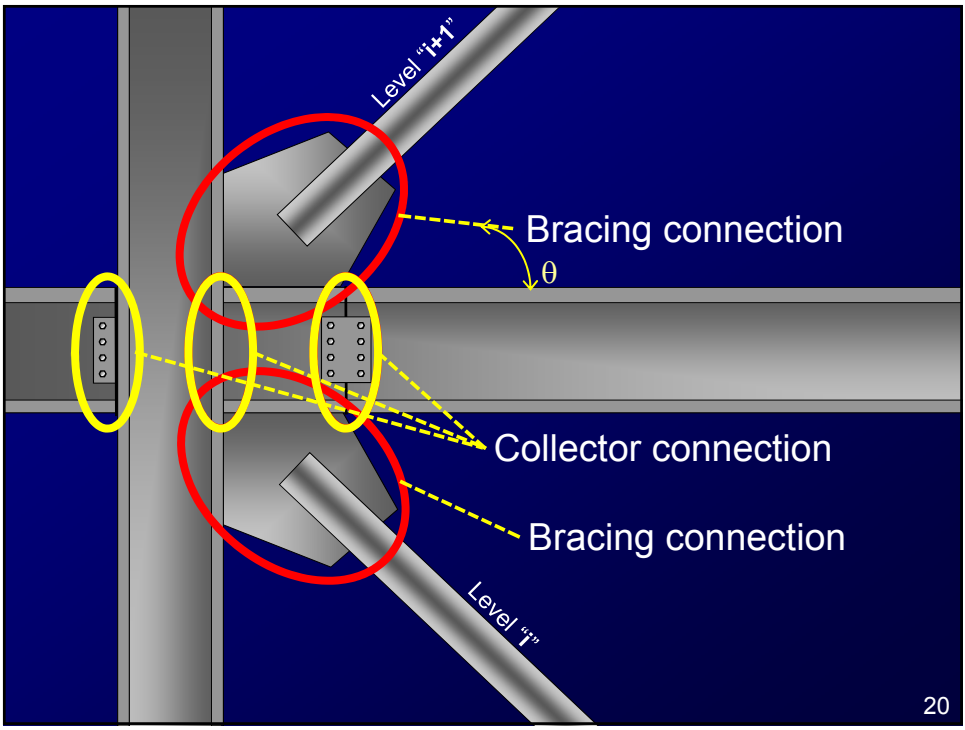
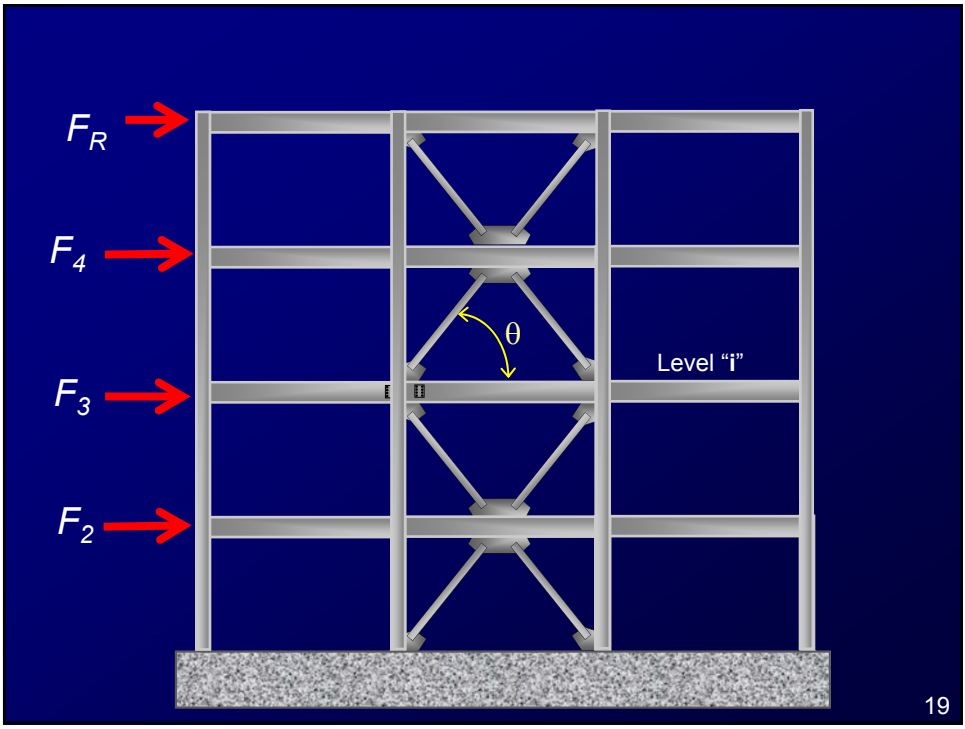
$T_{max}$

$C_{min}$

- Force
- Colors
- Analysis
- Diaphragm
- Capacity
- Post-Buckling

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# Part I:

## Wind



## *Wind*

Each vertical force distribution is sufficient

Can be considered separately

Member forces statically balanced

Direction of load is reversible

Braces change from tension to compression

Gravity shear

Adds to shear from braces

Counteracts shear from braces

Gusset Analysis

Uniform Force Method

Variants



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## Wind

$$F_{coll(i)} + F_{bm(i)} + T_{brace(i+1)} \cos \theta_{(i+1)} = C_{brace(i)} \cos \theta_i$$

$$T_{col(i+1)} + C_{br(i)} \sin \theta_{(i)} + T_{brace(i+1)} \sin \theta_{(i+1)} = T_{col(i)} + V_{bm(i)}$$

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## Gusset Analysis

$e_b = \frac{1}{2}$  beam depth

$e_c = \frac{1}{2}$  column depth

$\alpha$  = column flange or web to centroid of gusset-to-beam connection

$\beta$  = beam flange or web to centroid of gusset-to-column connection

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## Gusset Analysis

$V_c = \frac{\beta}{r} P$	$H_c = \frac{e_c}{r} P$
$H_b = \frac{\alpha}{r} P$	$V_b = \frac{e_b}{r} P$

$$r = \sqrt{(\alpha + e_c)^2 + (\beta + e_b)^2}$$

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## Wind

$$H_{conn(i)} = F_{coll(i)} + H_{c(i+1)} - H_{c(i)}$$

$$= H_{b(i)} - F_{bm(i)} - H_{b(i+1)}$$

$$V_{conn(i)} = V_{bm(i)} - V_{b(i+1)} - V_{b(i)}$$

Force Colors

Analysis

Statics

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## Wind

$$H_{conn(i)} = F_{coll(i)} + H_{c(i+1)} - H_{c(i)}$$

$$= H_{b(i)} - F_{bm(i)} - H_{b(i+1)}$$

Force

Colors

Analysis

Statics

$$V_{conn(i)} = V_{bm(i)} + V_{b(i+1)} + V_{b(i)}$$

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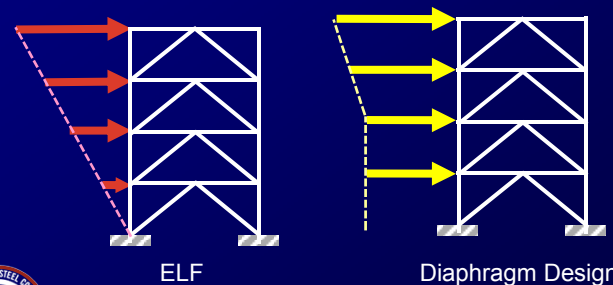
# Part II:

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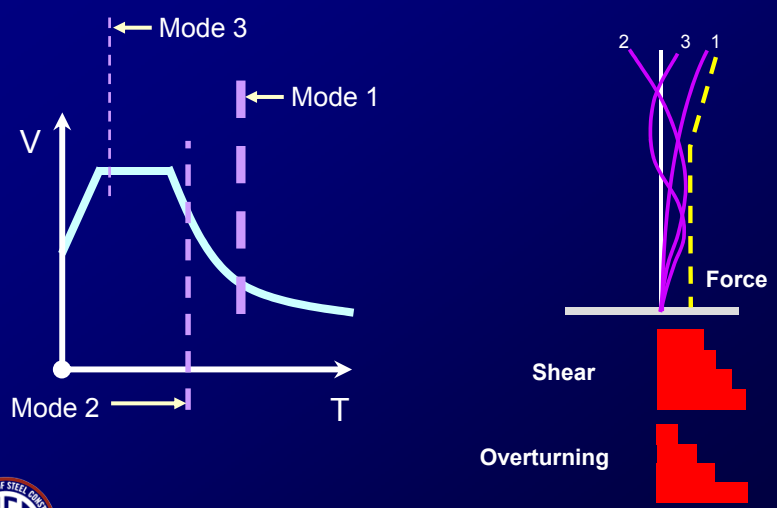
## Seismic *R=3*

# Seismic: $R=3$

Vertical force distribution insufficient



# Modal Response



## ELF vertical distribution

**Force**

**Shear**

**Overturning**

$$C_{vx} = \frac{w_x h_x^k}{\sum_{i=1}^n w_i h_i^k}$$

ASCE 7  
Eq. 12.8-12

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## Diaphragm force coefficients

**Force**

**Overestimated Shear**

**Overestimated Overturning**

$$F_{pi} \leq 0.4 S_{DS} / W_{px}$$

$$F_{px} = \frac{\sum_{i=x}^n F_i}{\sum_{i=x}^n w_i} W_{px}$$

ASCE 7  
Eq. 12.10-1

$$F_{pi} \geq 0.2 S_{DS} / W_{px}$$

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## Diaphragm analysis

Just one example of a collector force distribution

33% 17% 17% 33%

$F_p$   $F_{coll}$   $V$   $F_{chord}$

 There's always a solution in steel

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## Seismic: $R=3$

Vertical force distribution insufficient

Need not abandon static equilibrium

    Create 2 load cases, each satisfying equilibrium

**Case 1**

    Vertical force distribution

    Same procedure as wind

*Member forces statically balanced*

    Governs vertical forces at connection


**Case 2**

    Vertical force distribution with  $F_p$  instead of  $F_i$

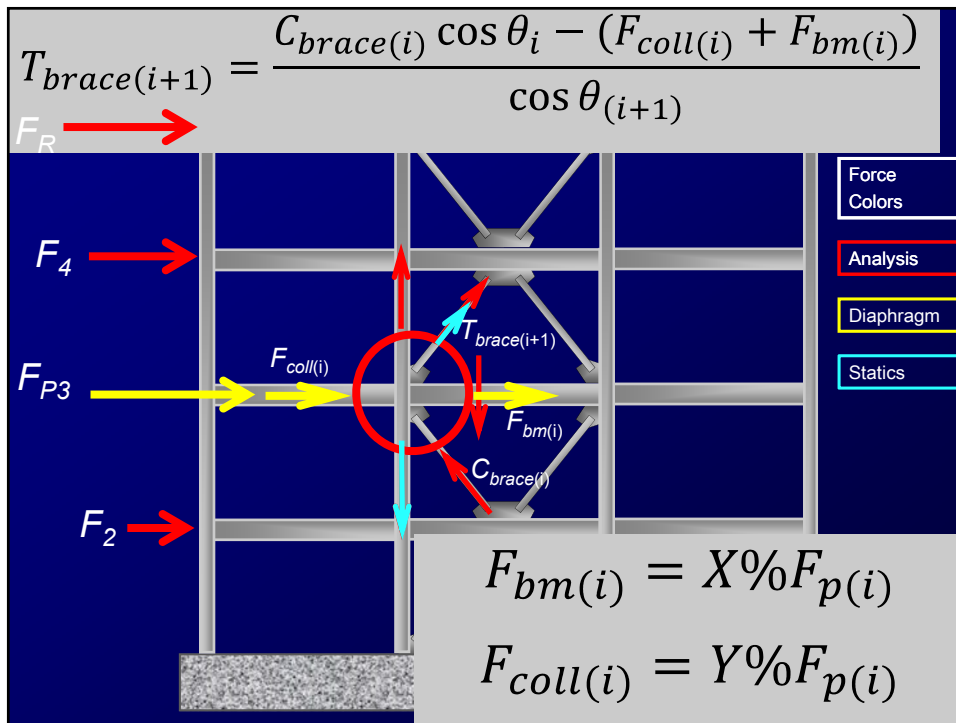
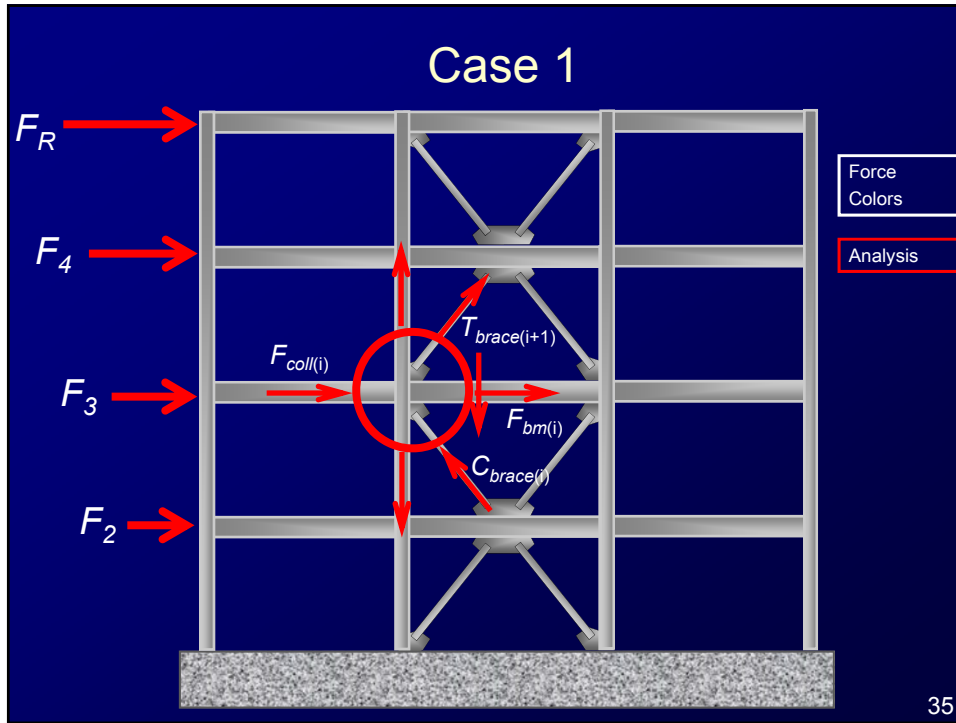
    ➔ *Adjustment need for static equilibrium*

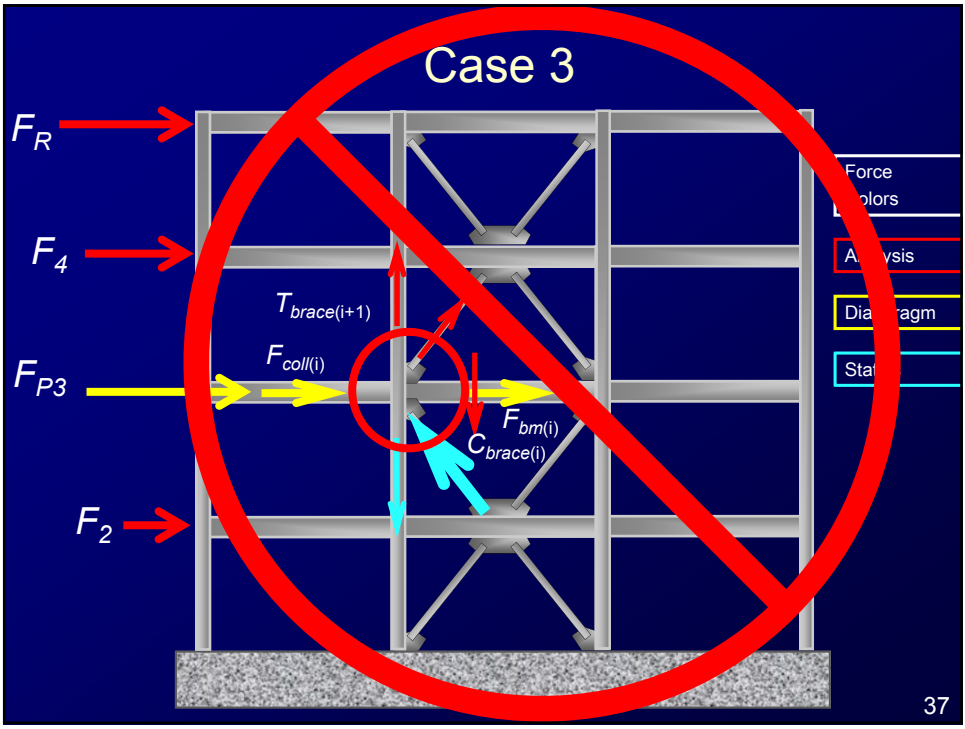
*Apply  $\Omega_0$  to collectors for SDC C*

    May govern horizontal forces at connection



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# Seismic: $R=3$

Footnote: Modal Response Spectrum Analysis →

Member forces lose signs  
 SRSS or CQC combination  
 Assume direction

Member forces not statically balanced

- Case 1b  
*Adjust collector forces*
- Case 2b  
*Adjust brace forces above*



**Case 1b**

$$F_{coll(i)} = C_{brace(i)} \cos \theta_i$$

$$-T_{brace(i+1)} \cos \theta_{(i+1)}$$

$$-F_{bm(i)}$$

Force Colors  
 Analysis  
 MRSA  
 Statics

$$T_{col(i)} = T_{brace(i+1)} \sin \theta_{(i+1)}$$

$$T_{col(i+1)} + C_{br(i)} \sin \theta_{(i)} - V_{bm(i)}$$

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## Modal response spectrum analysis

### Collectors

#### Model collectors

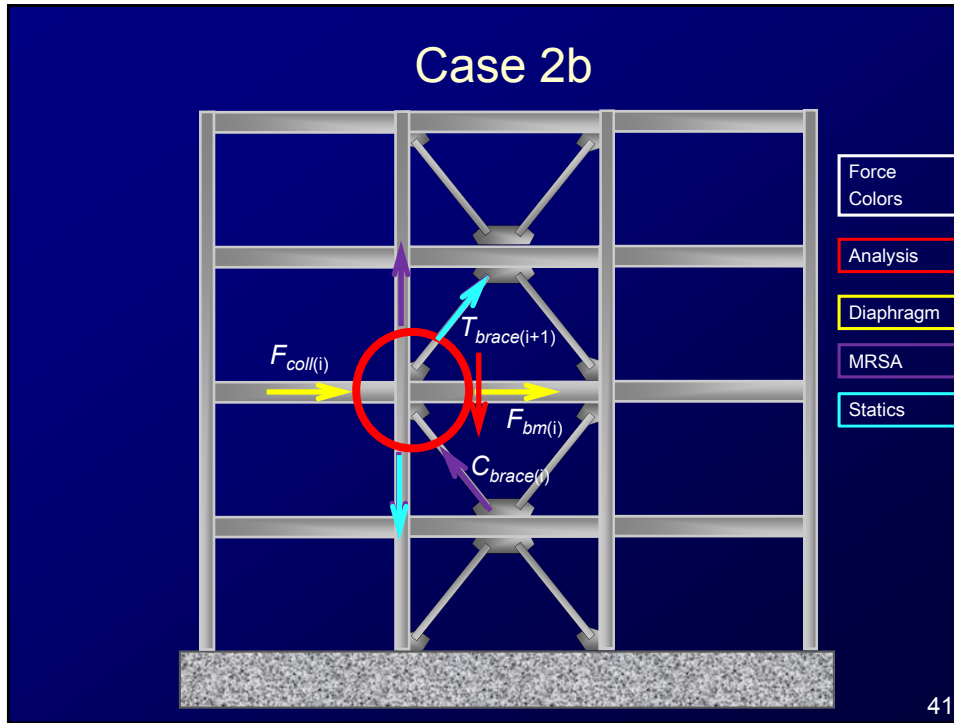
Modal combination gives forces

Use "Section Cuts" to obtain difference ( $V_i - V_{i+1}$ ) for each mode

Modal combination gives forces

Do not use the difference between  $V_{i+1}$  and  $V_i$  after modal combination





## A word about $\Omega_o$ ...

### Omegification

Do your analysis

Combine forces

Diaphragm collector forces

Transfer forces

Braced-frame beam forces

Omegify collector and collector connection forces

$\Omega_o$  is not limited to  $F_p$  forces

$\Omega_o$  is applied to critical, non-ductile (or not-very-ductile) elements

Braced-frame beam is a collector

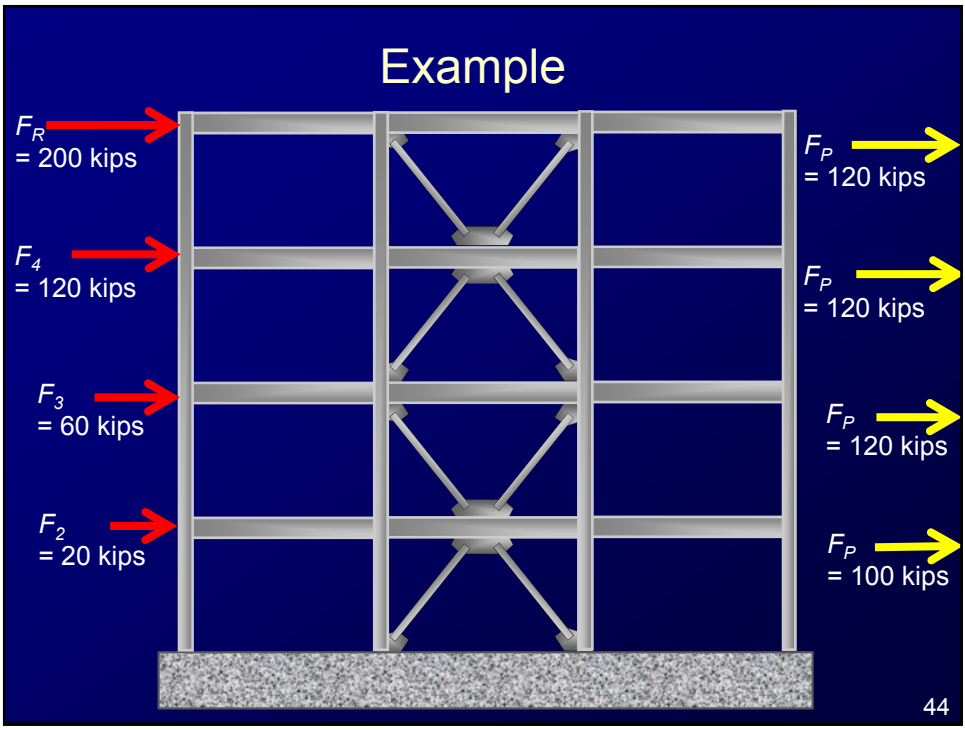

Wait until the end to combine with gravity loads

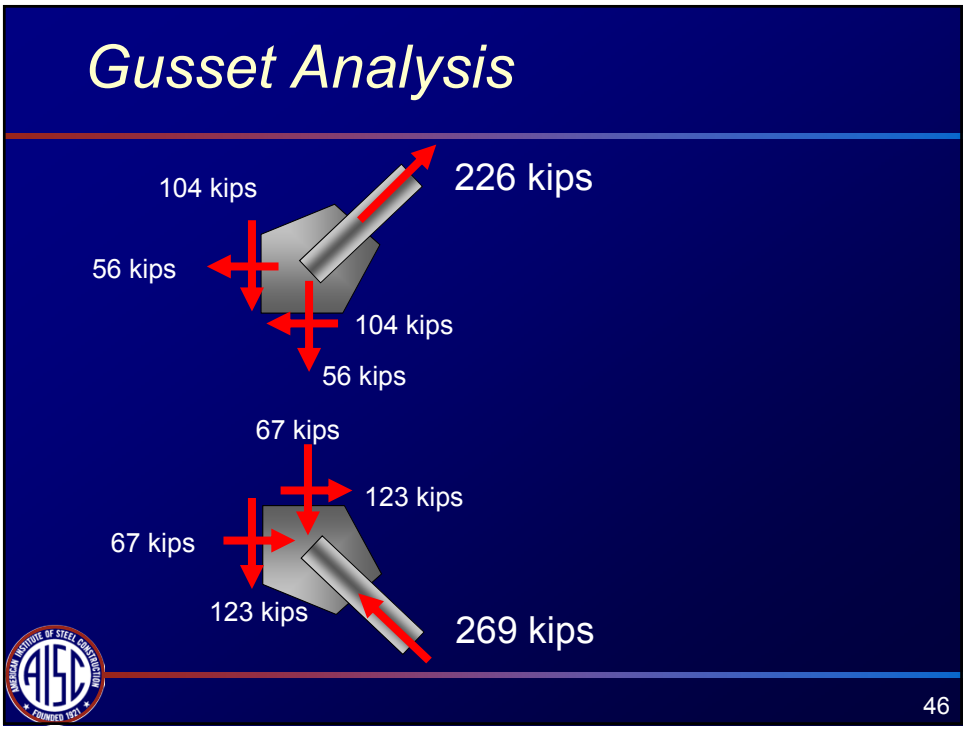
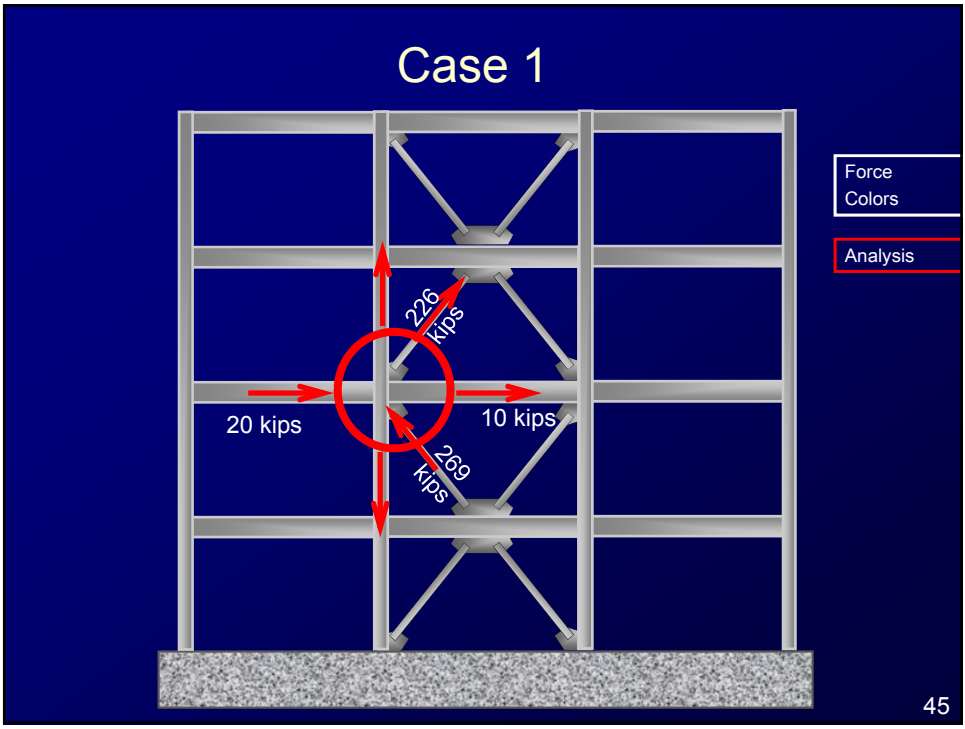


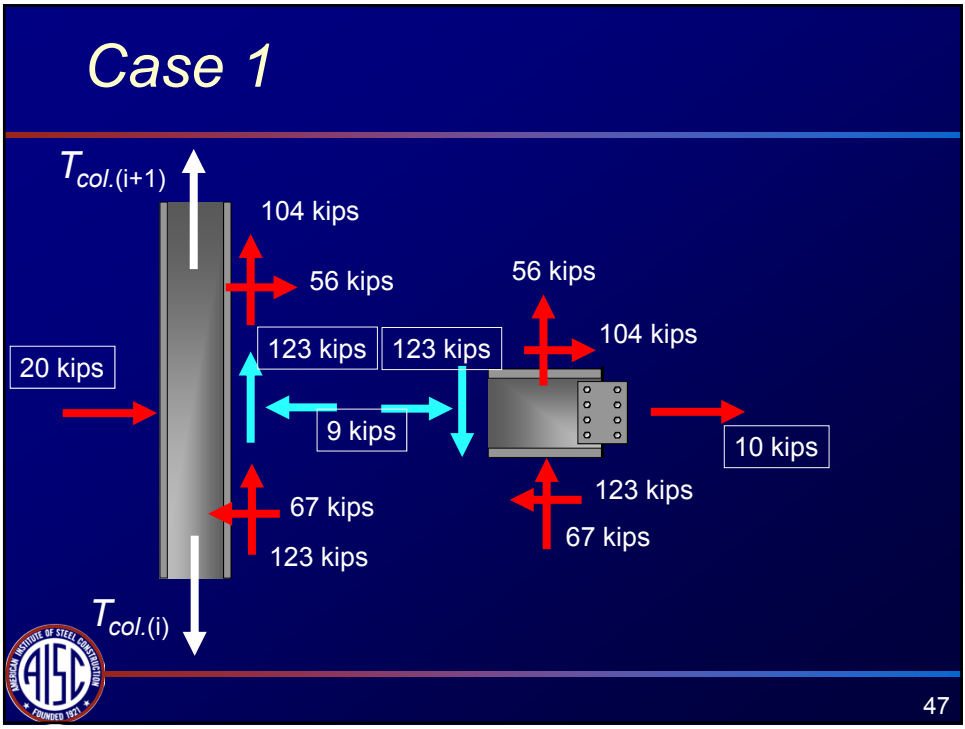
# Part III:

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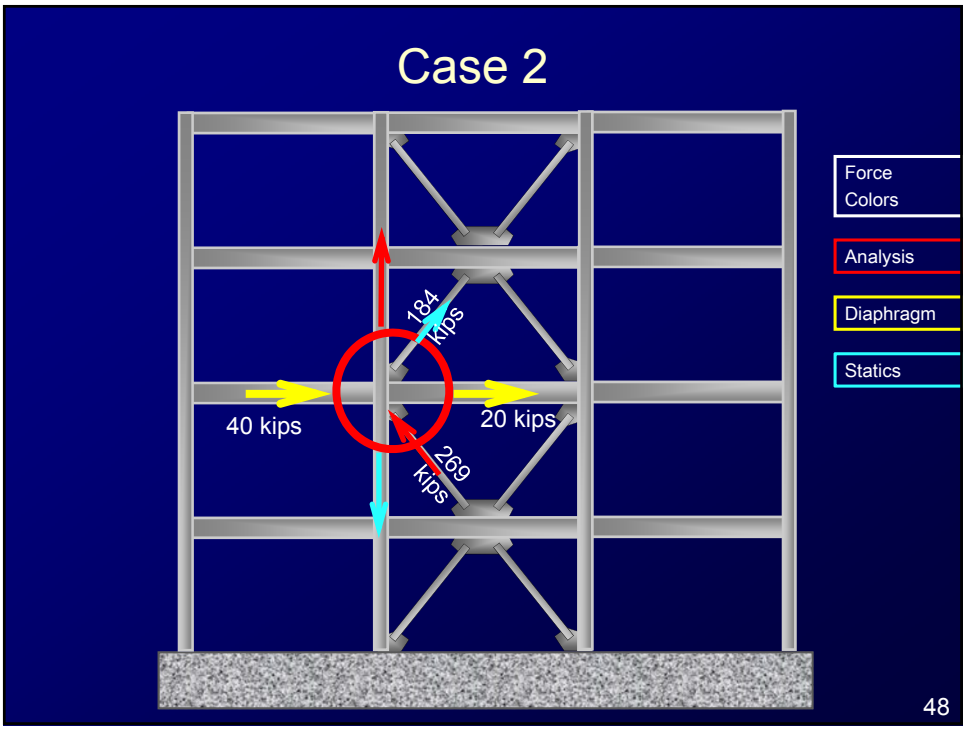
## Example: R3BF







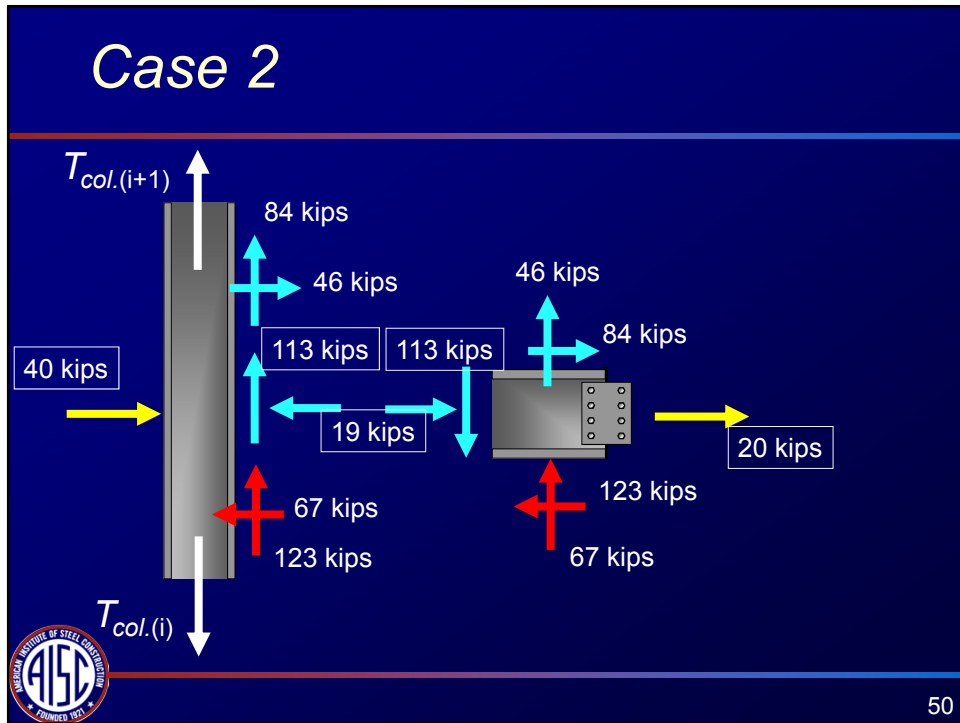
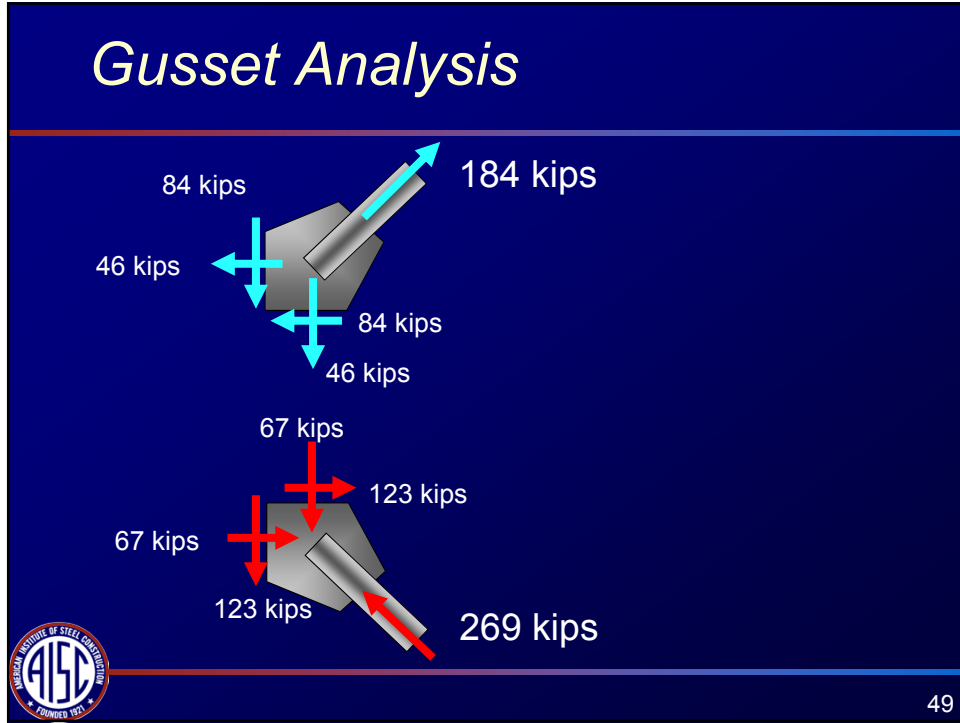
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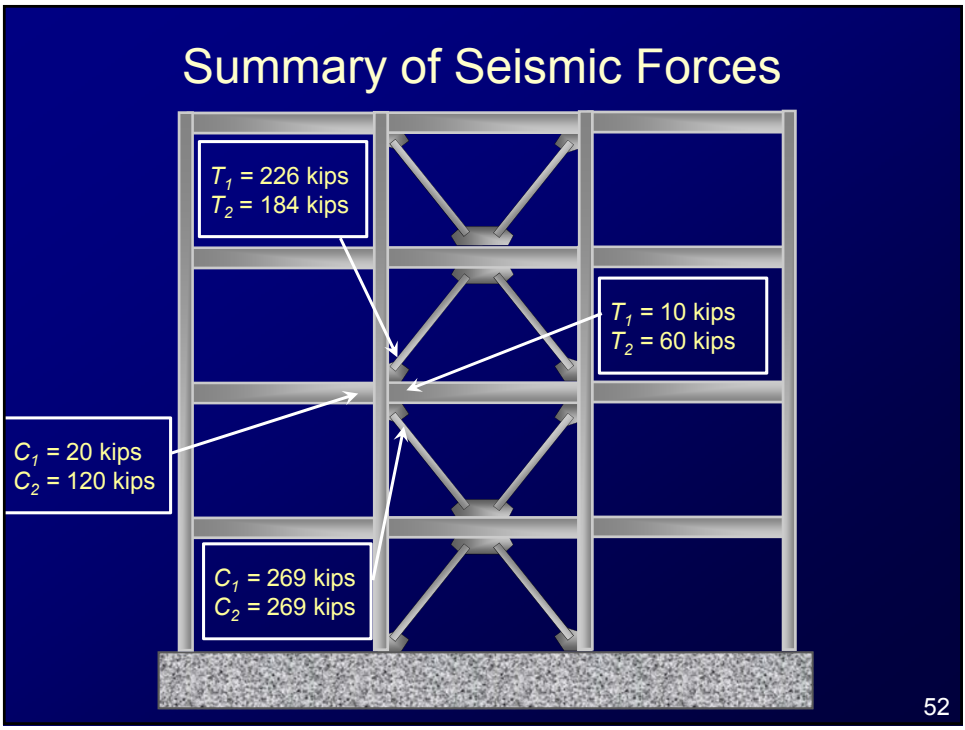
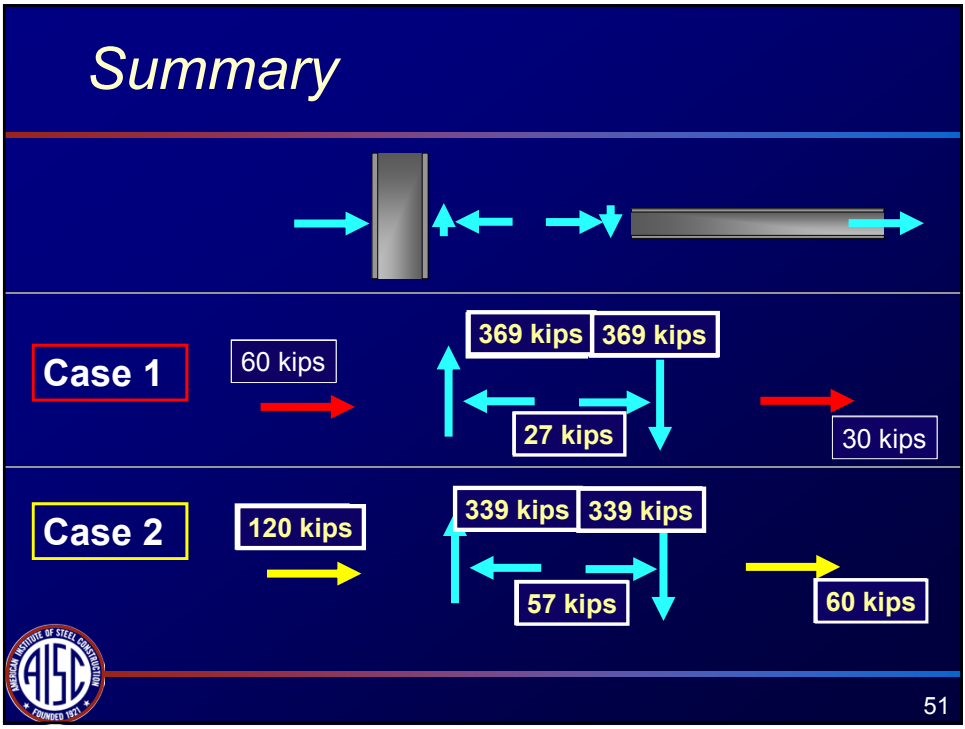


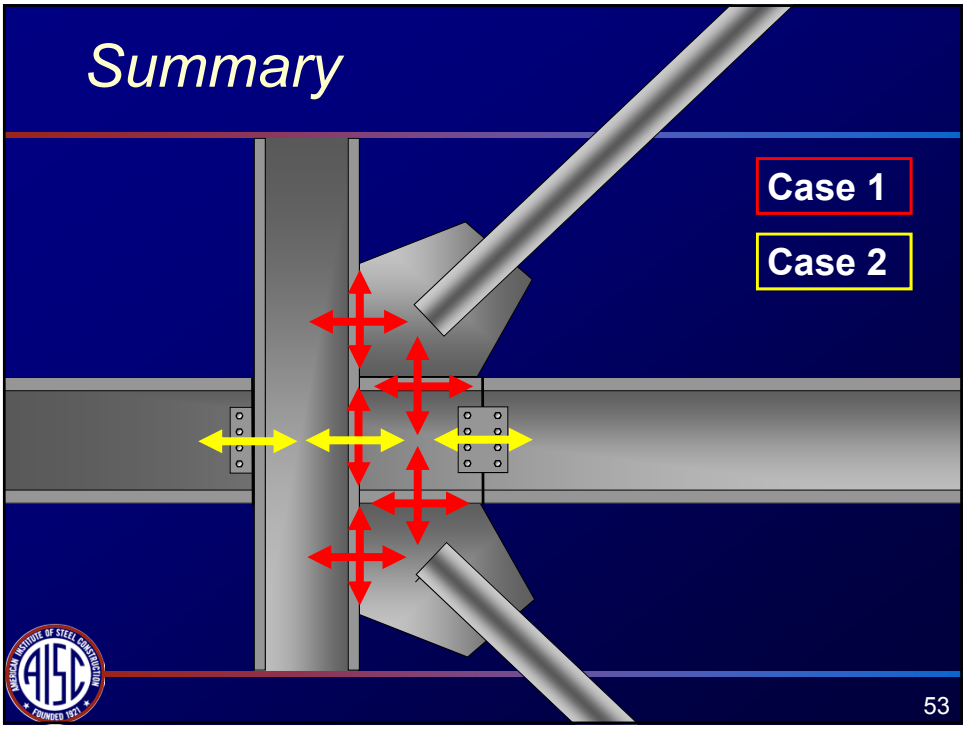
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# Part IV:

## Seismic $R=3.25$

# Seismic: $R=3.25$ (OCBF)

Vertical force distribution insufficient  
Connections designed for  $\Omega_o E$

## Case 1

Vertical force distribution  
Amplify all seismic forces by  $\Omega_o$   
*Collectors*  
*Braces*

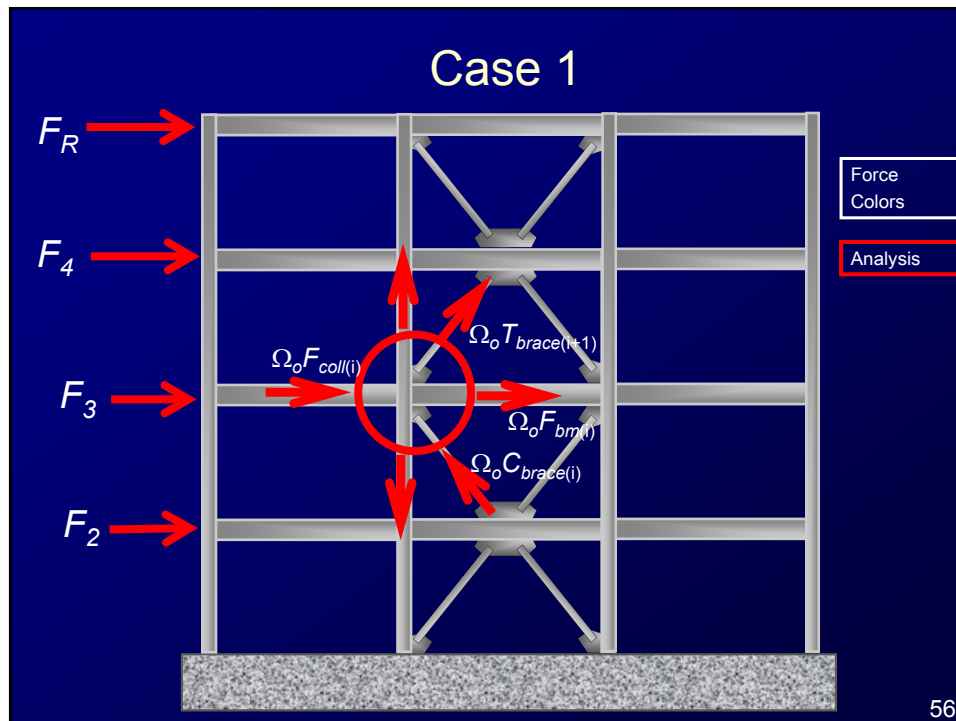
Statically consistent

## Case 2

Vertical force distribution with  $F_{p(i)}$  instead of  $F_i$   
Adjust seismic forces in brace above for static equilibrium  
Apply to  $\Omega_o$  collectors and connections

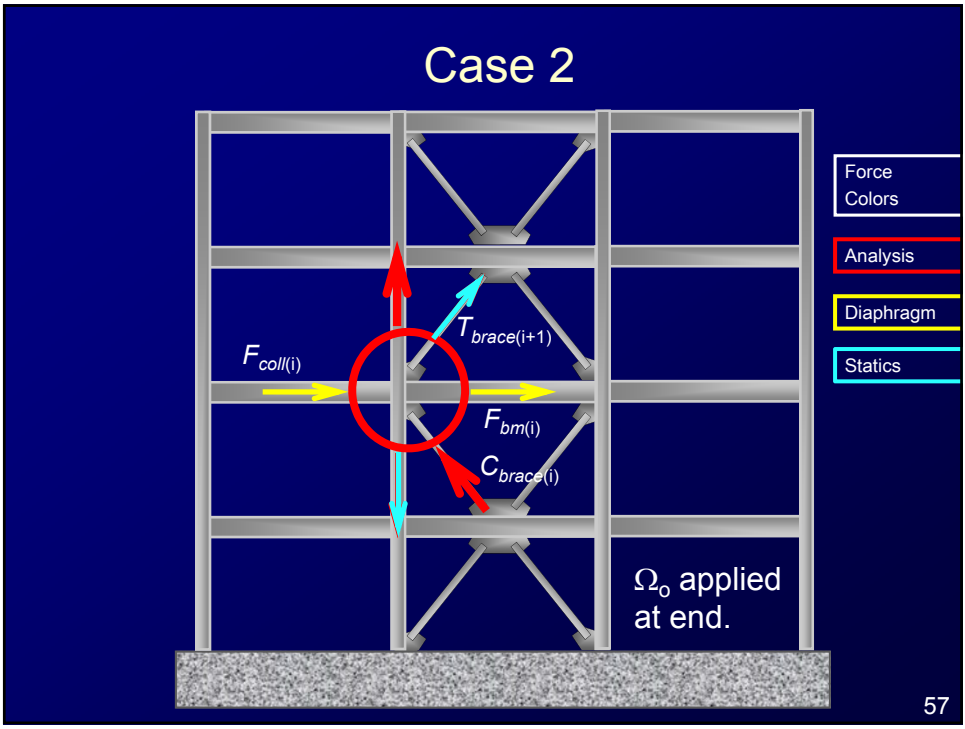


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# Part V:

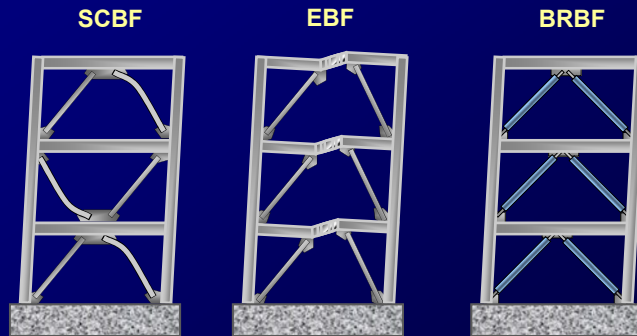
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# Seismic $R > 3.25$



## Seismic: $R > 3.25$

Vertical force distribution is insufficient  
Must anticipate system yielding mechanisms



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## Seismic: $R > 3.25$

### Case 1

Vertical force distribution superseded by system yield mechanism

Substitute forces corresponding to yield capacity

### Case 2

System yield mechanism with  $F_p$

### System-level analysis

Capture a mechanism

$\Omega_o$  superseded by mechanism analysis

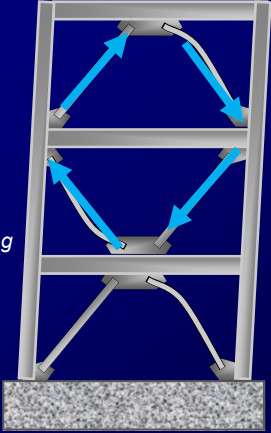


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## SCBF


$T_{brace(i+1)} = T_{max}$   
 $= R_y F_y A_g$   
 AISC 341 F2.3

$C_{brace(i)} = C_{max}$   
 $= F_{cr(expected)} A_g$   
 AISC 341 F2.3



$C_{brace(i+1)}$

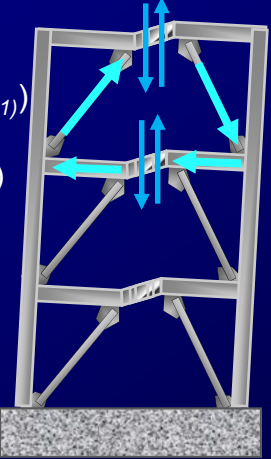
$T_{brace(i)}$


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## EBF


$T_{brace(i+1)} = T_{max}$   
 $= F(V_{n(i+1)})$

$C_{beam(i)} = F(V_{n(i)})$



$V_{n(i+1)} \leq 1.25 \cdot 0.6 R_y F_y A_w$   
 $\leq 1.25 \cdot 2 R_y F_y Z / e$   
 AISC 341 F3.3

$V_{n(i)} \leq 1.25 \cdot 0.6 R_y F_y A_w$   
 $\leq 1.25 \cdot 2 R_y F_y Z / e$


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# BRBF

$$T_{brace(i+1)} = T_{max} = 1.1 \omega R_y F_y A_{sc}$$

AISC 341 F4.3

$$C_{brace(i)} = C_{max} = 1.1 \beta \omega R_y F_y A_{sc}$$

AISC 341 F4.3

$C_{brace(i+1)}$

$T_{brace(i)}$

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## Seismic: $R > 3.25$ ; Case 1

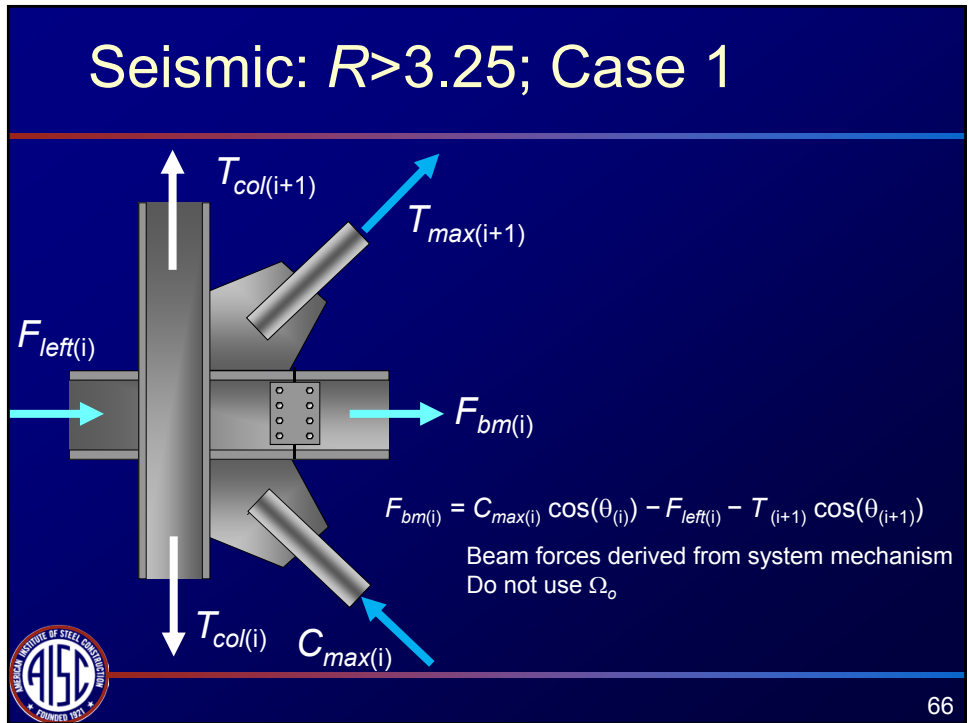
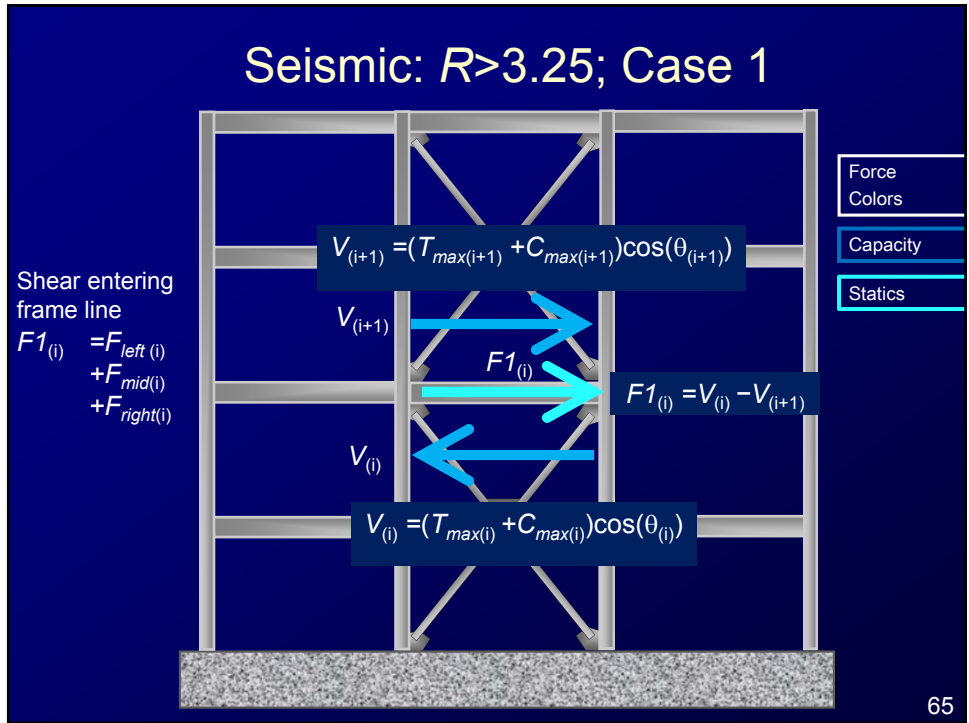
Shear entering frame line

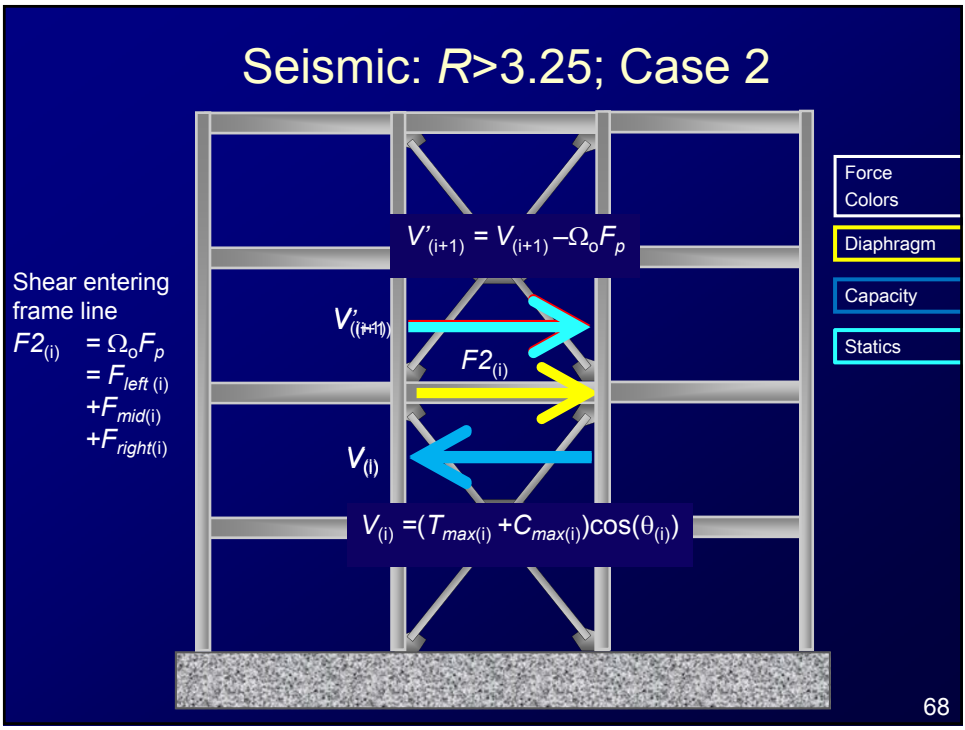
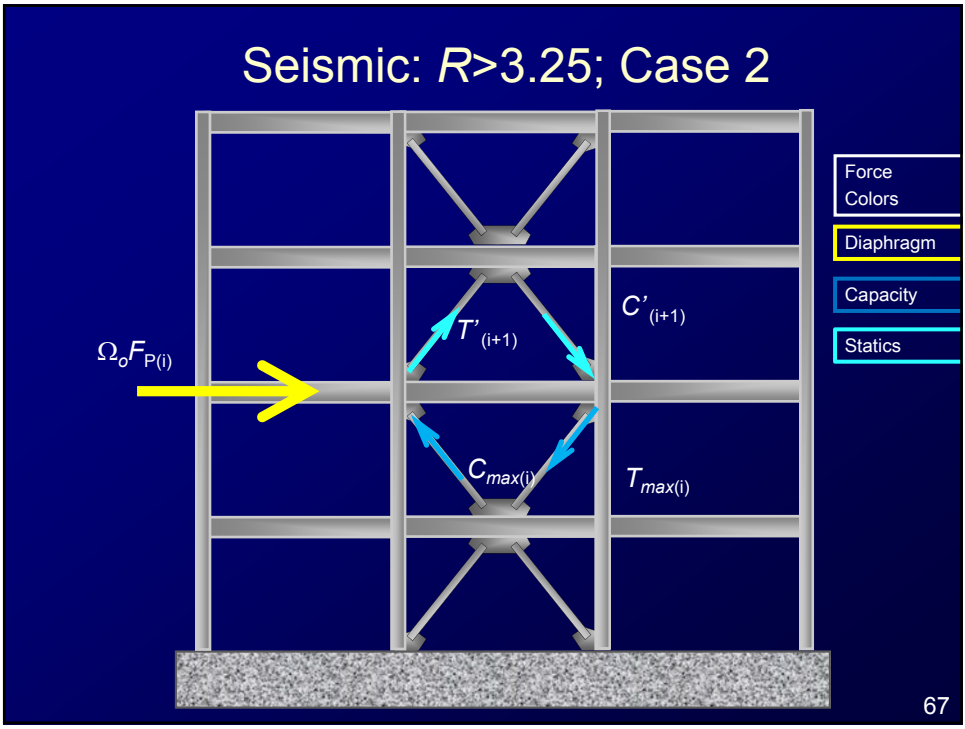
$$F1_{(i)} = F_{left(i)} + F_{mid(i)} + F_{right(i)}$$

Force
Colors
Capacity
Statics

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## Seismic: $R > 3.25$ ; Case 2

$T'_{(i+1)} = \frac{1}{2} V'_{(i+1)} / \cos(\theta_{(i+1)})$

$F_{bm(i)} = C_{max(i)} \cos(\theta_{(i)}) - F_{left(i)} - T'_{(i+1)} \cos(\theta_{(i+1)})$

Beam forces derived from system mechanism  
 Do not use  $\Omega_o$  on top of  $\Omega_i$




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## EBF: Coupled link beams

$T_{brace(i+1)} = T_{max} = F(V_{n(i)})$

$T_{brace(i)} = T_{max} = F(V_{n(i)})$

$V_{n(i)} \leq 1.25 * 0.6 R_y F_y A_w$   
 $\leq 1.25 * 2 R_y F_y Z / e$

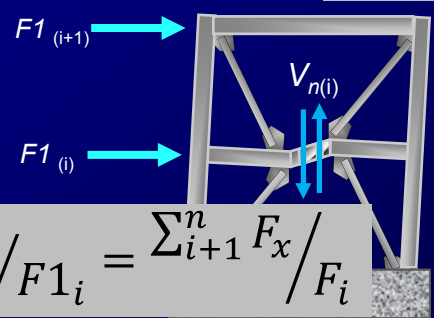


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# EBF: Coupled link beams

$$F1_{(i+1)} (h_i + h_{i+1}) + F1_{(i)} h_i = V_{n(i)} L_i$$

$$F2_{i+1} / F2_i = \sum_{i+1}^n F_x / F_{p_i}$$



$$F1_{i+1} / F1_i = \sum_{i+1}^n F_x / F_i$$

One engineer's approach:

Case 1:  
 Use vertical distribution.

Case 2:  
 Use vertical distribution with  $F_p$ .

Use distribution shapes.

Scale link shear capacity.



## Part VI:

## Post-buckled SCBF



# Post-buckled SCBF

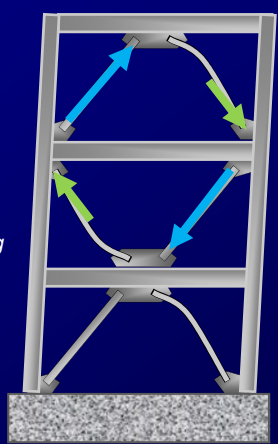
Vertical force distribution is insufficient  
 Must anticipate system yielding mechanisms  
 Case 1 for  $R > 3.25$  applies  
 Case 2 for  $R > 3.25$  applies  
 Include post-buckling condition  
 Case 3 required



# Post-buckled SCBF

$$T_{brace(i+1)} = T_{max} = R_y F_y A_g$$

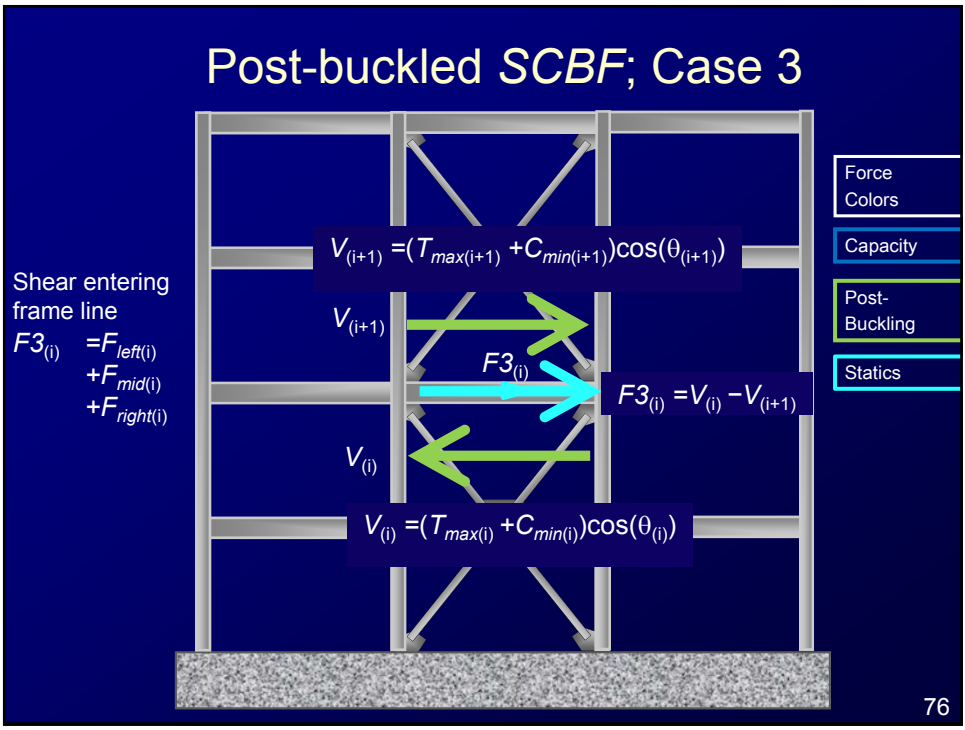
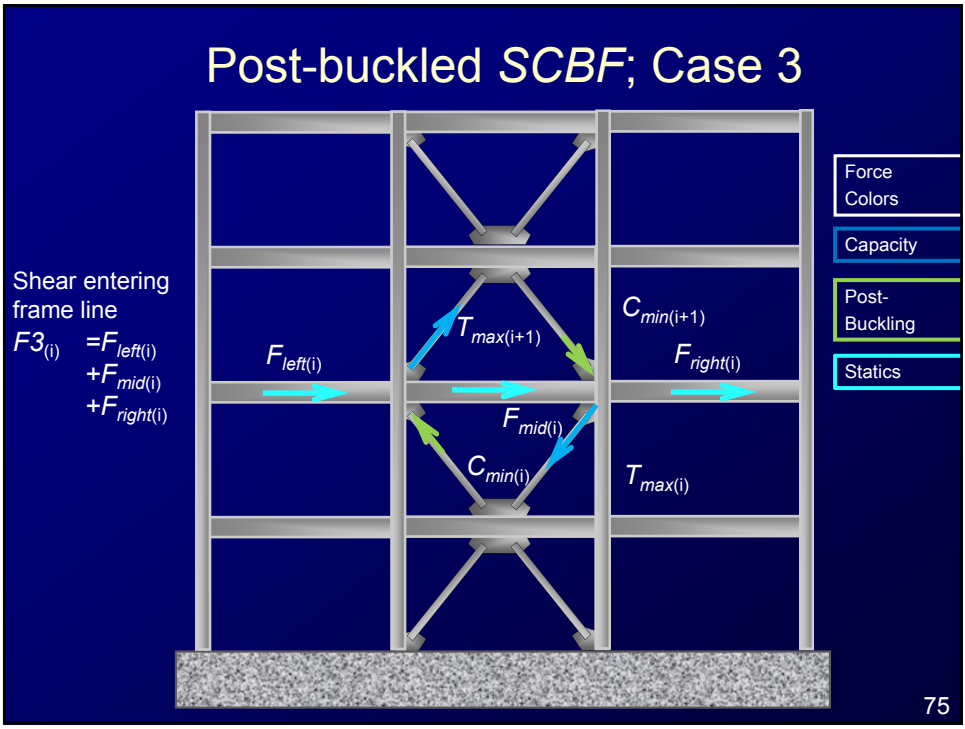
$$C_{brace(i)} = C_{min} = 0.3 F_{cr} A_g$$



$$C_{brace(i+1)} = C_{min} = 0.3 F_{cr} A_g$$

$$T_{brace(i)} = T_{max} = R_y F_y A_g$$






## Post-buckled SCBF; Case 3

$$F_{bm(i)} = F_{left(i)} + T_{max(i+1)} \cos(\theta_{(i+1)}) - C_{min(i)} \cos(\theta_{(i)})$$

$$T_{max} = R_y F_y A_g \quad C_{min} = 0.3 F_{cr} A_g$$

Beam forces derived from system mechanism  
 Do not use  $\Omega_o$




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## Post-buckled SCBF; Case 3

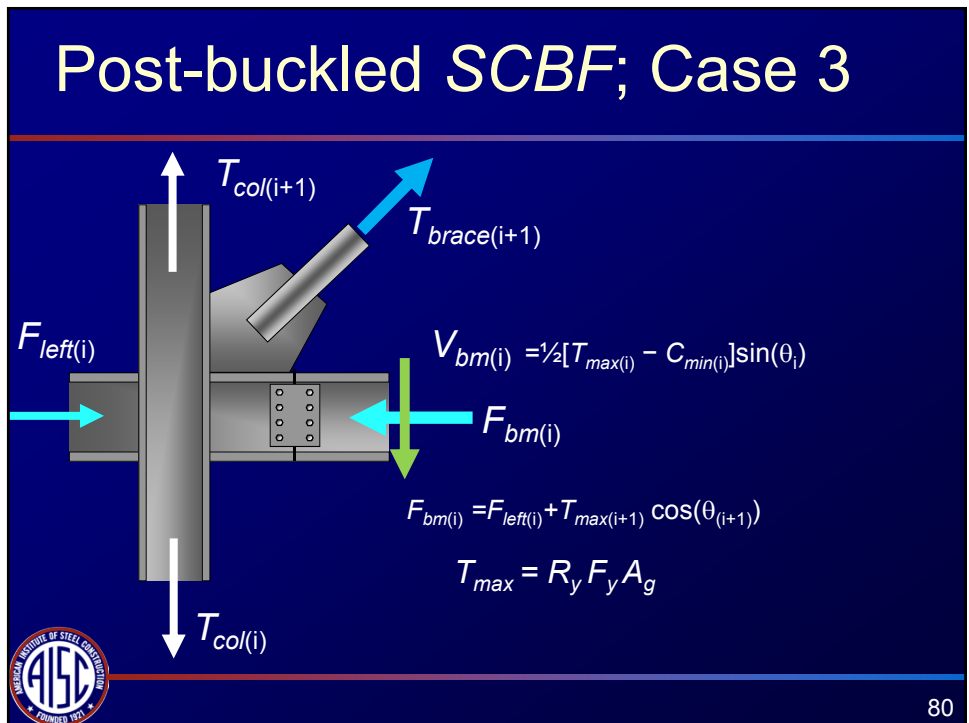
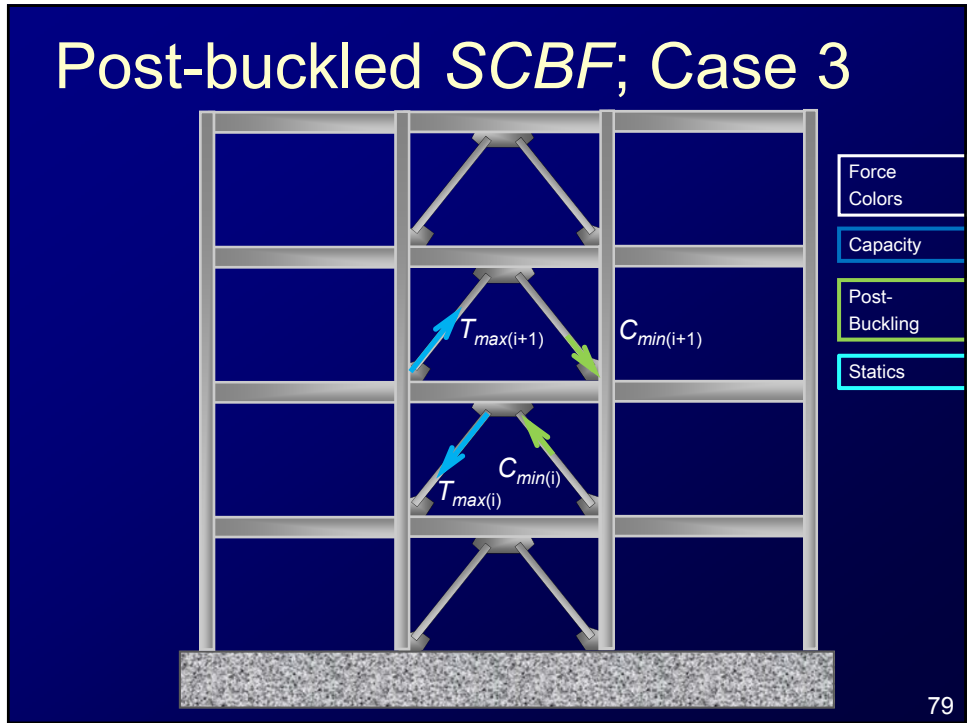
$$T_{brace(i+1)} = T_{max} = R_y F_y A_g$$

$$C_{brace(i+1)} = C_{min} = 0.3 F_{cr} A_g$$

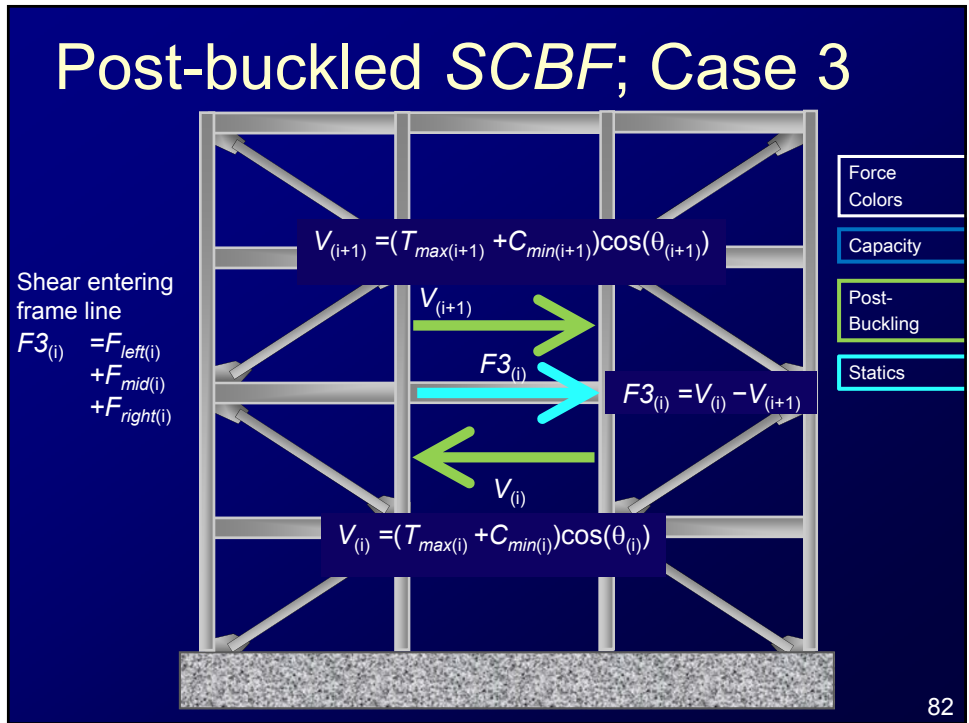
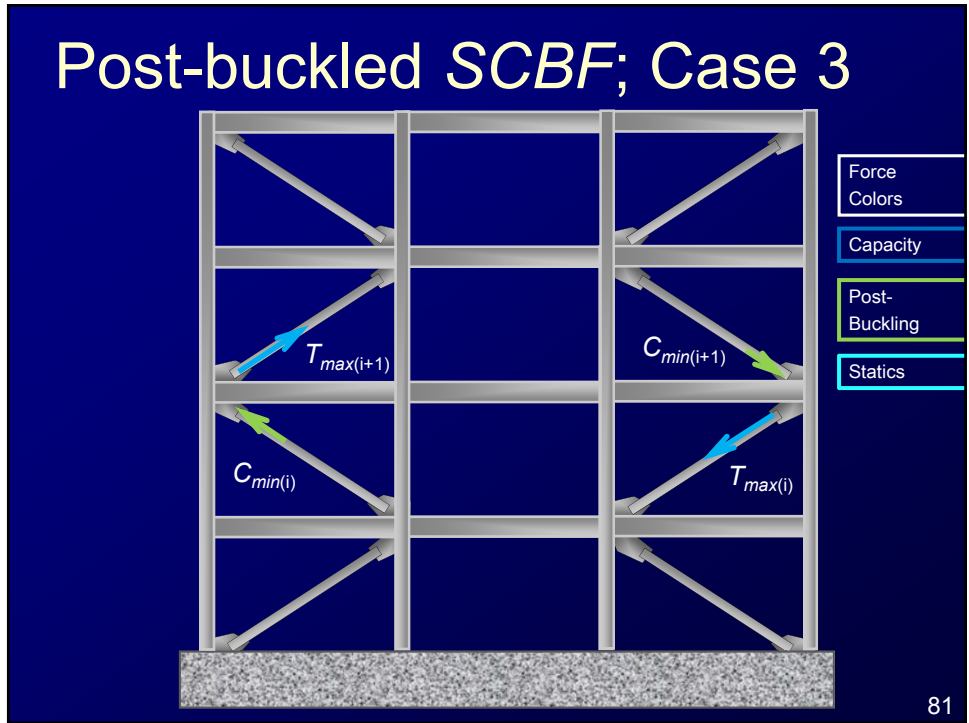
$$T_{brace(i)} = T_{max} = R_y F_y A_g$$

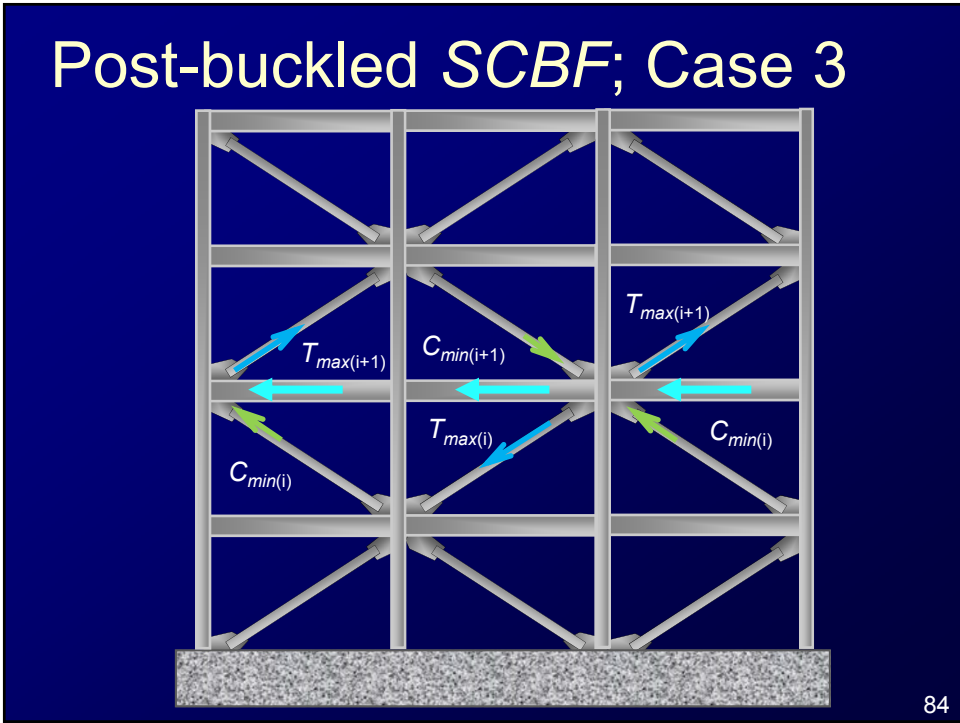
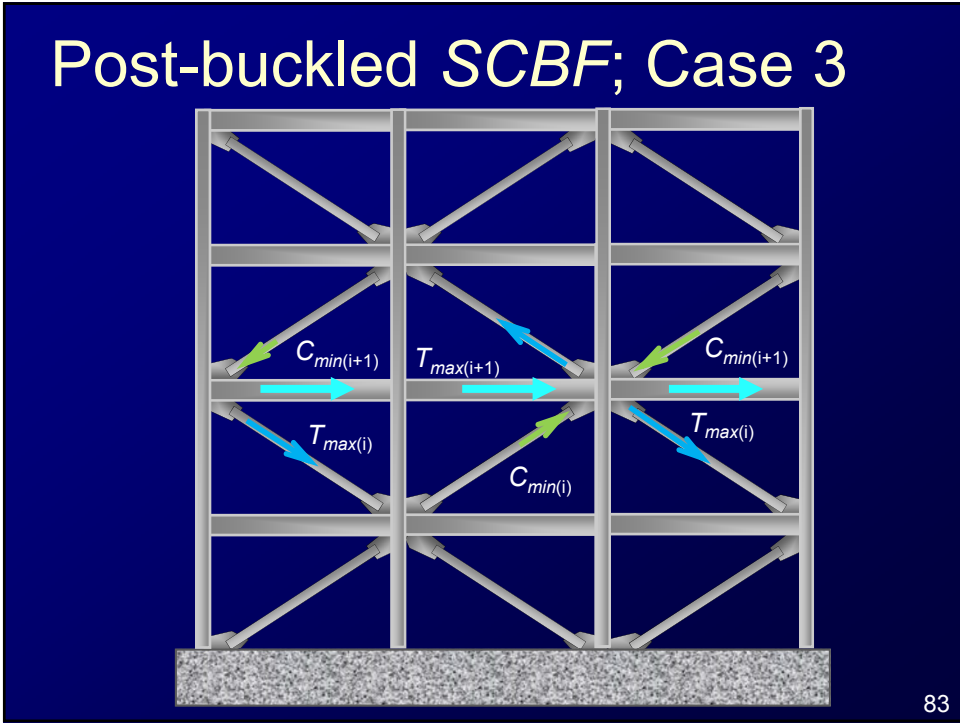
$$C_{brace(i)} = C_{min} = 0.3 F_{cr} A_g$$


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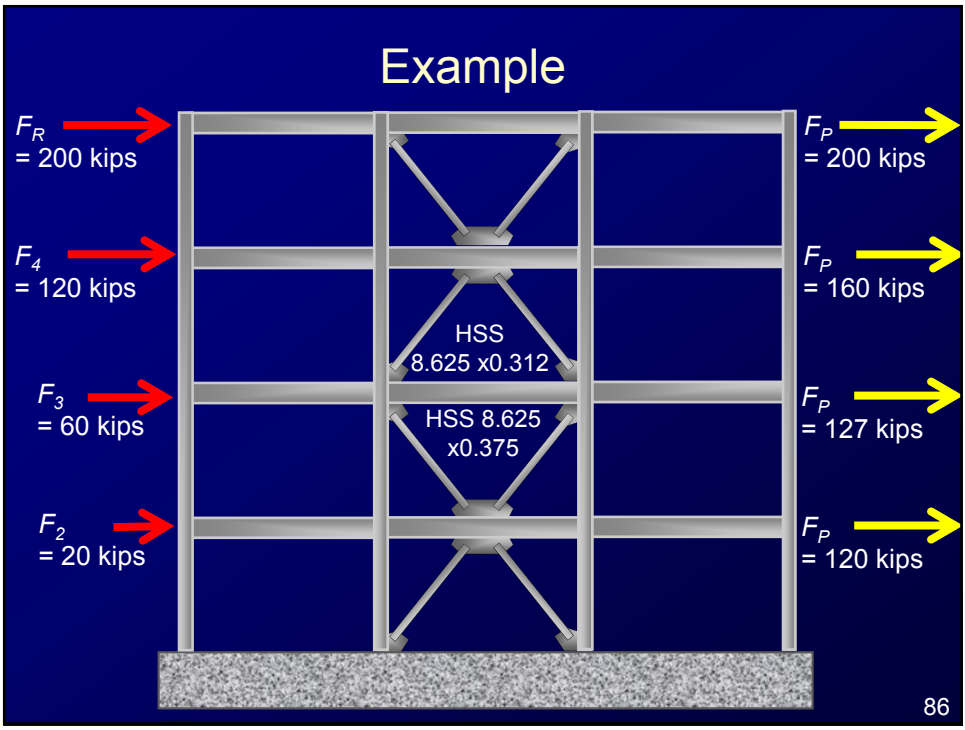



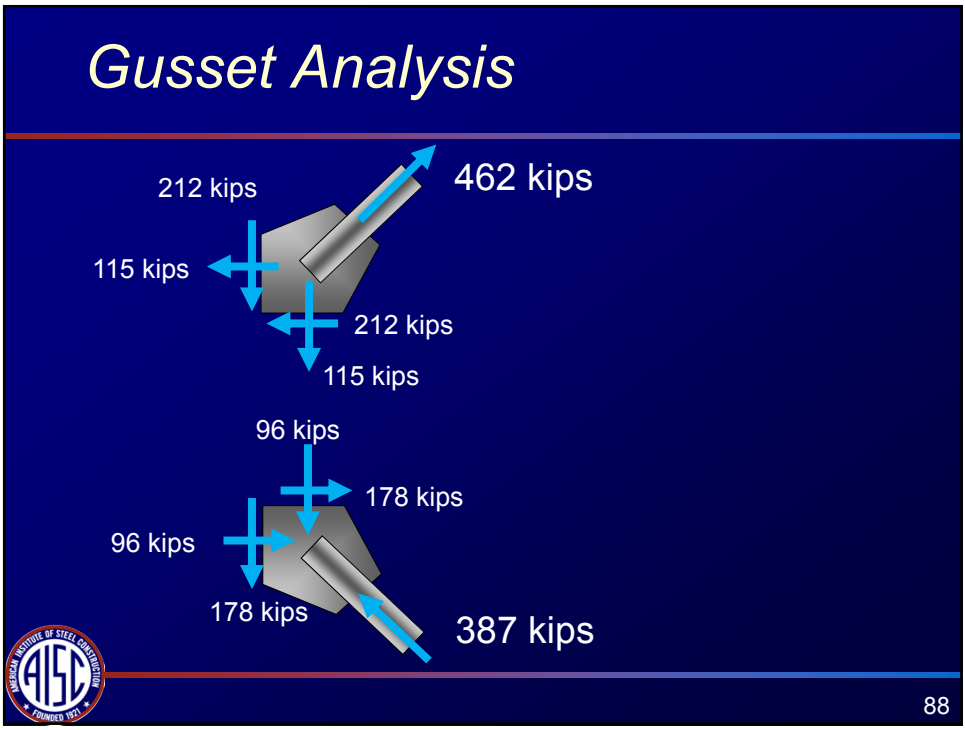
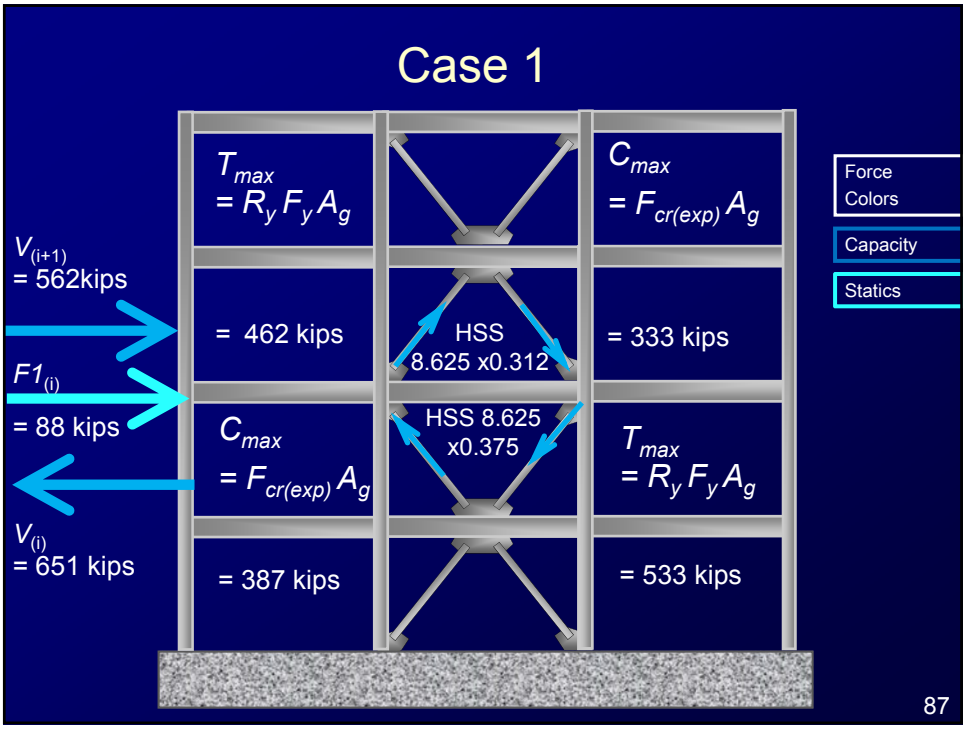


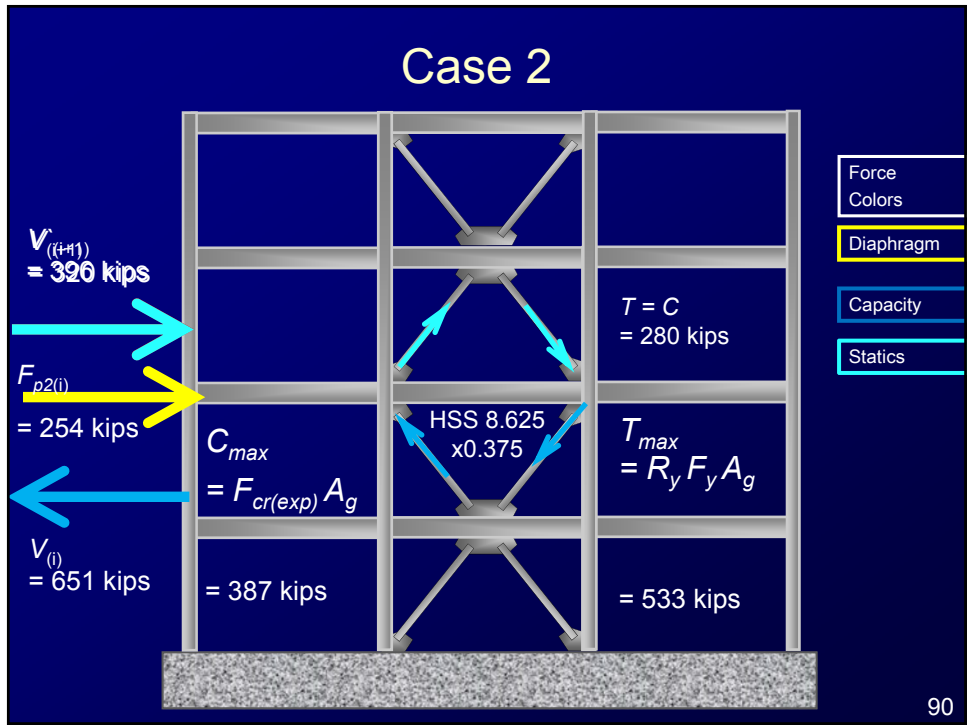
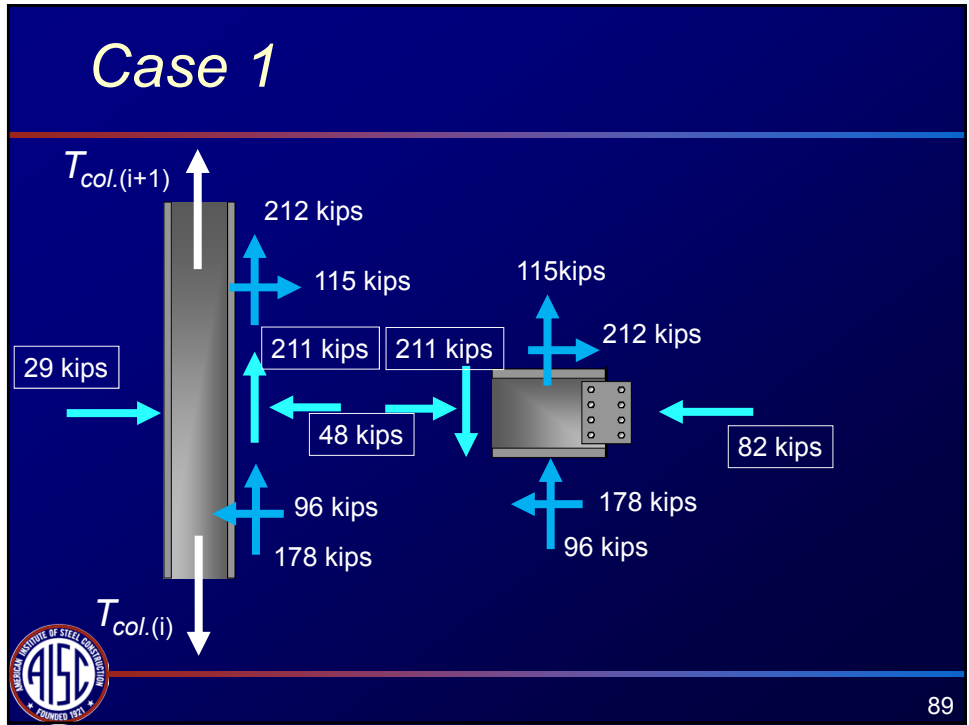
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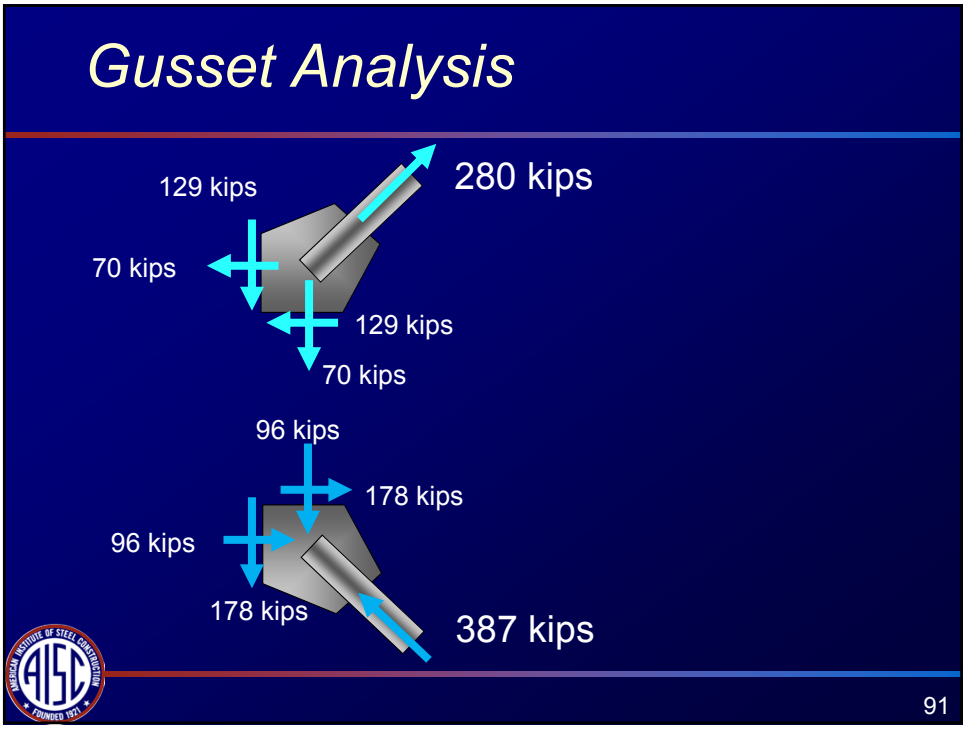
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## Example: SCBF

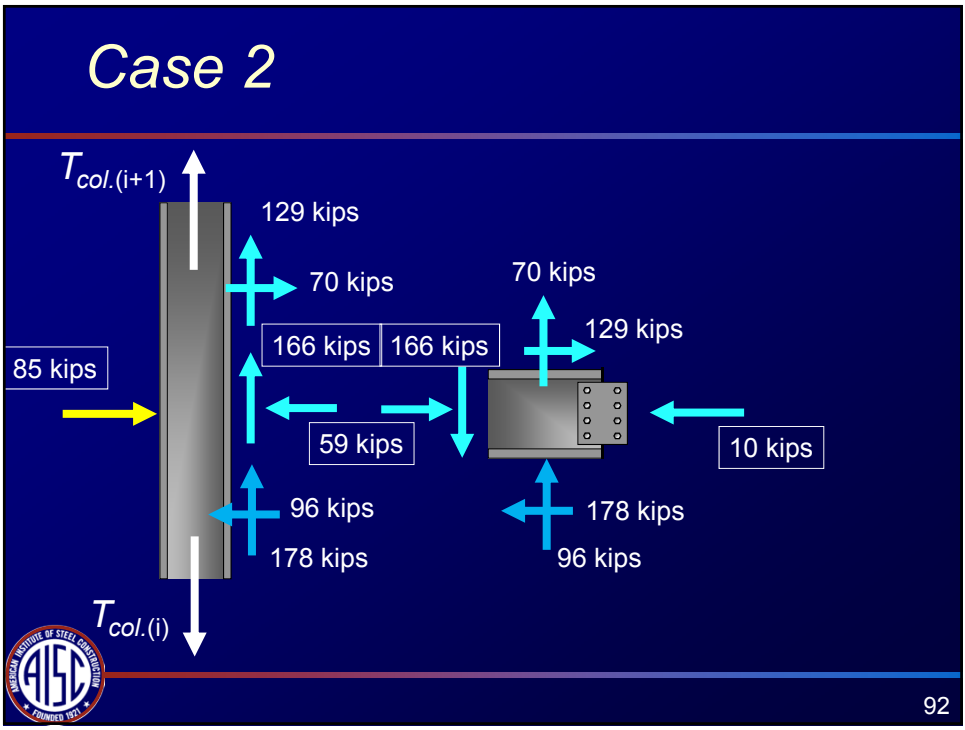






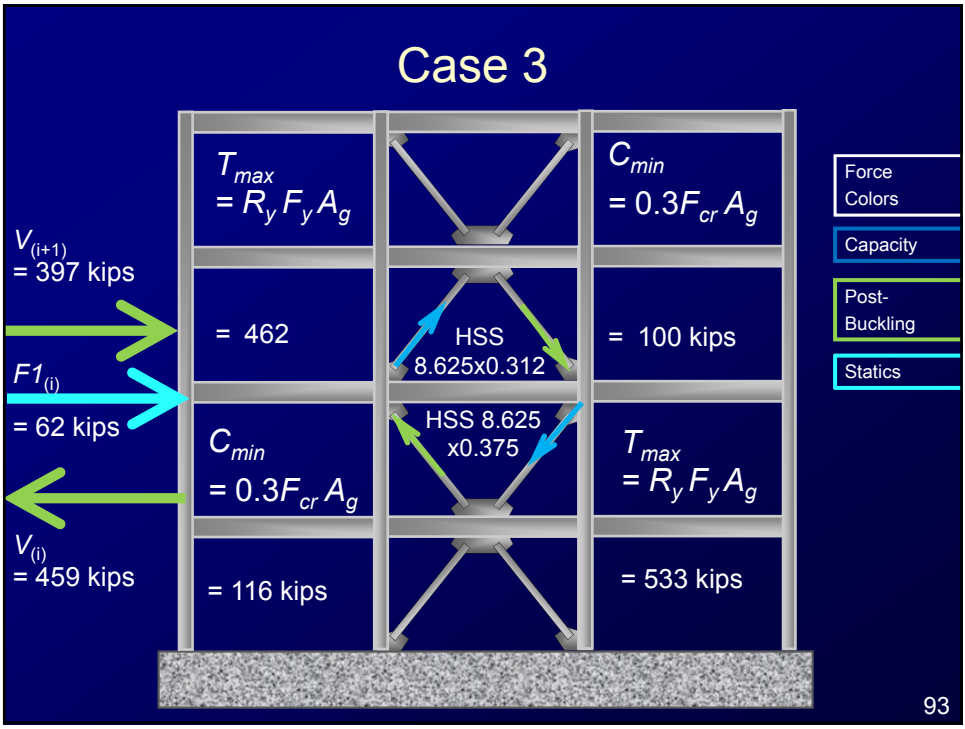


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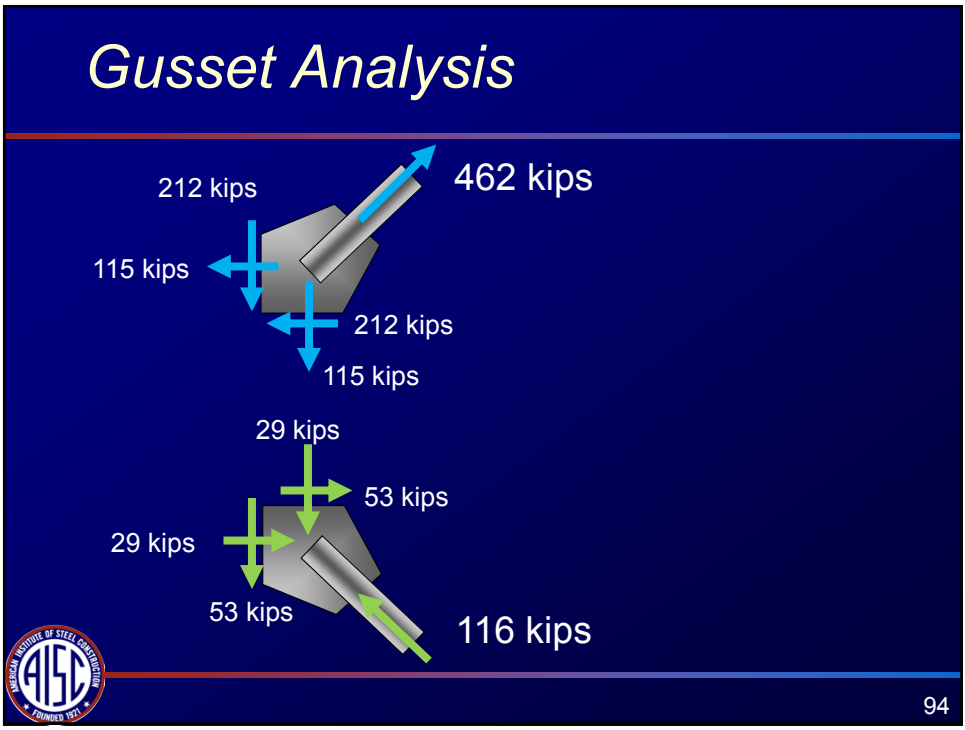


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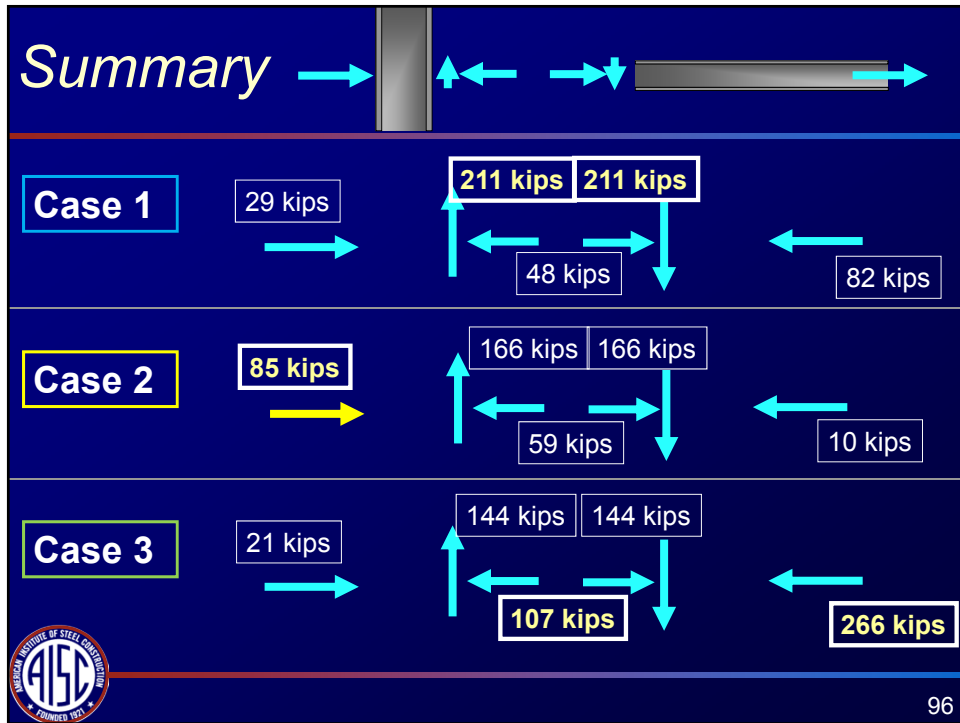
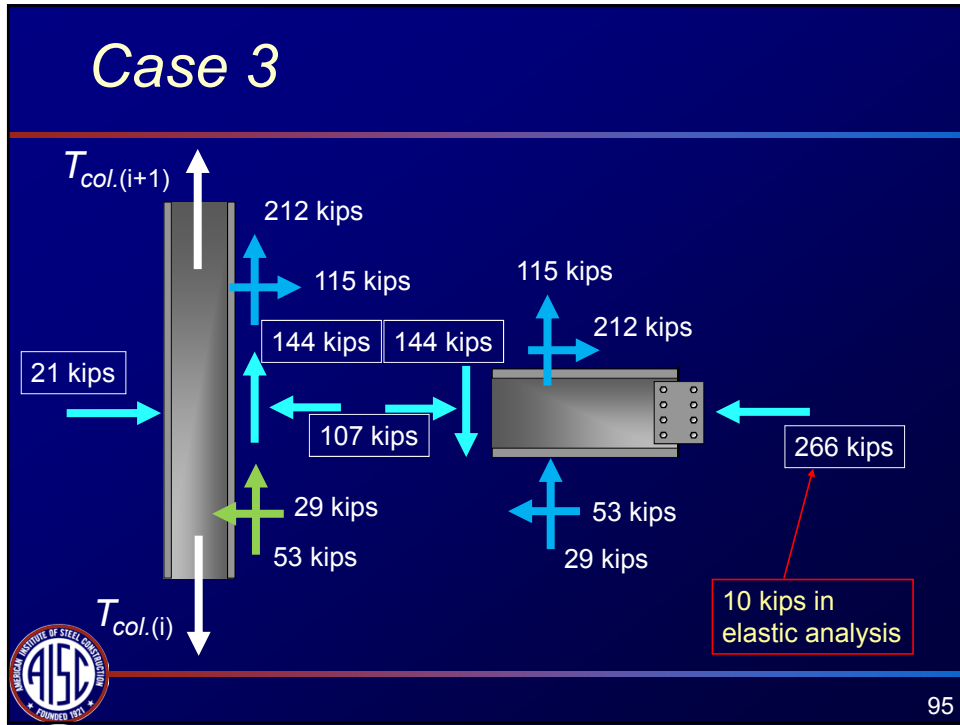


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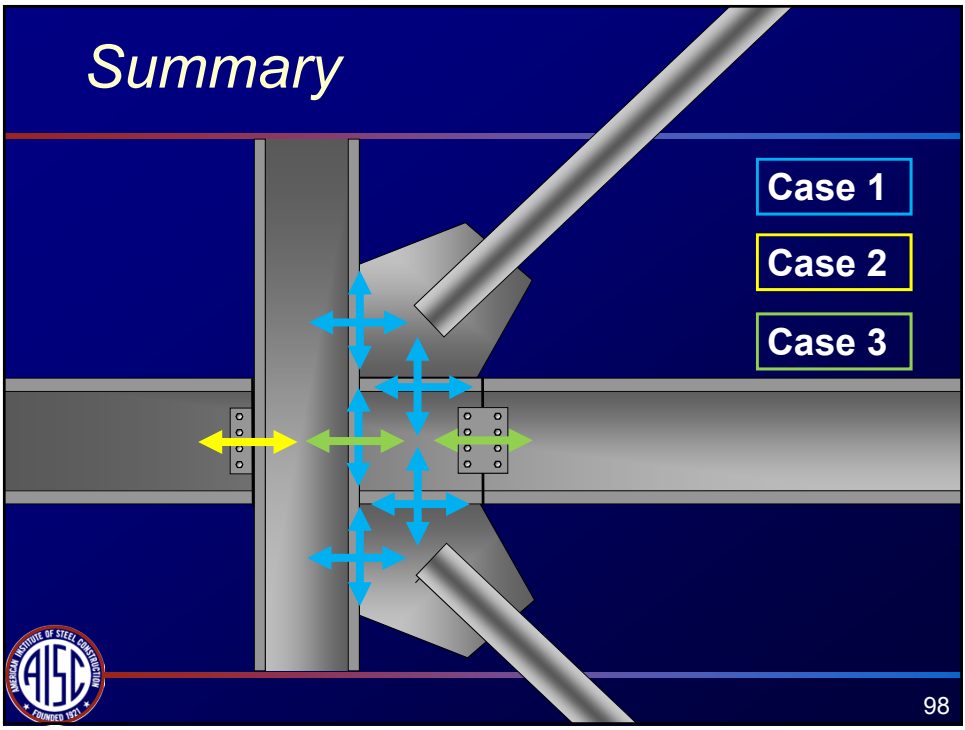
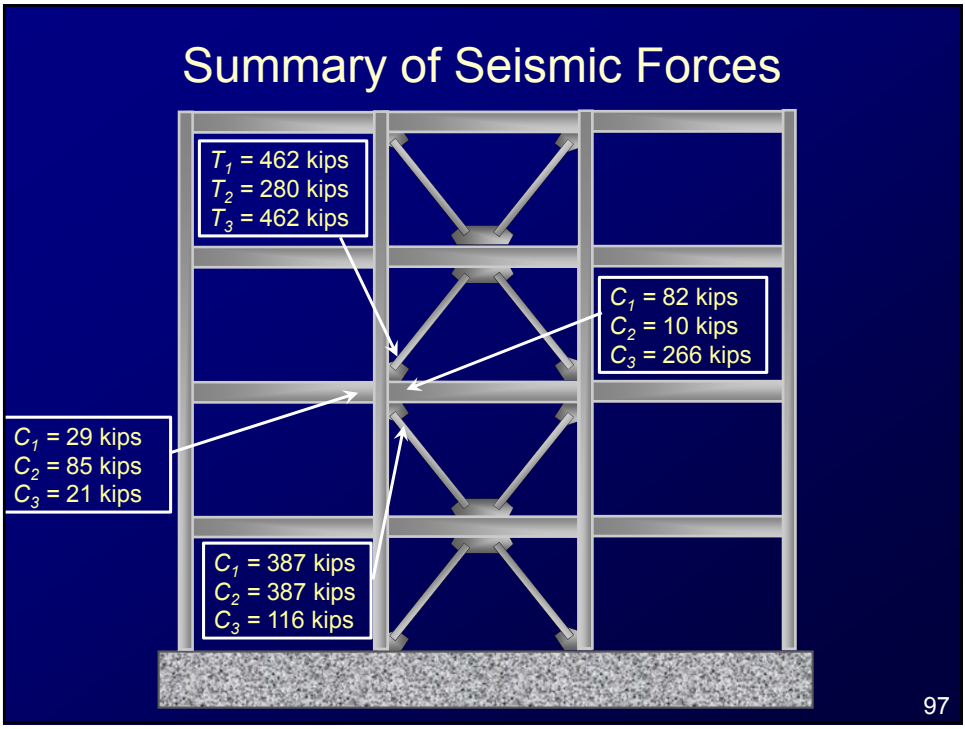


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# Conclusion



## *Conclusion*

3 types of forces must be reconciled in the design of braced-frame connections for lateral load

Base-shear forces                                      Wind,  $R=3$ ,  $R>3$

Equivalent lateral force  
Modal response spectrum analysis

Diaphragm accelerations                               $R=3$ ,  $R>3$

System yield mechanism forces                       $R>3$

Understanding the purpose of the design loads is key to meaningful application



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## Conclusion

Forces can be reconciled by envisioning two separate load cases (3 for SCBF)

### Case 1

Base-shear forces or mechanism forces

### Case 2

Diaphragm accelerations combined with base-shear forces or mechanism forces

Adjustments made to satisfy statics

Load Cases can be consolidated

Case 1 results in maximum vertical forces at connections

Case 2 *may* result in maximum horizontal forces at connections



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## Conclusion

### Omegification

R3BF (SDC C), OCBF

*Omegify all of E*

$R > 3$

*Use mechanism analyses*

*Supersedes  $\Omega_o$*

*$\Omega_o$  still applies for collector and diaphragm*



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Thank you



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- Completely fill out online form. Don't forget to check the boxes next to each attendee's name!



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